

Quantum computing “al dente”

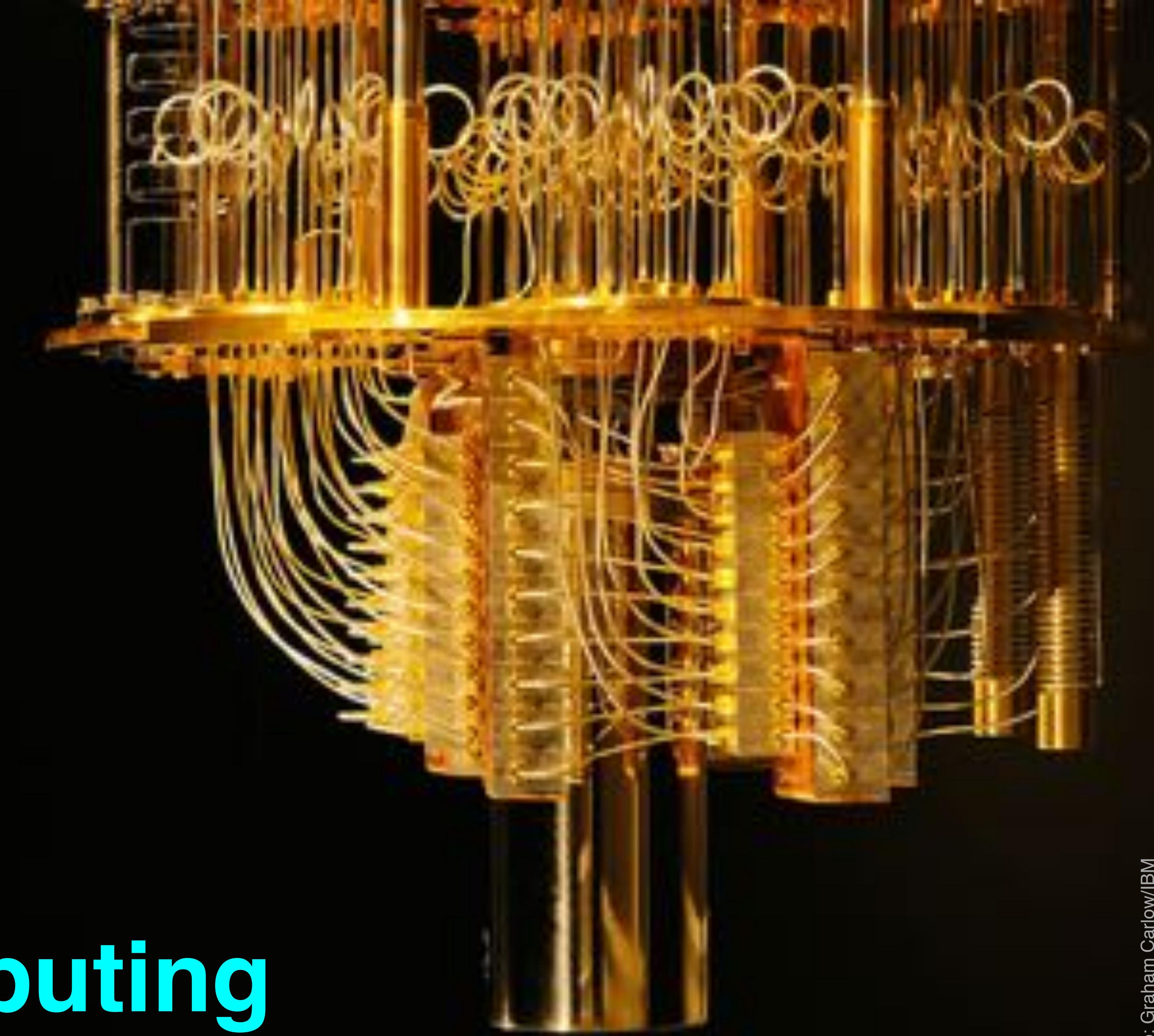
Simon Trebst
University of Cologne



Flatiron Institute
New York, July 2022

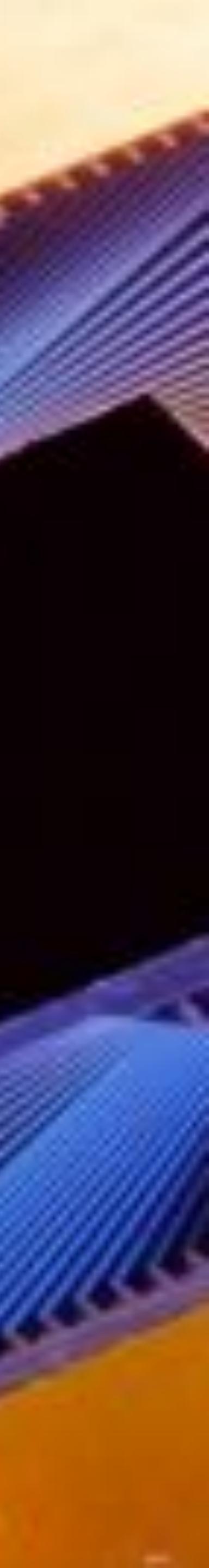


Quantum computing





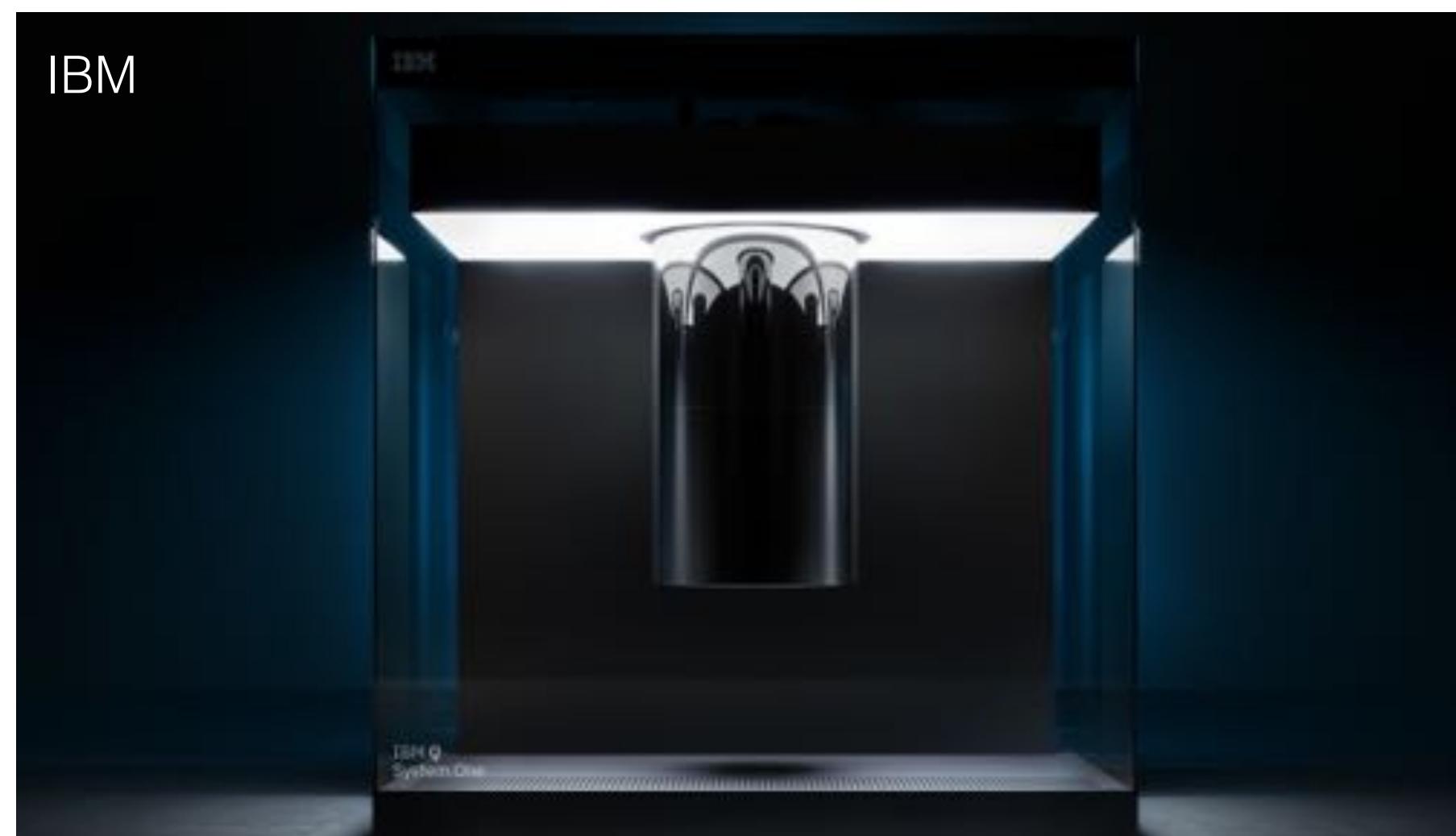
analog
devices



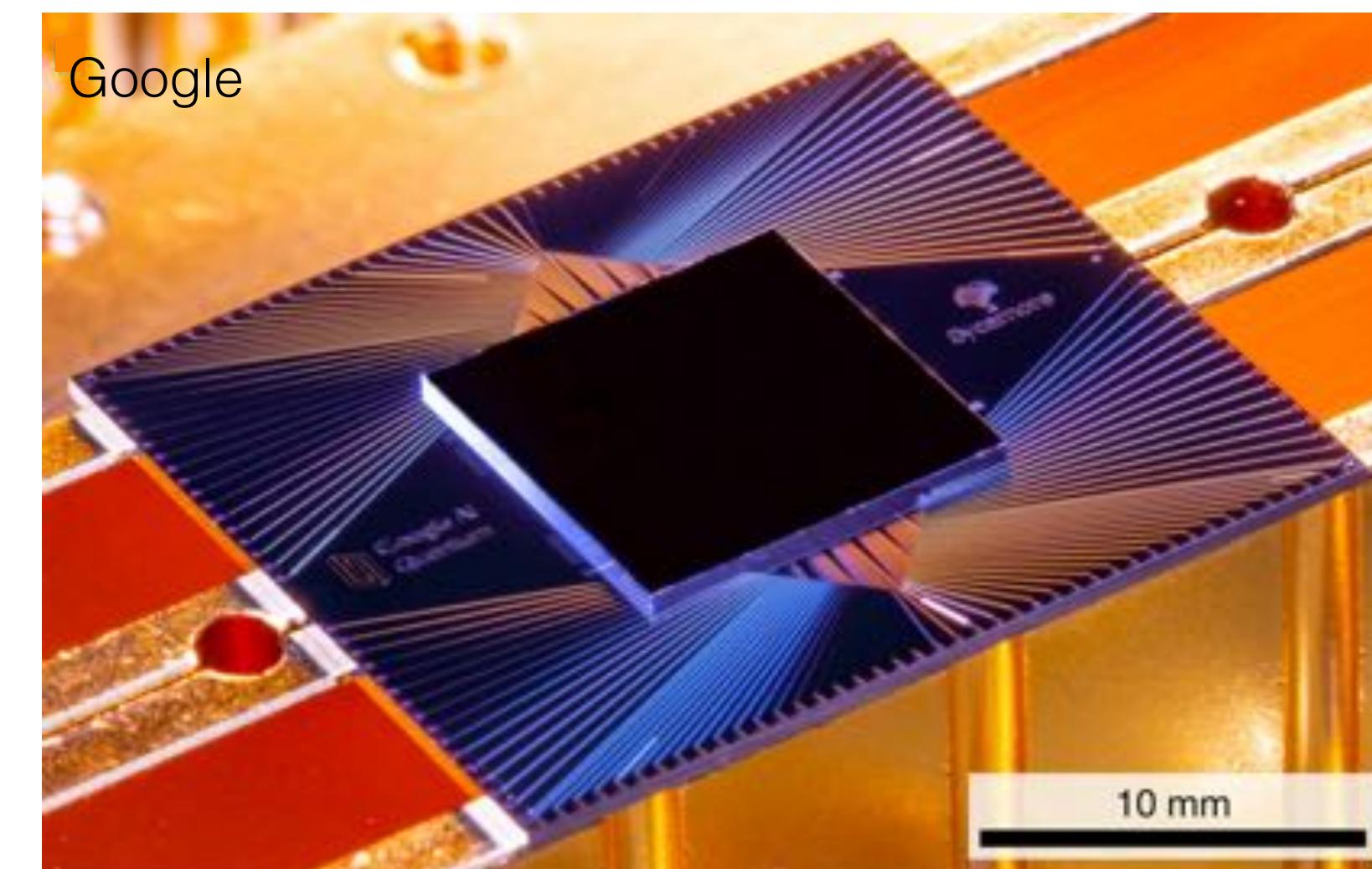
2020's: the NISQ era

An experimental pivot from of a **few pristine qubits**
to the realization of circuit architectures of **50-100 qubits**
but tolerating a significant level of **imperfections**.

