www.thp.uni-koeln.de/gravitation/courses/rci13.html

## 9<sup>th</sup> exercise sheet on Relativity and Cosmology I

Winter term 2013/14

Deadline for delivery: Thursday, 19th December 2013 during the exercise class.

## Exercise 24 (8 credit points): Dust

Derive the continuity equation and the Euler equation for dust given in the lecture within the framework of special relativity.

Furthermore, show that in an arbitrary reference frame it follows from the conservation of the energymomentum tensor of dust that dust particles move on geodesics.

## Exercise 25 (12 credit points): Ideal fluid

The energy–momentum tensor of an ideal fluid is given by

$$T^{\mu\nu} = \rho \, u^{\mu} u^{\nu} + P \left( u^{\mu} u^{\nu} + g^{\mu\nu} \right),$$

where  $u^{\mu}$  is the four-velocity,  $\rho$  is the density and *P* is the pressure of the fluid.

Use the fact that the energy–momentum tensor of an ideal fluid is divergence-free to derive the continuity equation and the Euler equation.

Furthermore, write out the continuity equation for the metric

$$g_{\mu\nu} = \text{diag}\left[-1, a(t)^2, a(t)^2, a(t)^2\right].$$