→ **noisy intermediate scale quantum devices**

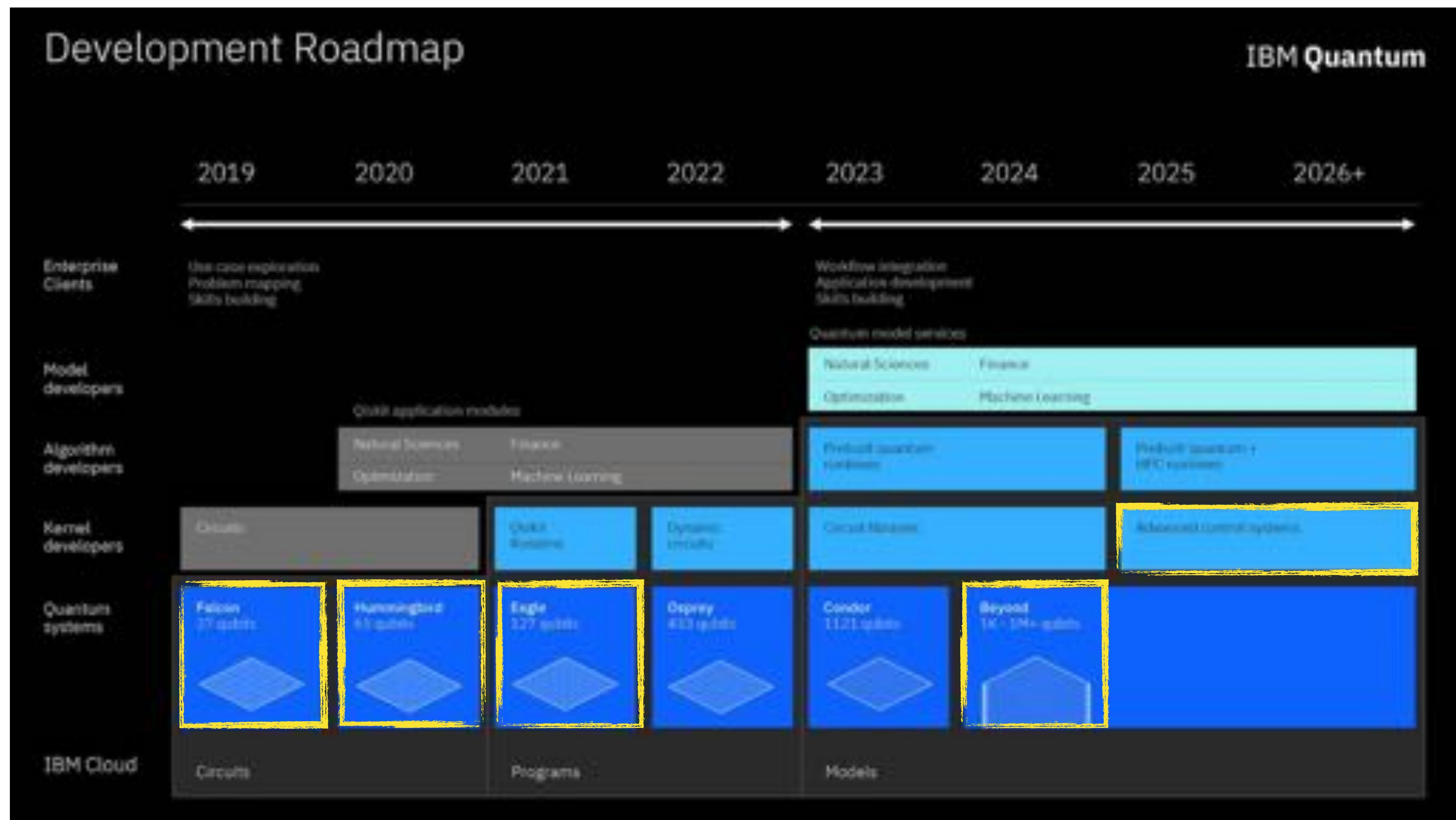


Eagle generation — 127 qubits



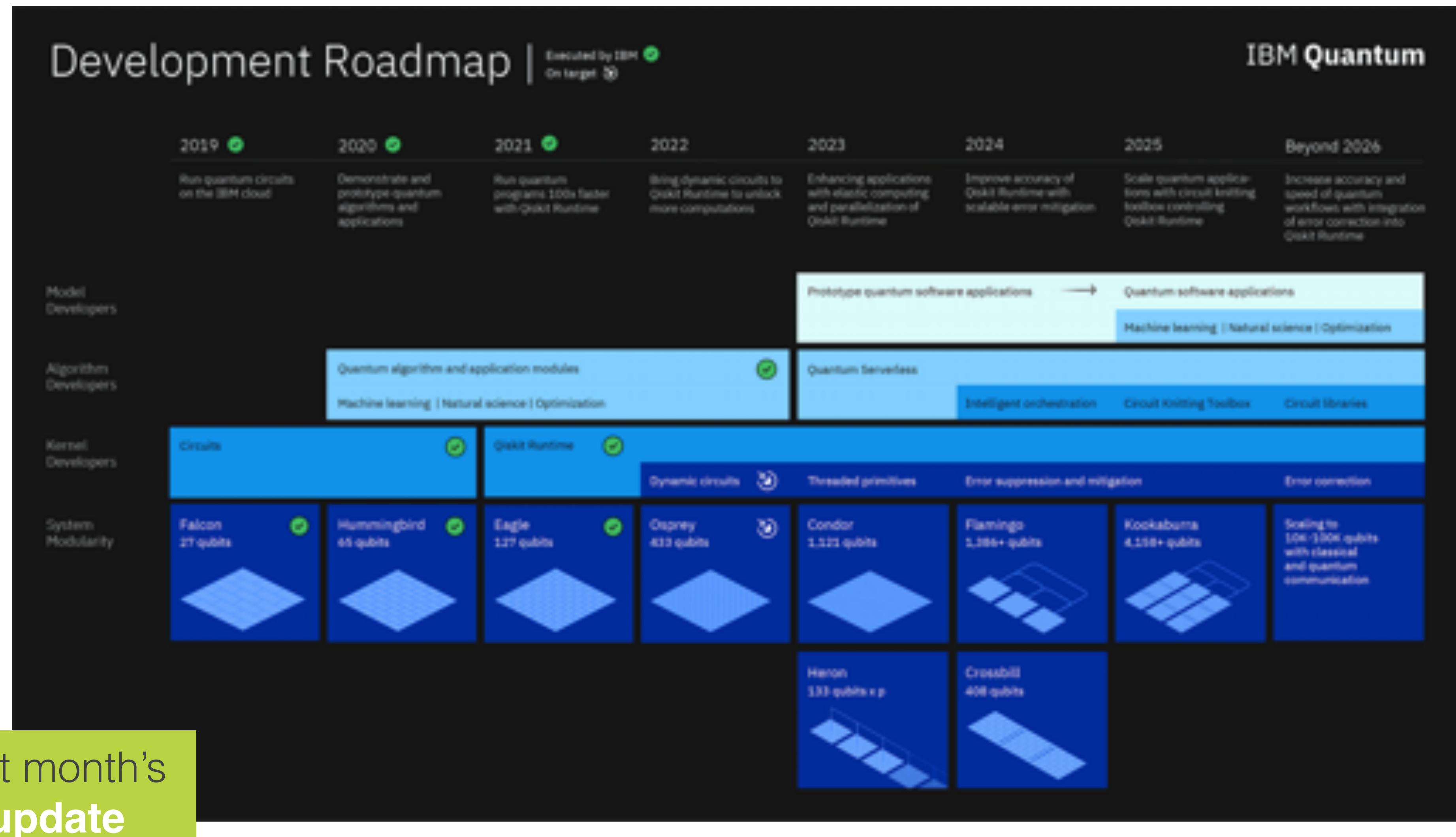
Sycamore chip — 53 qubits

Quantum Computing in the NISQ era



<https://research.ibm.com/blog/quantum-development-roadmap>

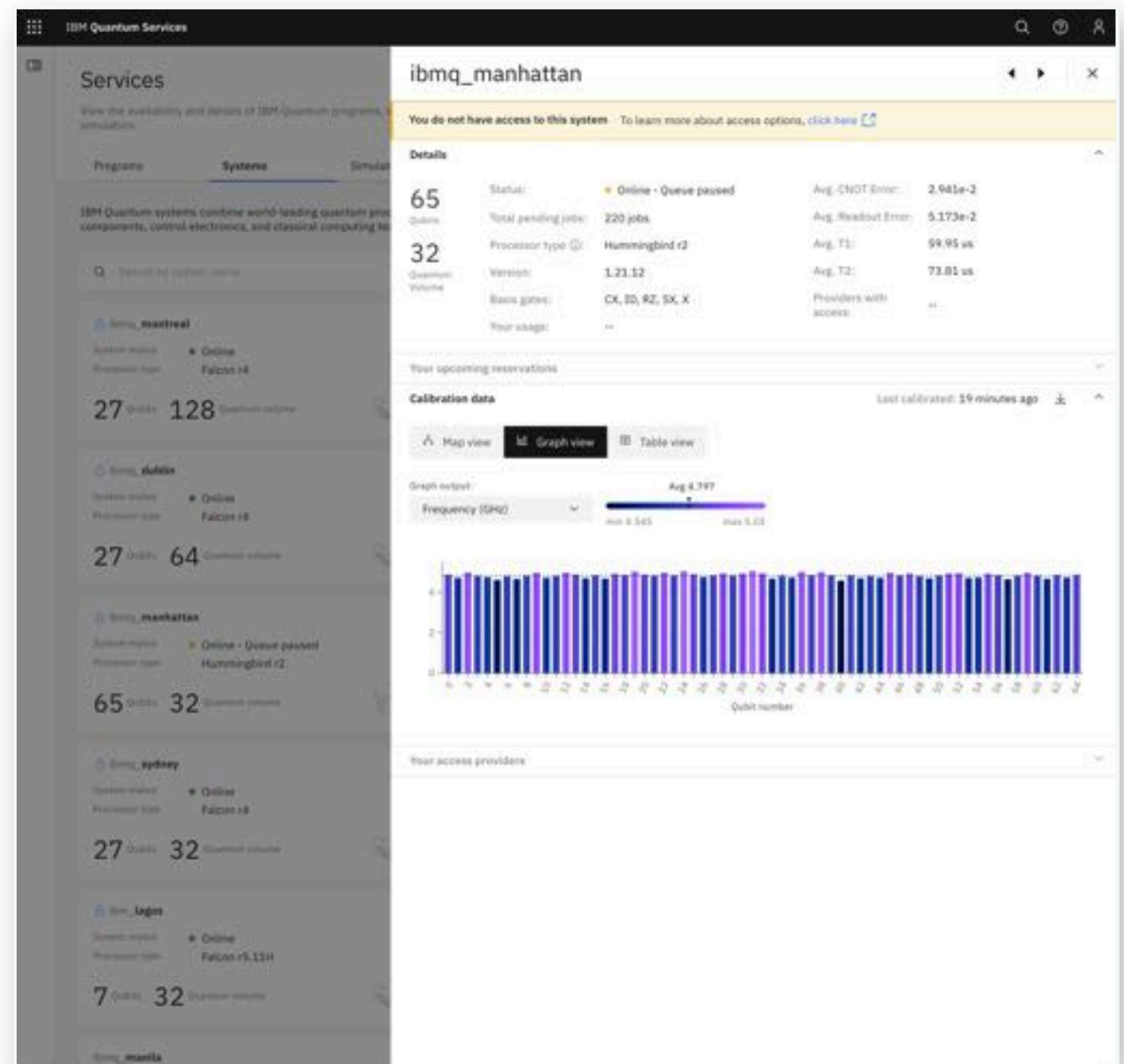
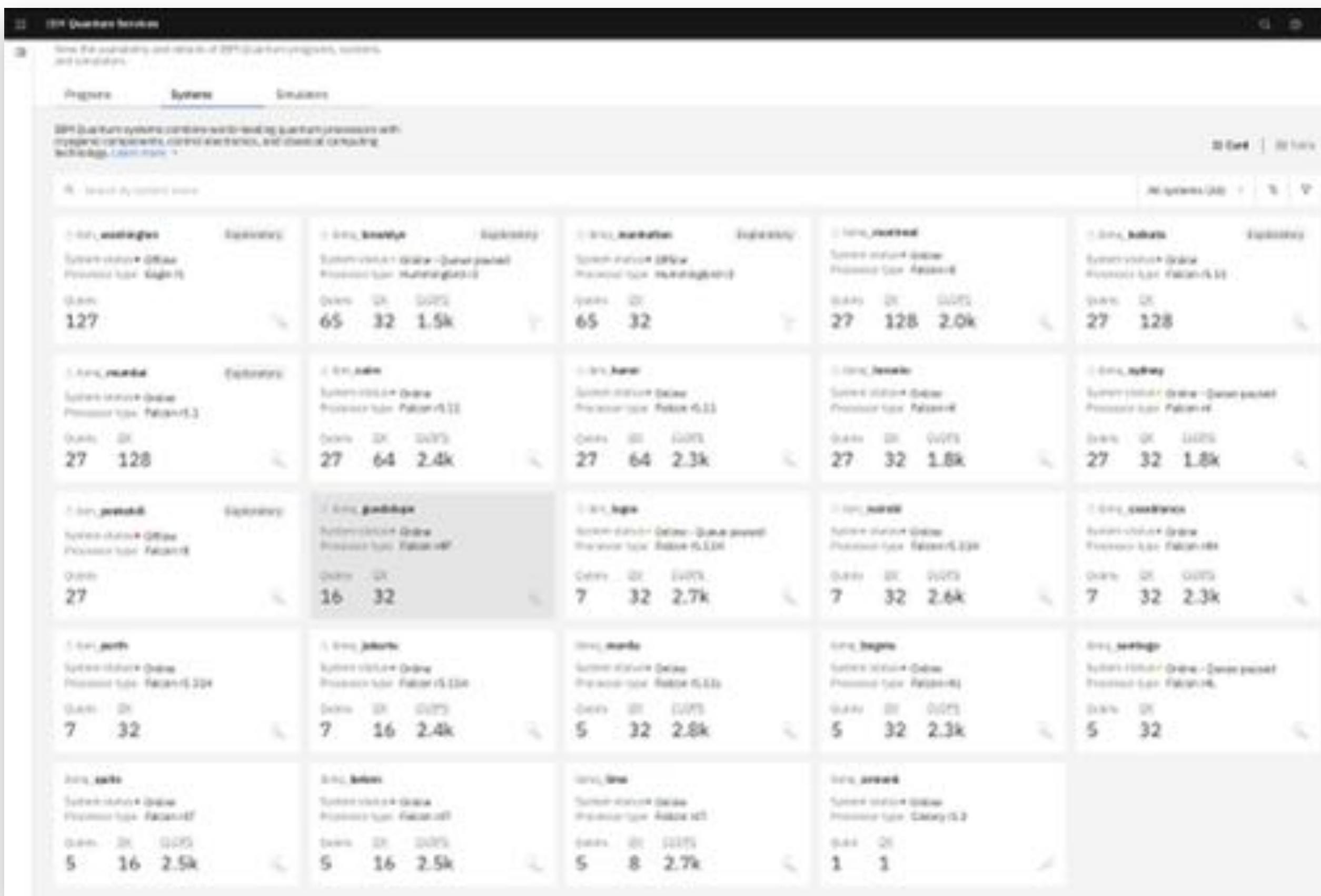
Quantum Computing in the NISQ era



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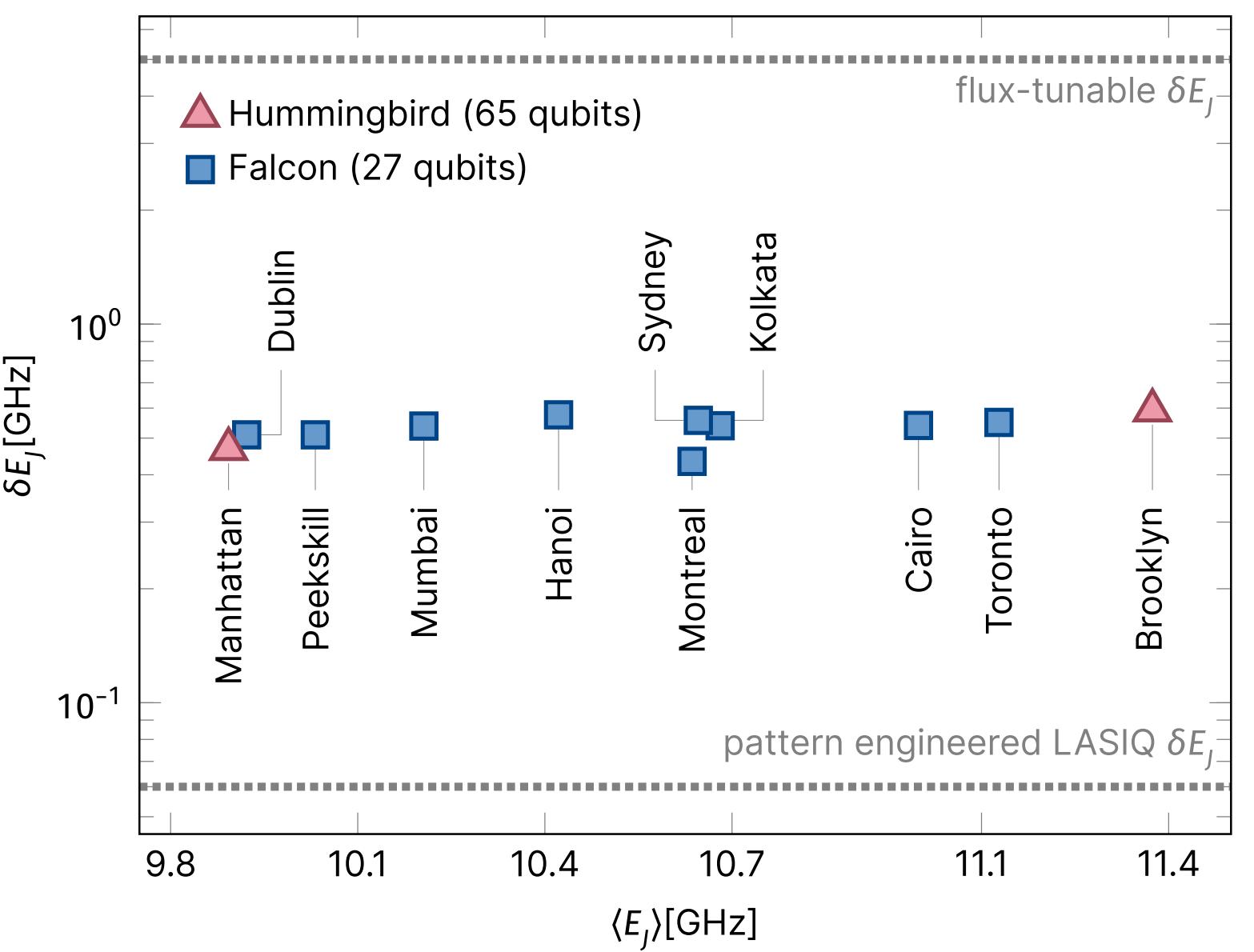
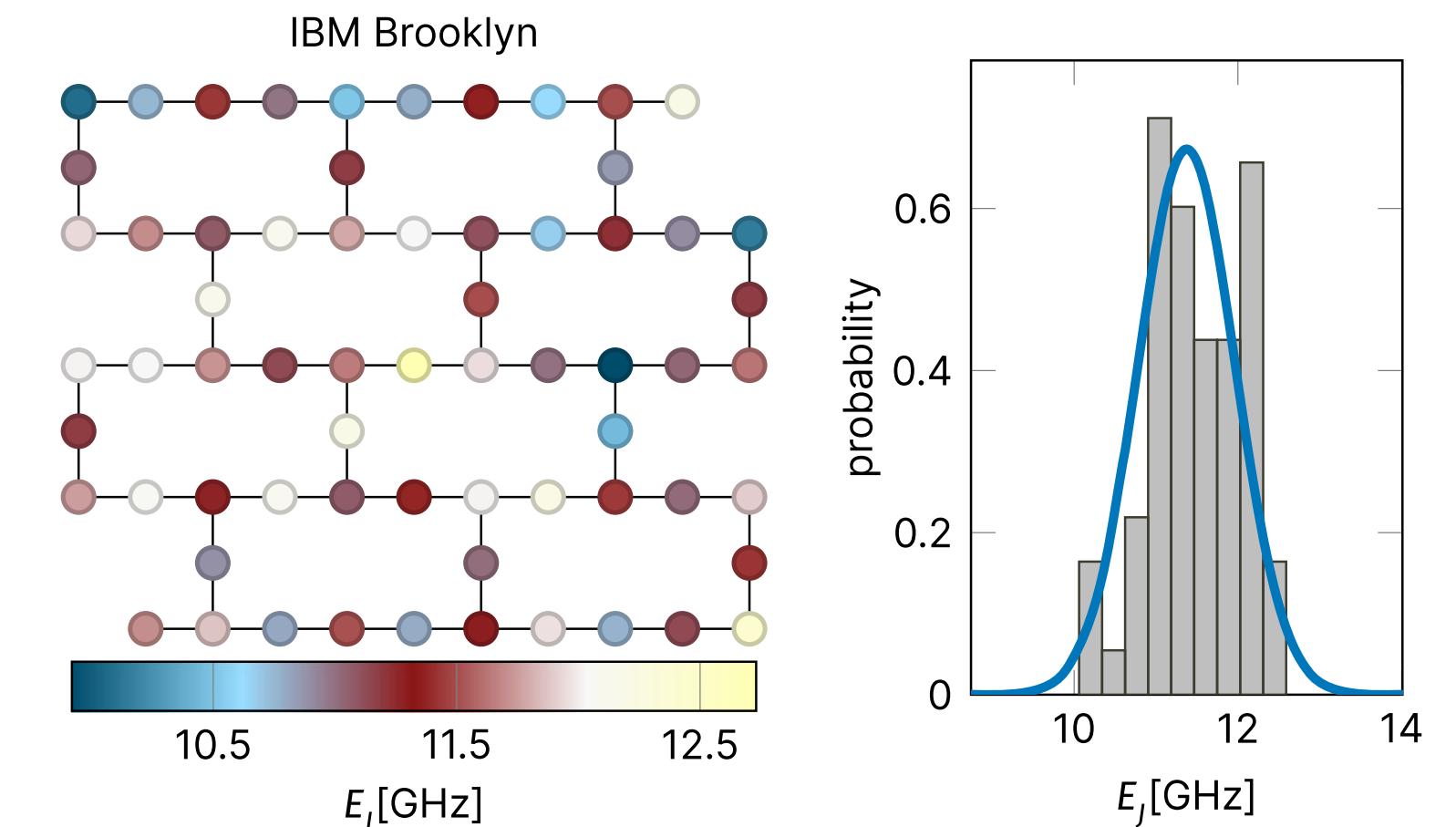
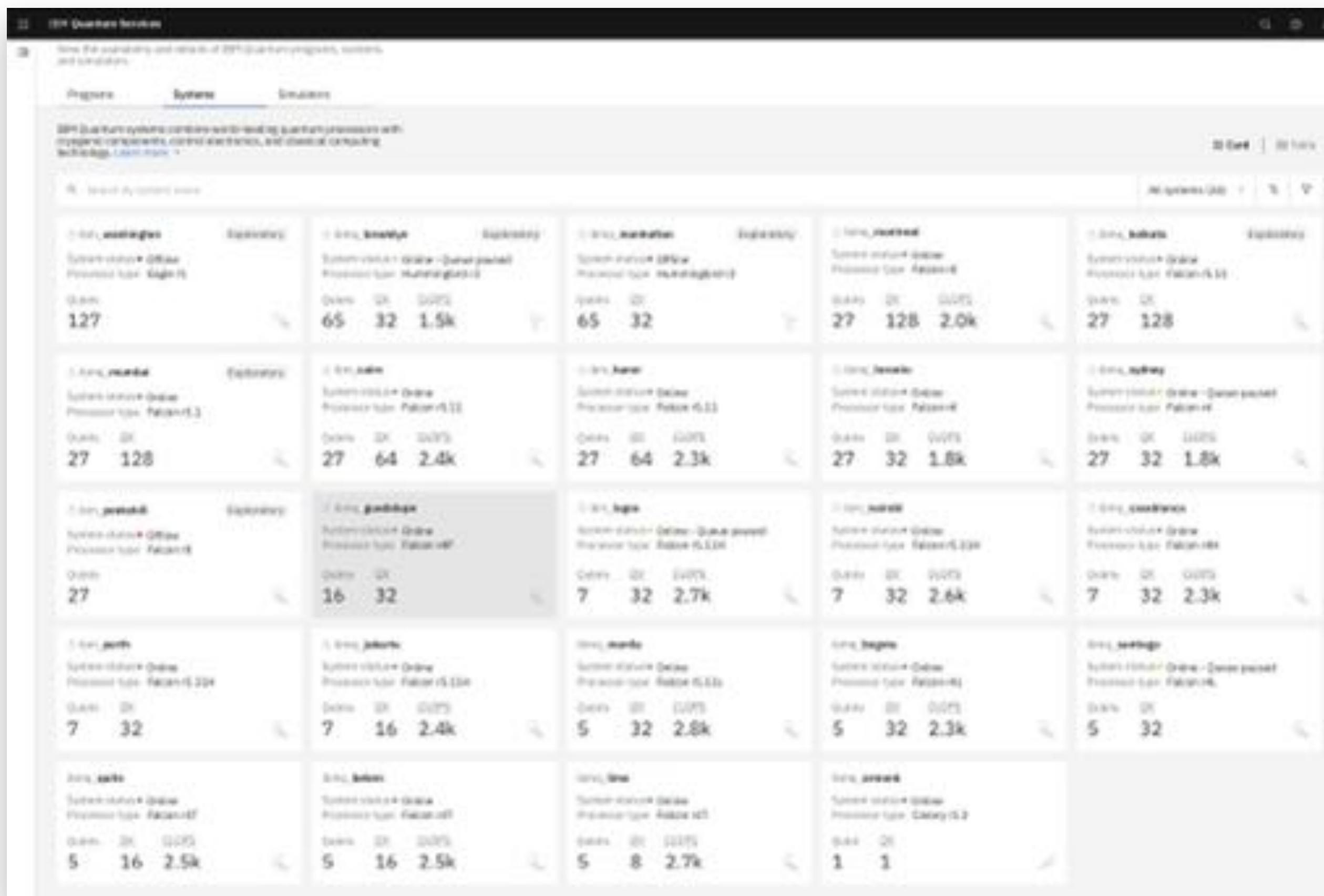
digital quantum processors

IBM quantum cloud devices with **5-127 qubits**



digital quantum processors

IBM quantum cloud devices with **5-127 qubits**

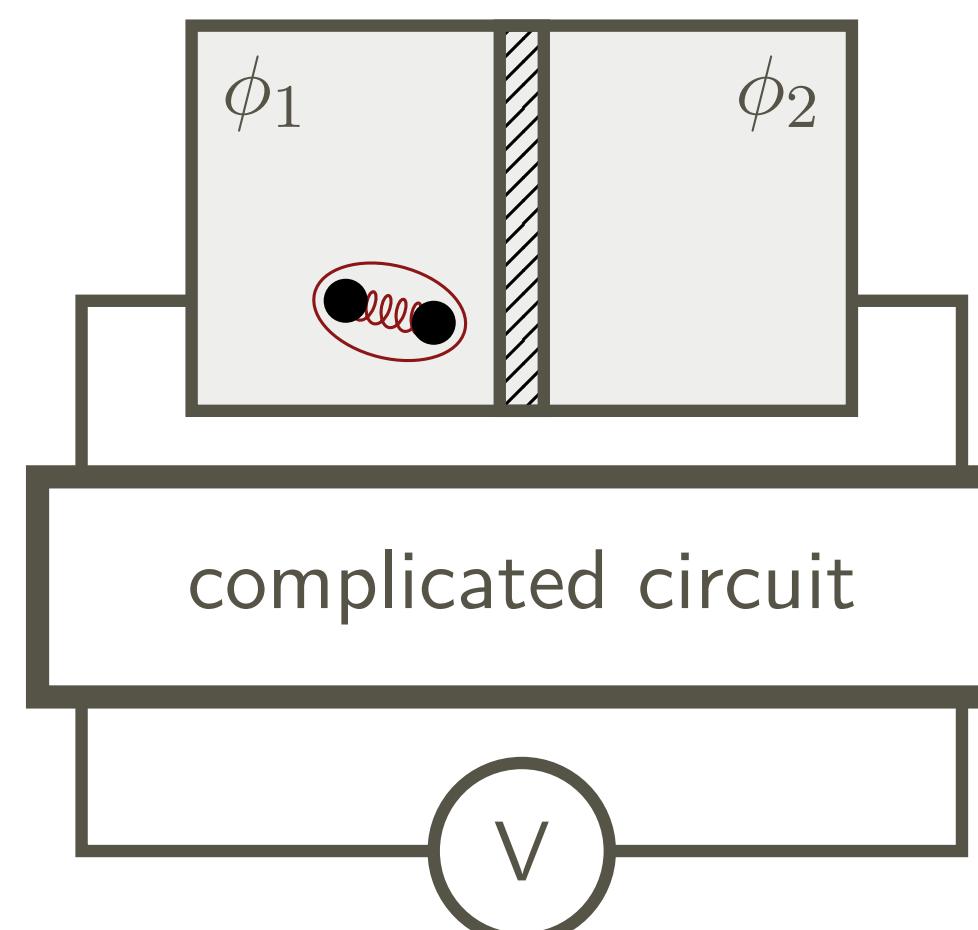


single transmon qubit

$$\hat{H}_{ST} = 4E_C (\hat{n} - n_g)^2 - E_J \cos \hat{\phi}$$

charging
energy

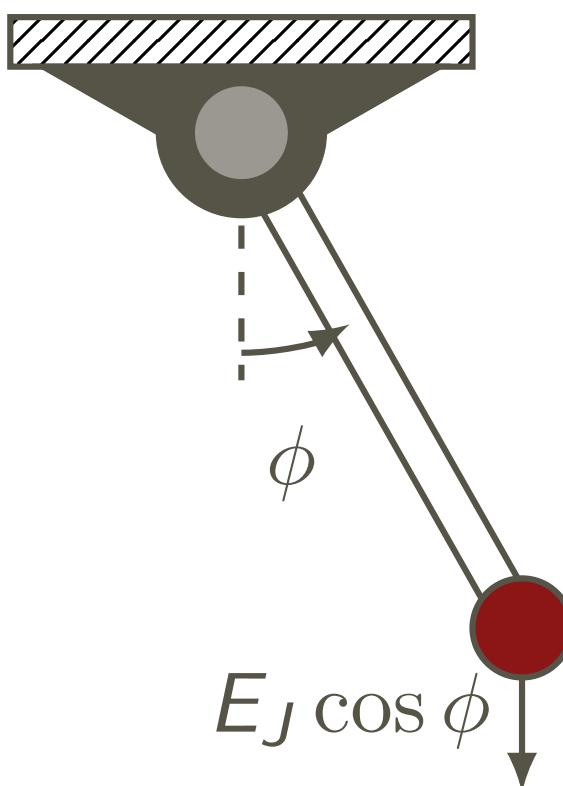
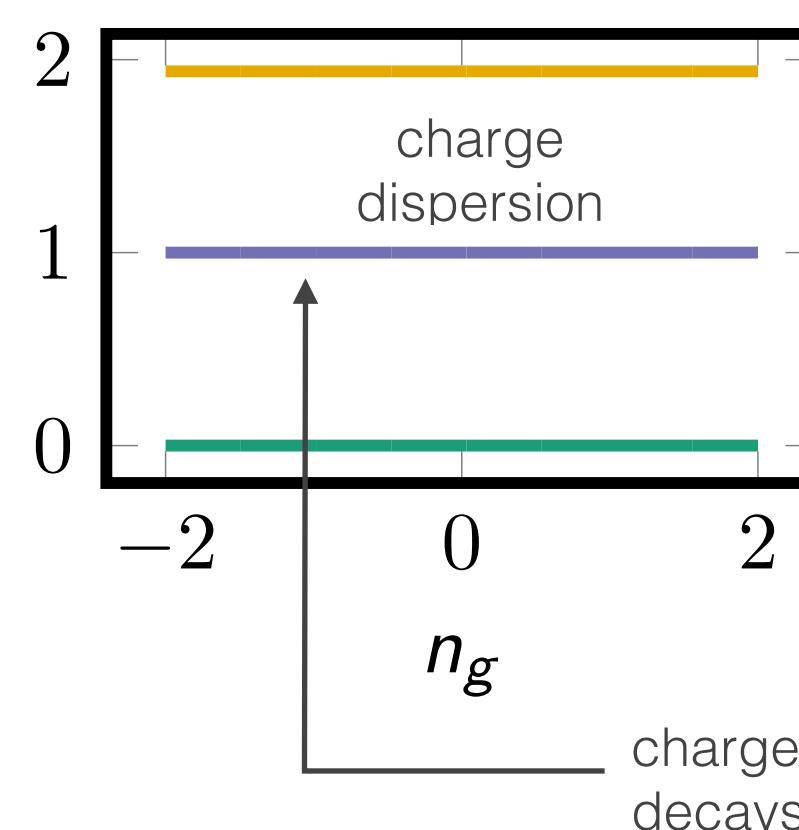
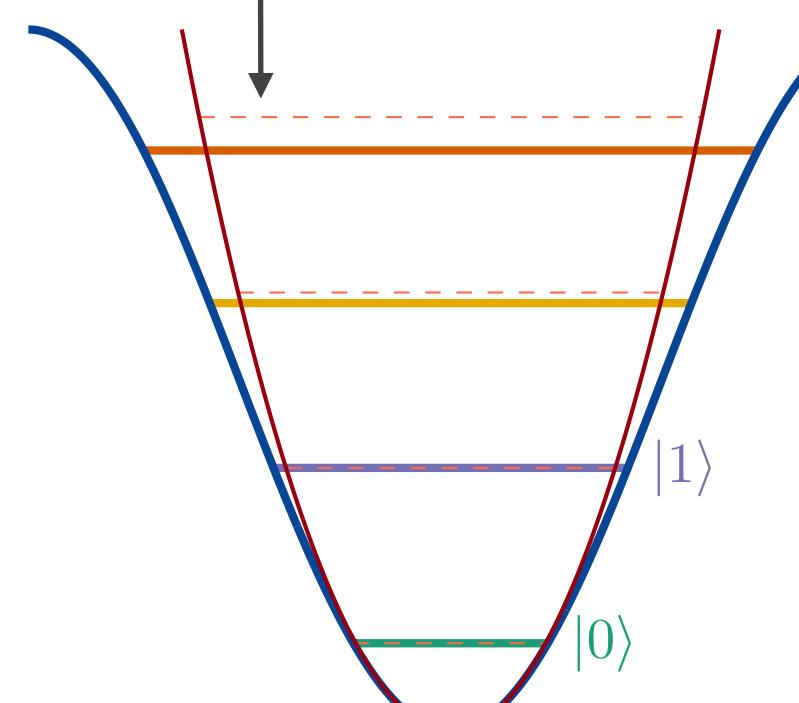
Josephson
tunneling



charge insensitive
cooper pair box

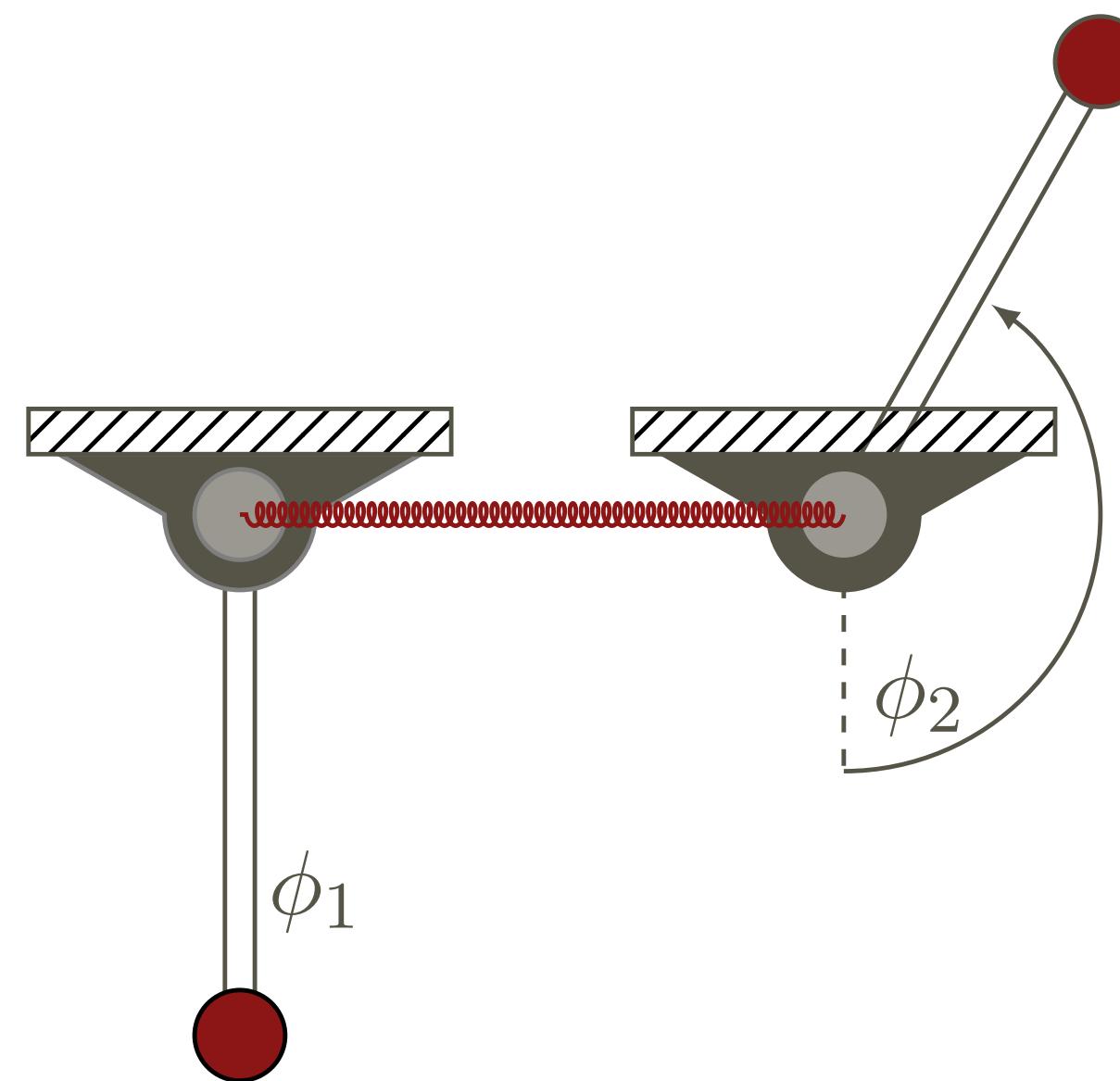
anharmonicity

level spacings converge
algebraically to equidistance

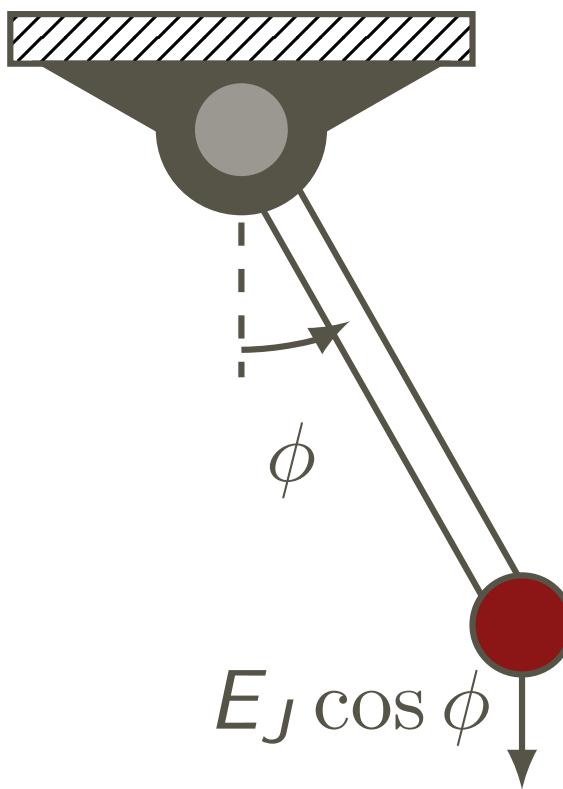
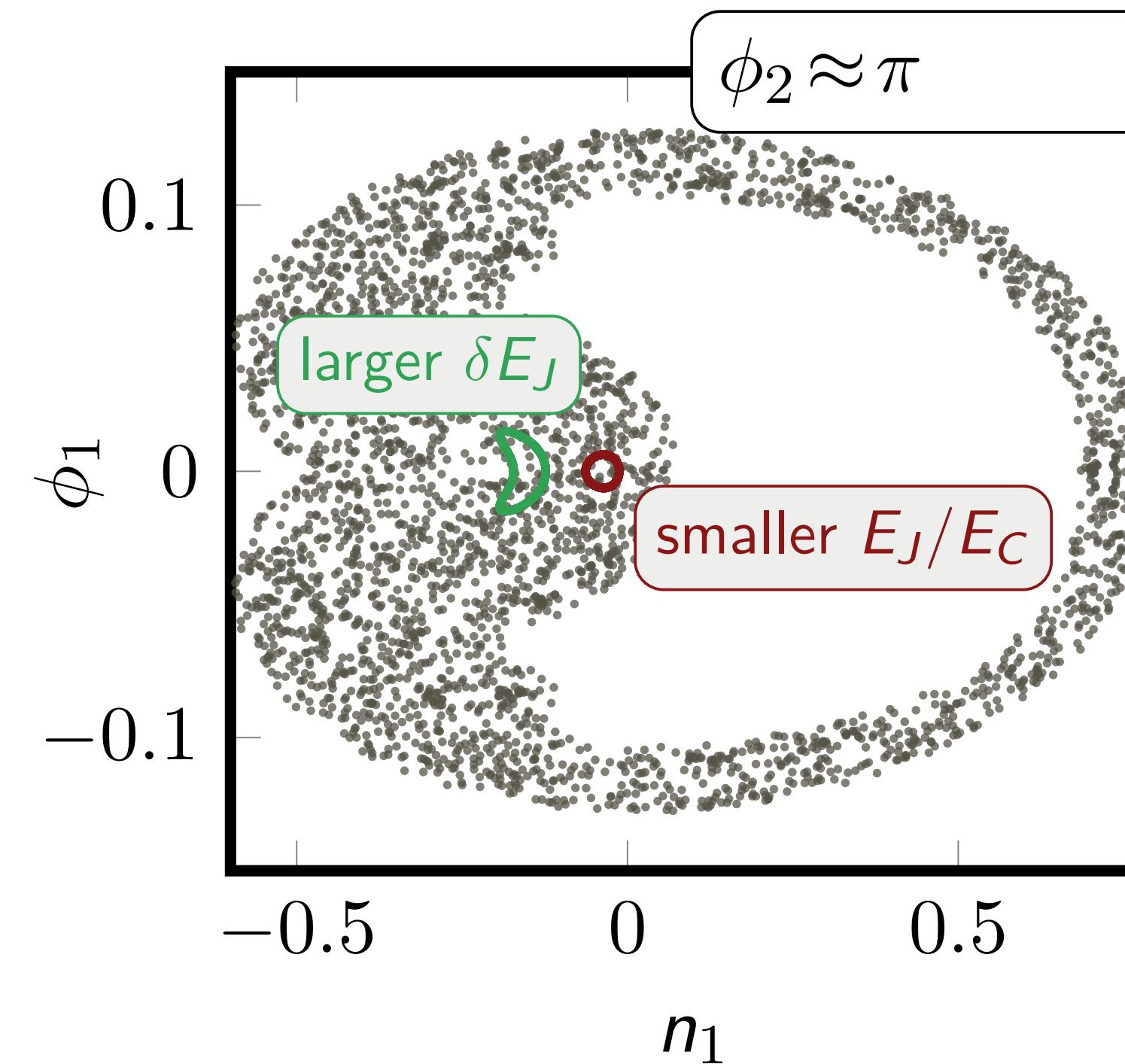


anharmonic
oscillator

two classical transmon qubits



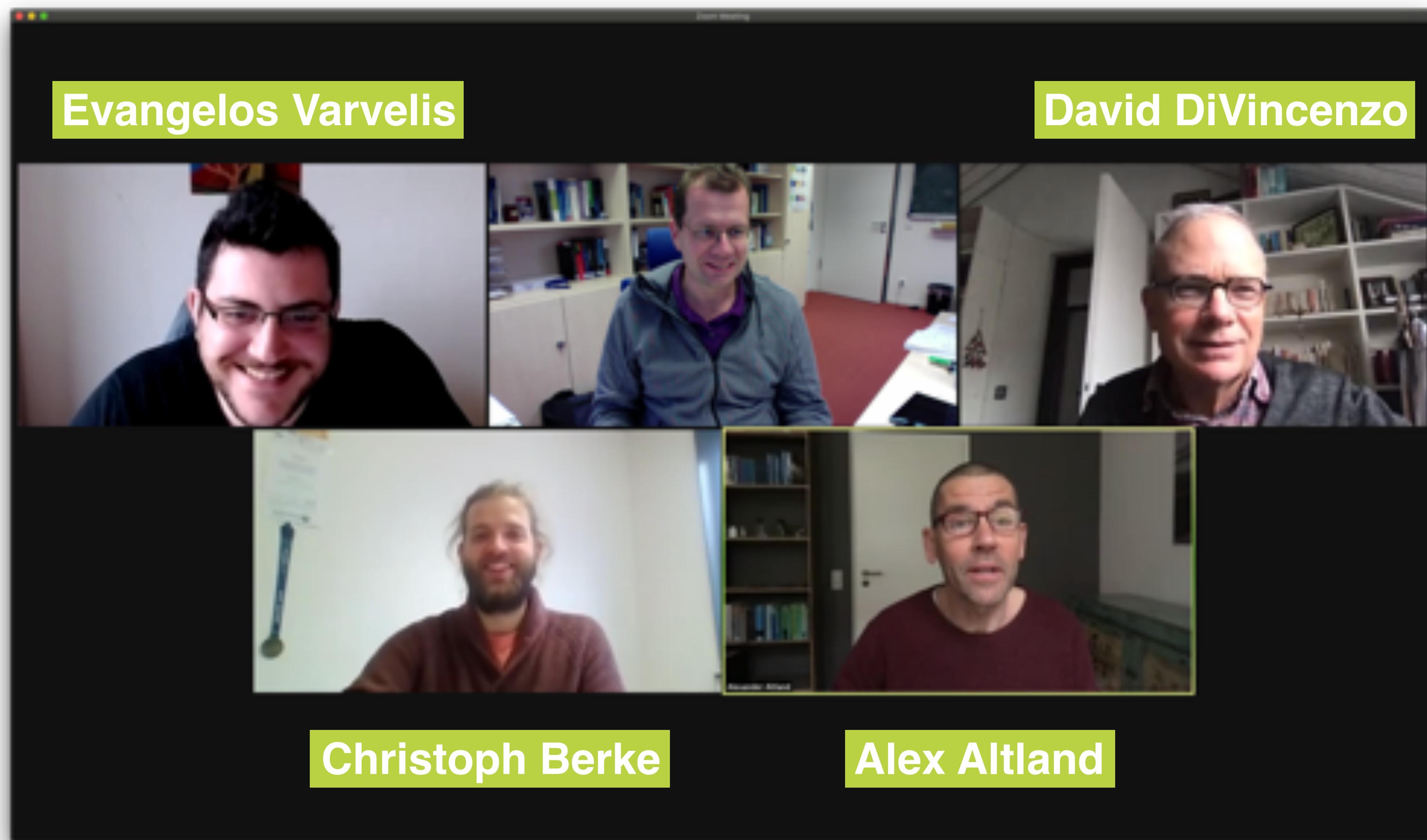
**coupled
oscillators**



**anharmonic
oscillator**

More quantitative analysis for 10 transmons (BSc thesis S. Börner, 2020)
Classical chaos on time scales way **below the typical coherence times**.

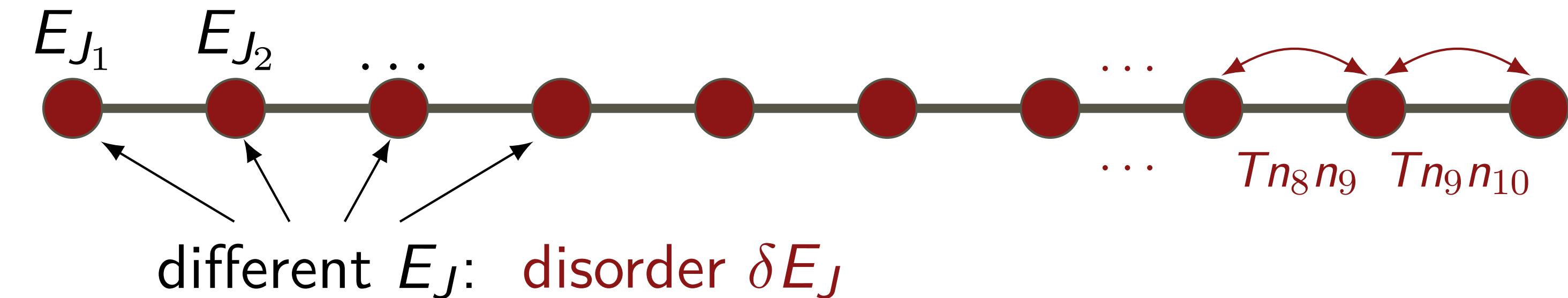
meet the team



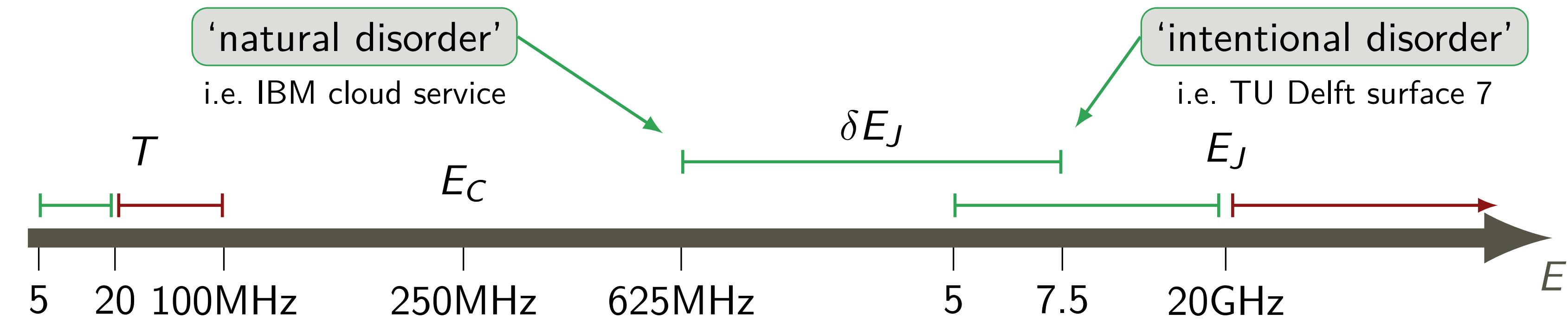
many transmon qubits

$$H = 4E_C \sum_i n_i^2 - \sum_i E_J i \cos \phi_i + T \sum_{\langle i,j \rangle} n_i n_j$$

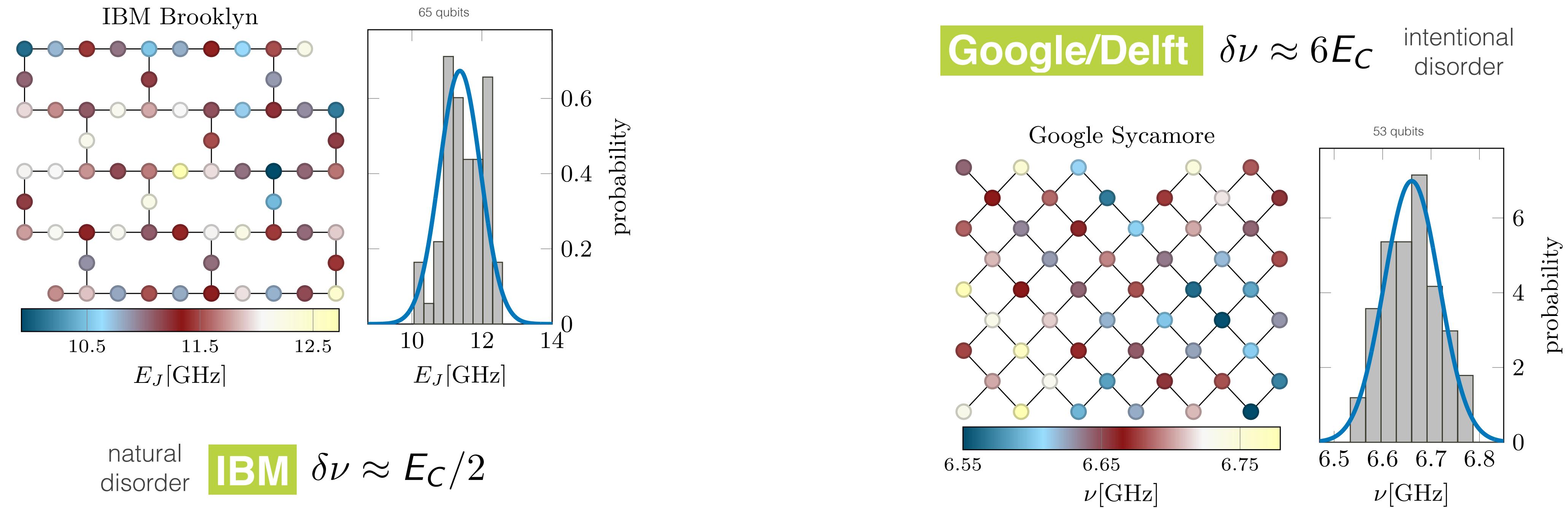
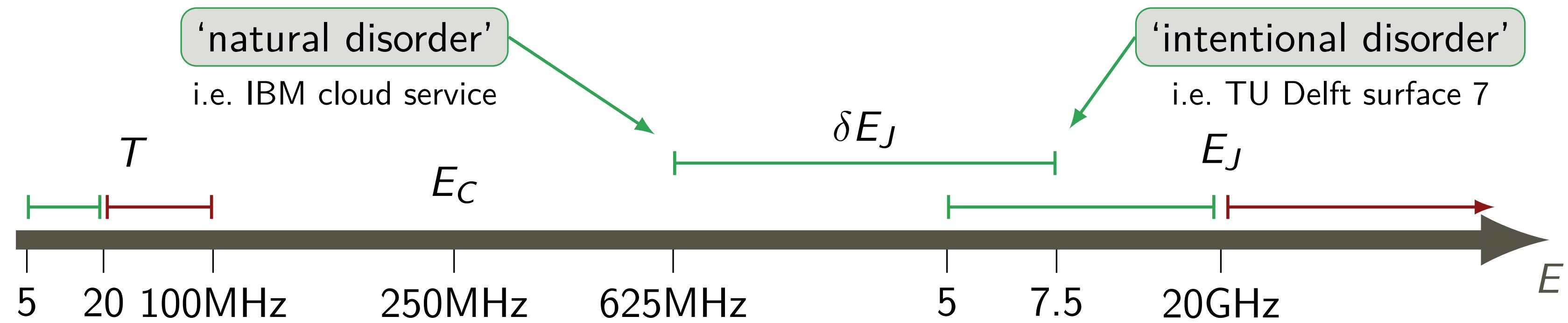
Capacitive coupling



relevant **energy scales**



disorder / experimental settings



many-body perspective

$$H = 4E_C \sum_i n_i^2 - \sum_i E_{J_i} \cos \phi_i + T \sum_{\langle i,j \rangle} n_i n_j$$

series expansions
random-wave approximation

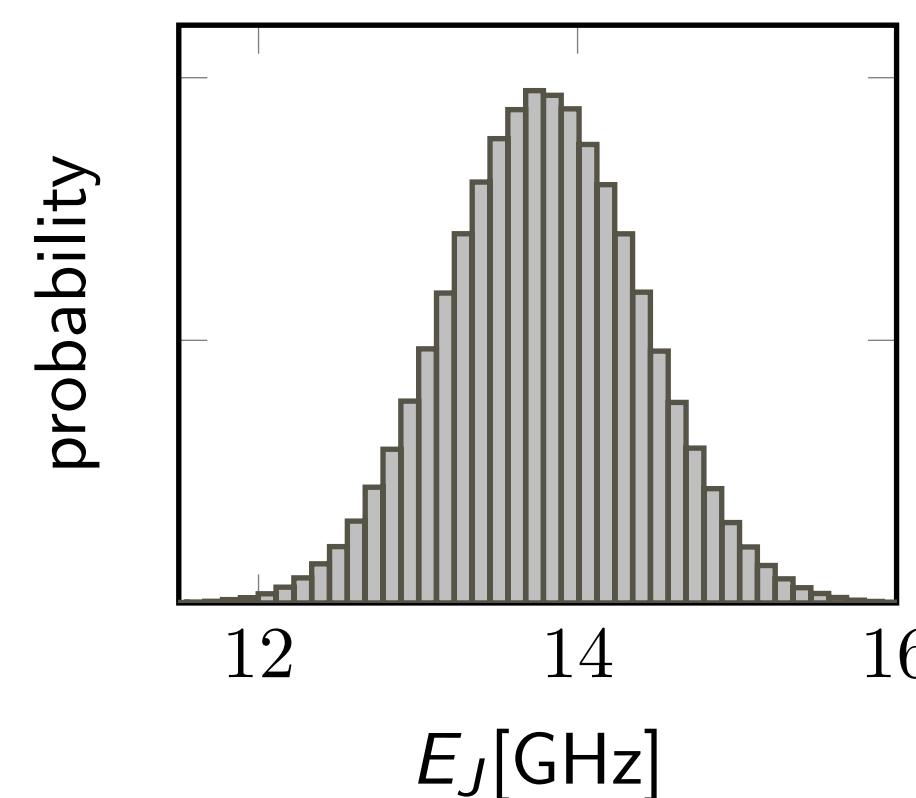
$$H = \sum_i \nu_i a_i^\dagger a_i - \frac{E_C}{2} \sum_i a_i^\dagger a_i (a_i^\dagger a_i + 1) + \sum_{\langle i,j \rangle} t_{ij} (a_i a_j^\dagger + a_i^\dagger a_j)$$

attractive **Bose-Hubbard** model

$$\nu_i = \sqrt{8E_{J_i}E_C}$$

large \longrightarrow small

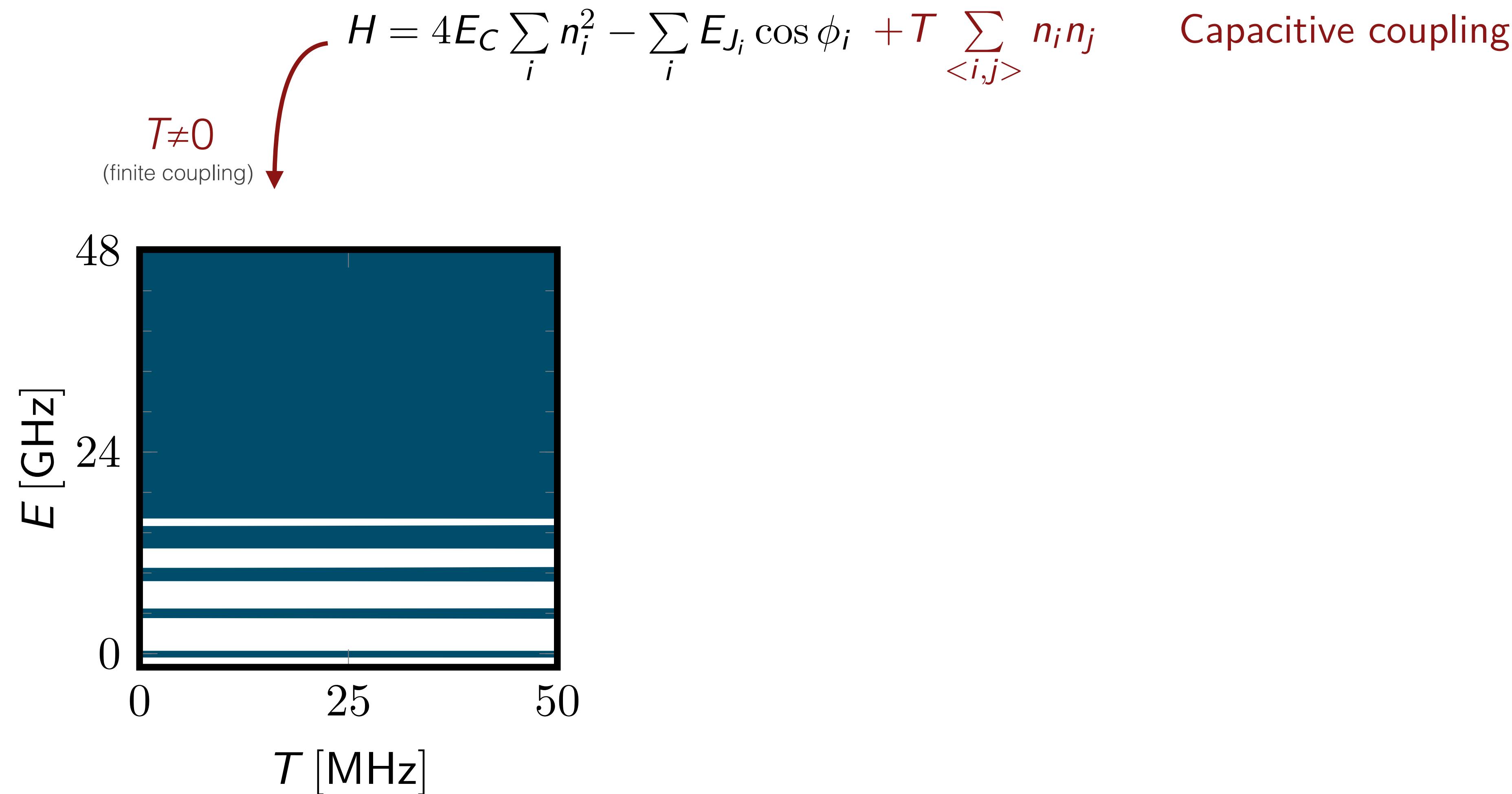
$$t_{ij} = \frac{T}{4\sqrt{2E_C}} \sqrt[4]{E_{J_i}E_{J_j}}$$



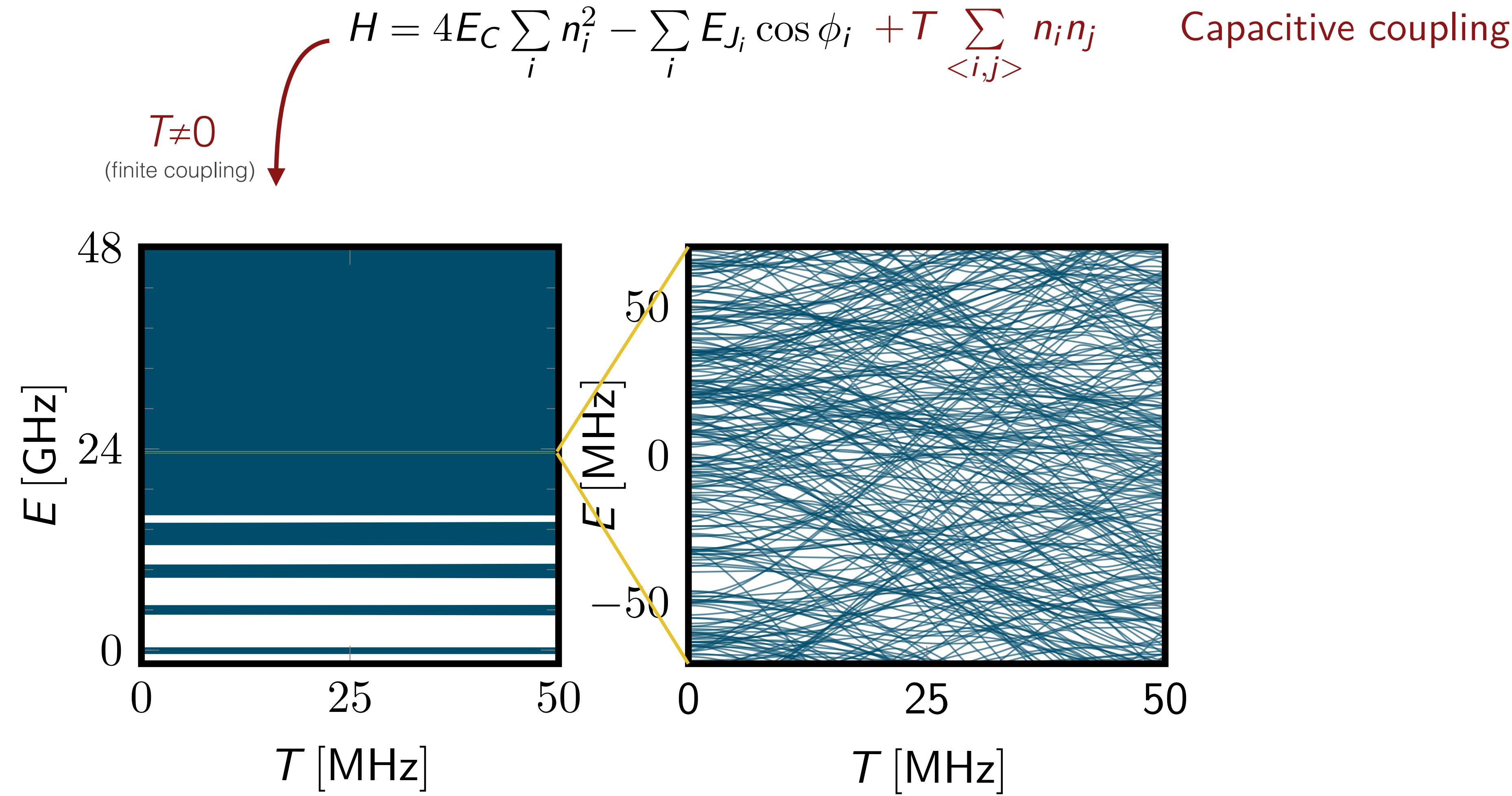
plus disorder
via variations of Josephson energy E_J

reference model for bosonic
many-body localization

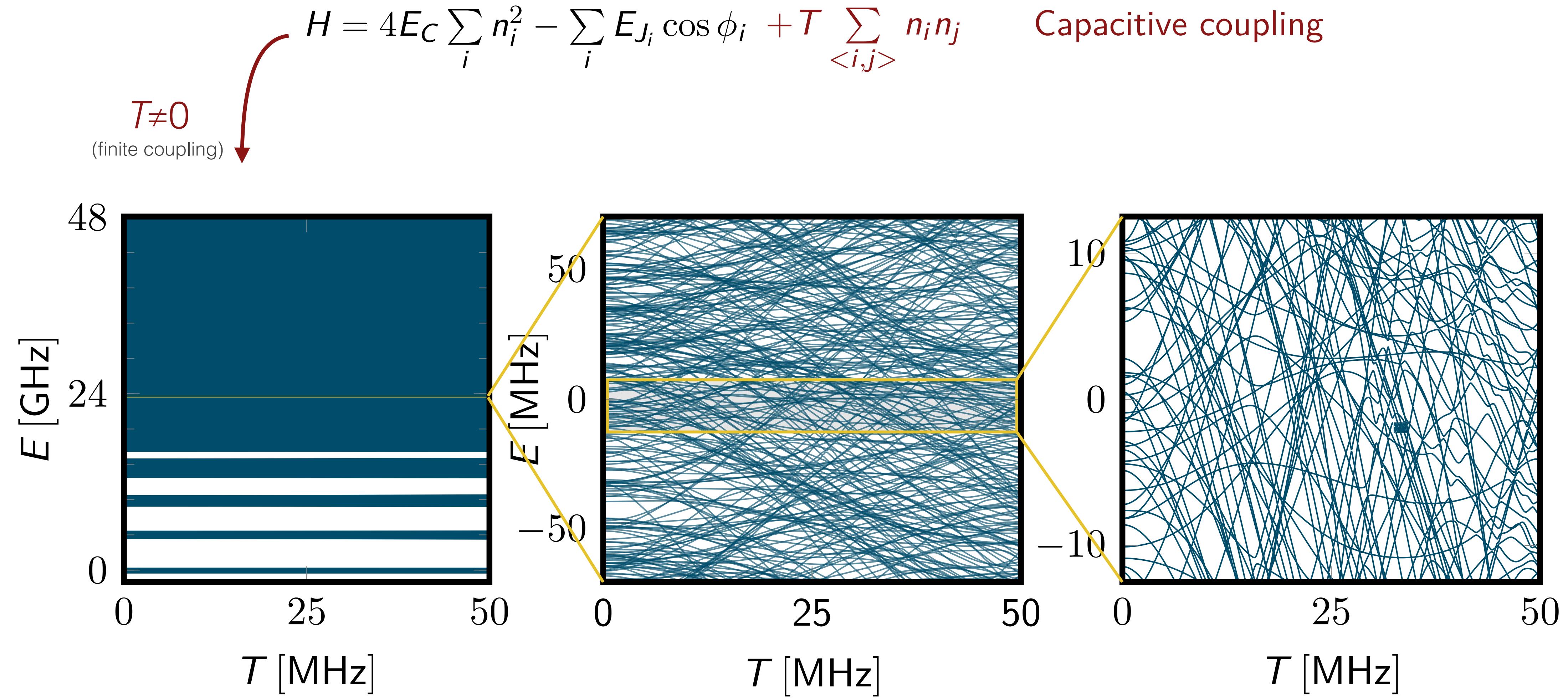
energy spectra – spaghetti plots



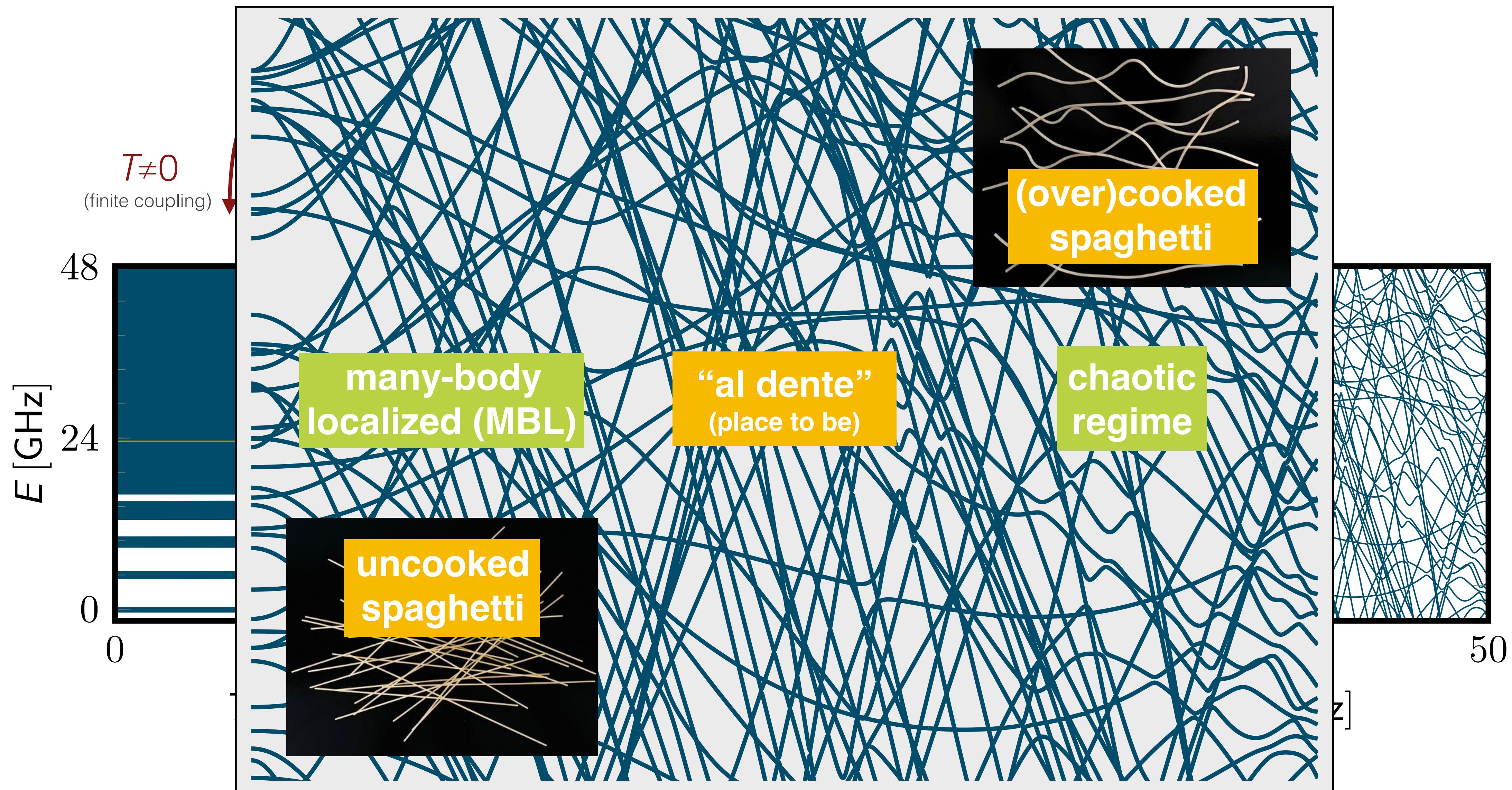
energy spectra – spaghetti plots



energy spectra – spaghetti plots



energy spectra – spaghetti plots



We need to find a **subtle balance**

– disorder can **protect qubits,**

but **entangling / coupling qubits** in its

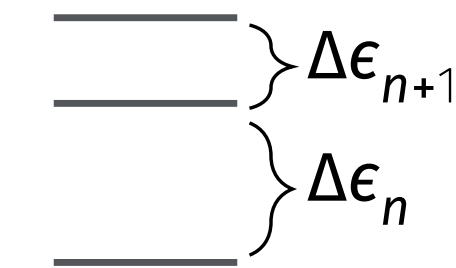
presence might lead to quantum chaos.

quantifying chaos

spectral statistics

level statistics

$$r_n = \Delta\epsilon_{n+1} / \Delta\epsilon_n$$

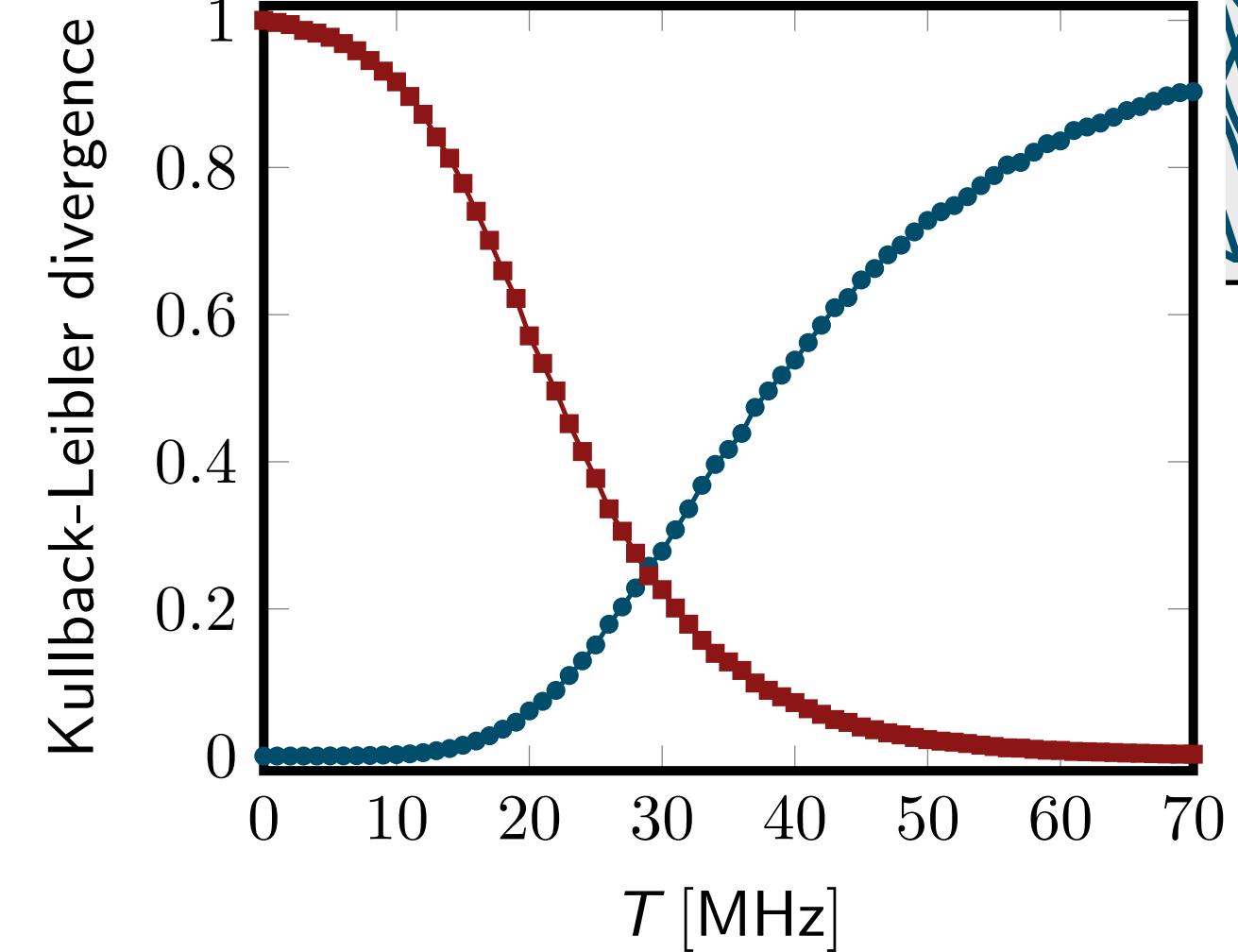
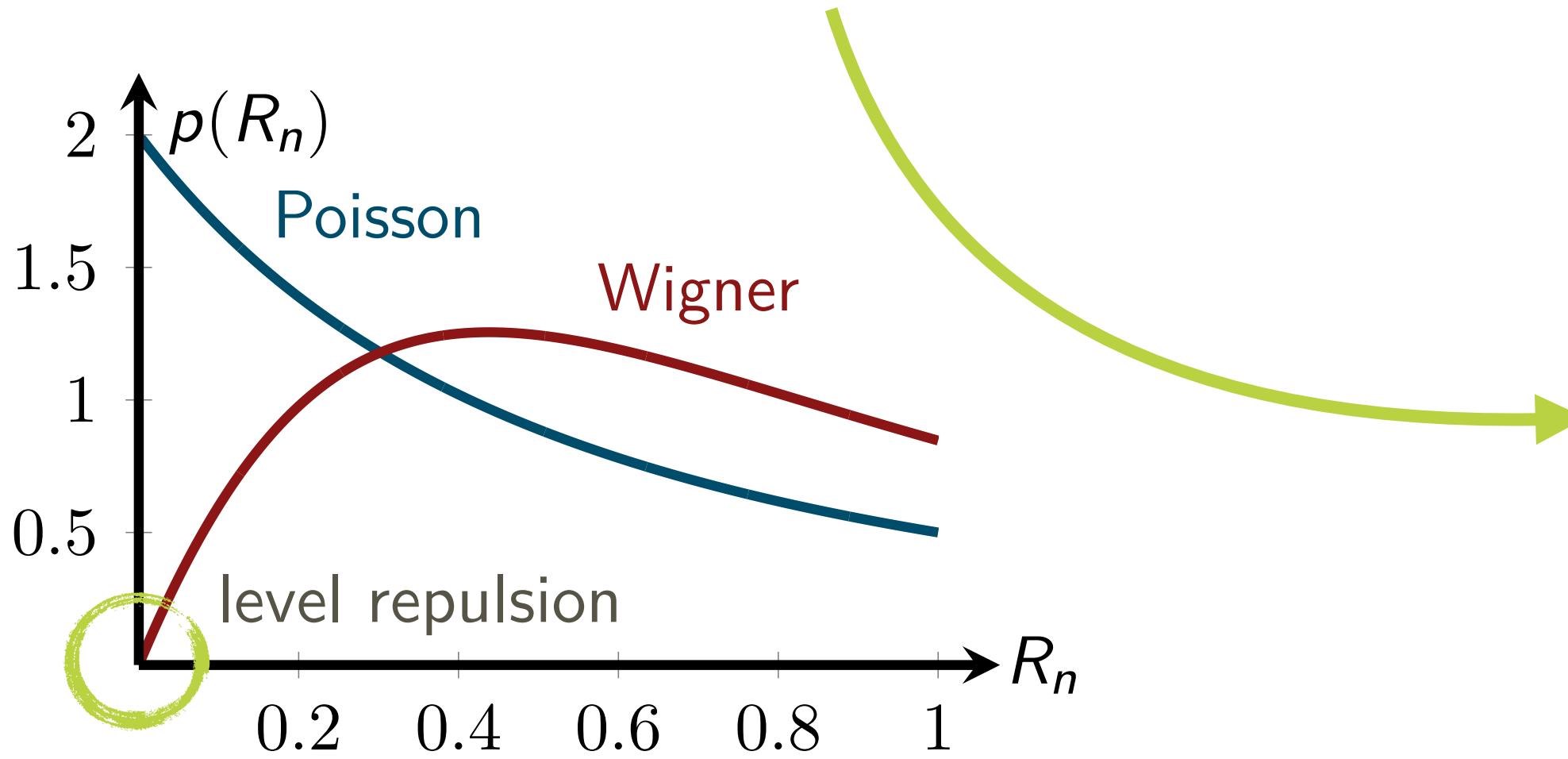


Kullback-Leiber divergence

$$D_{KL}(P||Q) = \sum_k p_k \log\left(\frac{p_k}{q_k}\right)$$

data

theory



quantifying chaos

spectral statistics

level statistics

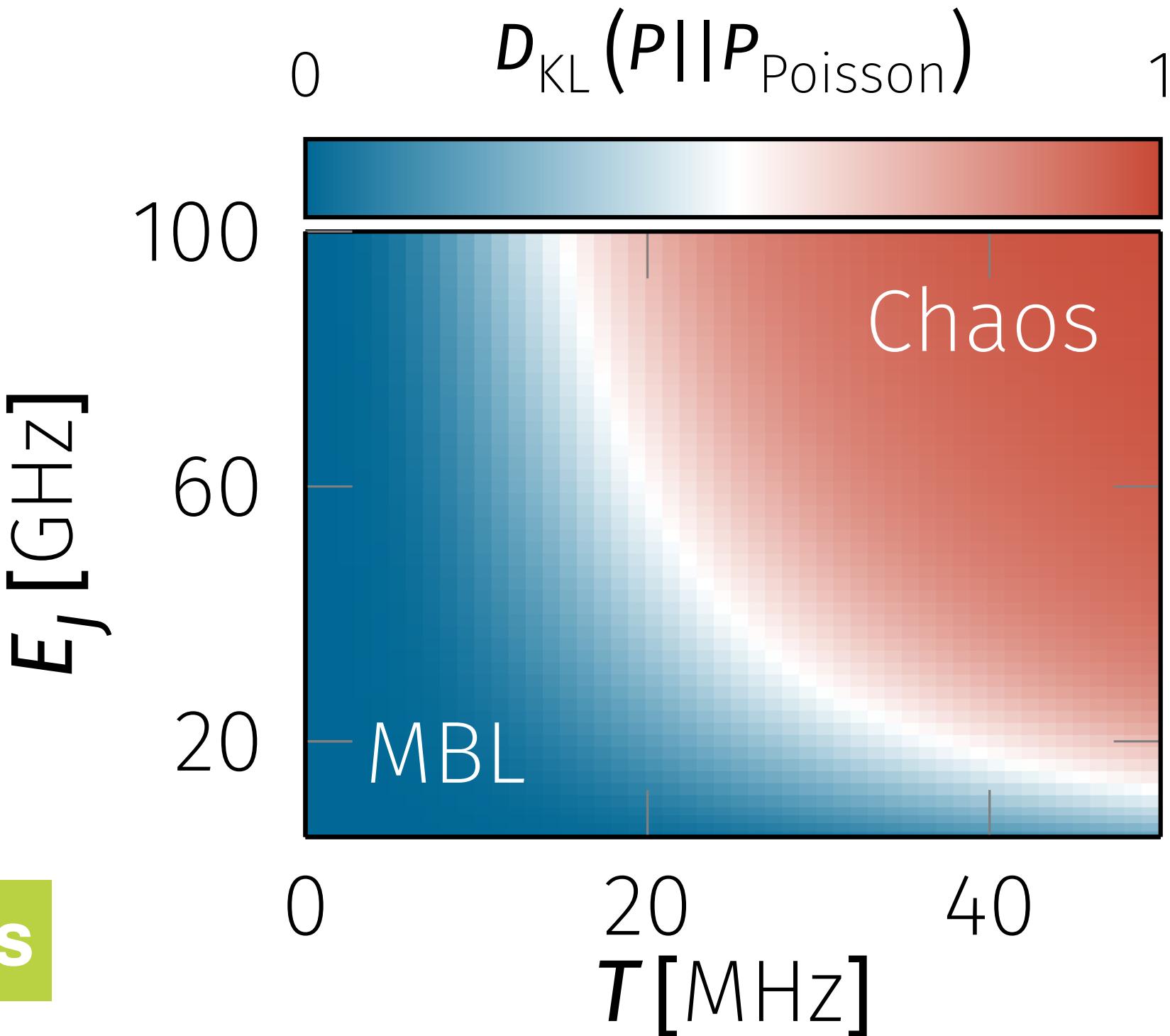
$$r_n = \Delta\epsilon_{n+1}/\Delta\epsilon_n$$

$$\begin{array}{c} \overline{\overline{\epsilon}} \\ \overline{\epsilon} \end{array} \left. \begin{array}{c} \Delta\epsilon_{n+1} \\ \Delta\epsilon_n \end{array} \right.$$

Kullback-Leiber divergence

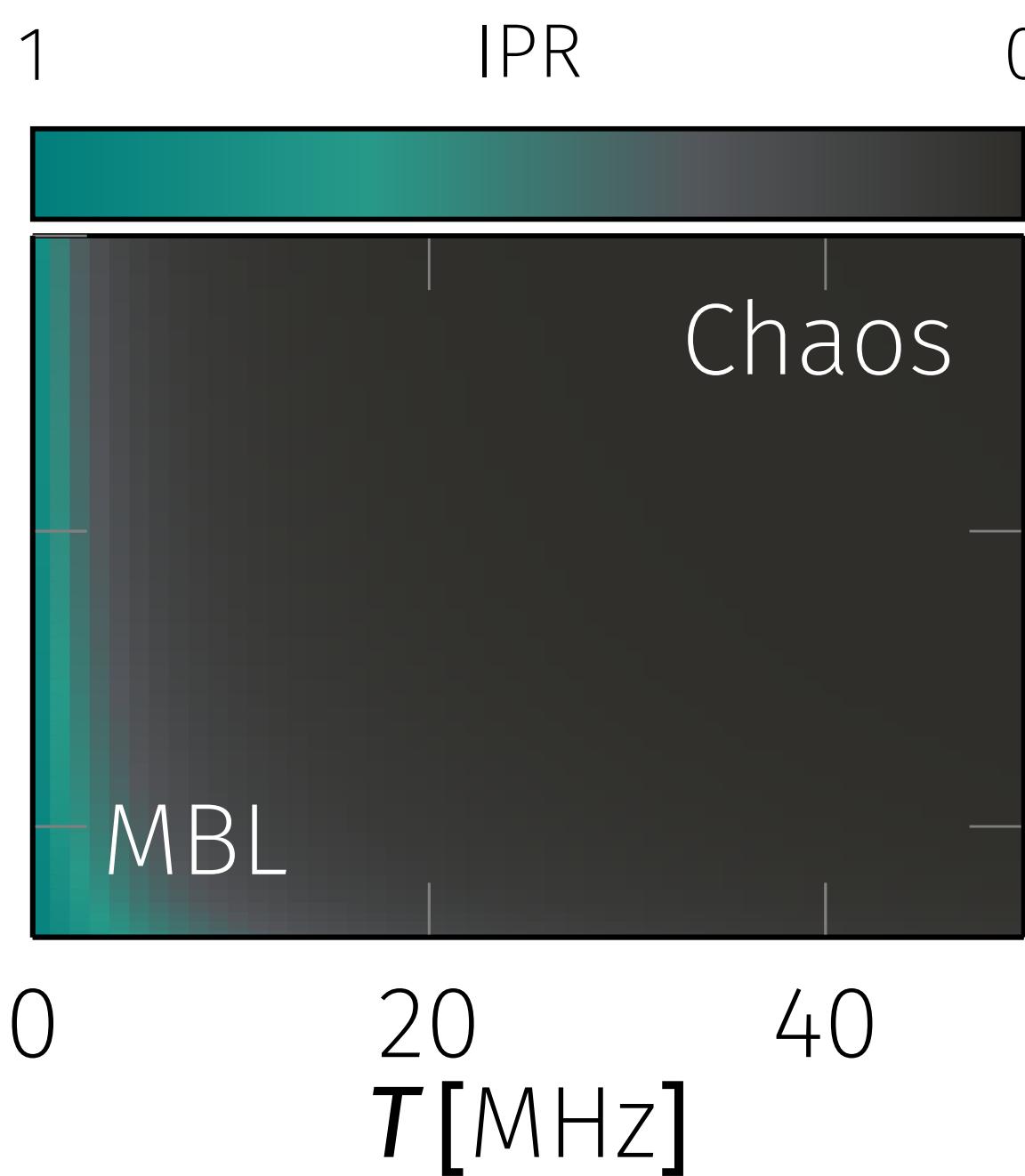
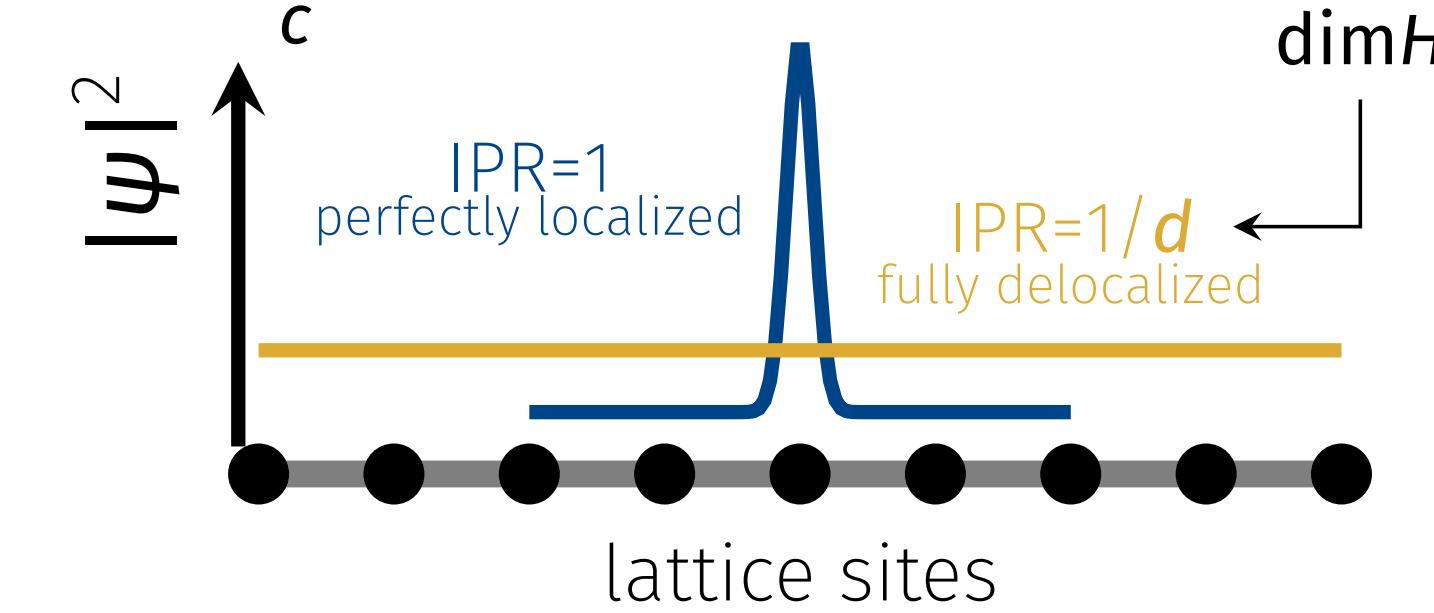
$$D_{\text{KL}}(P||Q) = \sum_k p_k \log\left(\frac{p_k}{q_k}\right)$$

↑ data ↑ theory



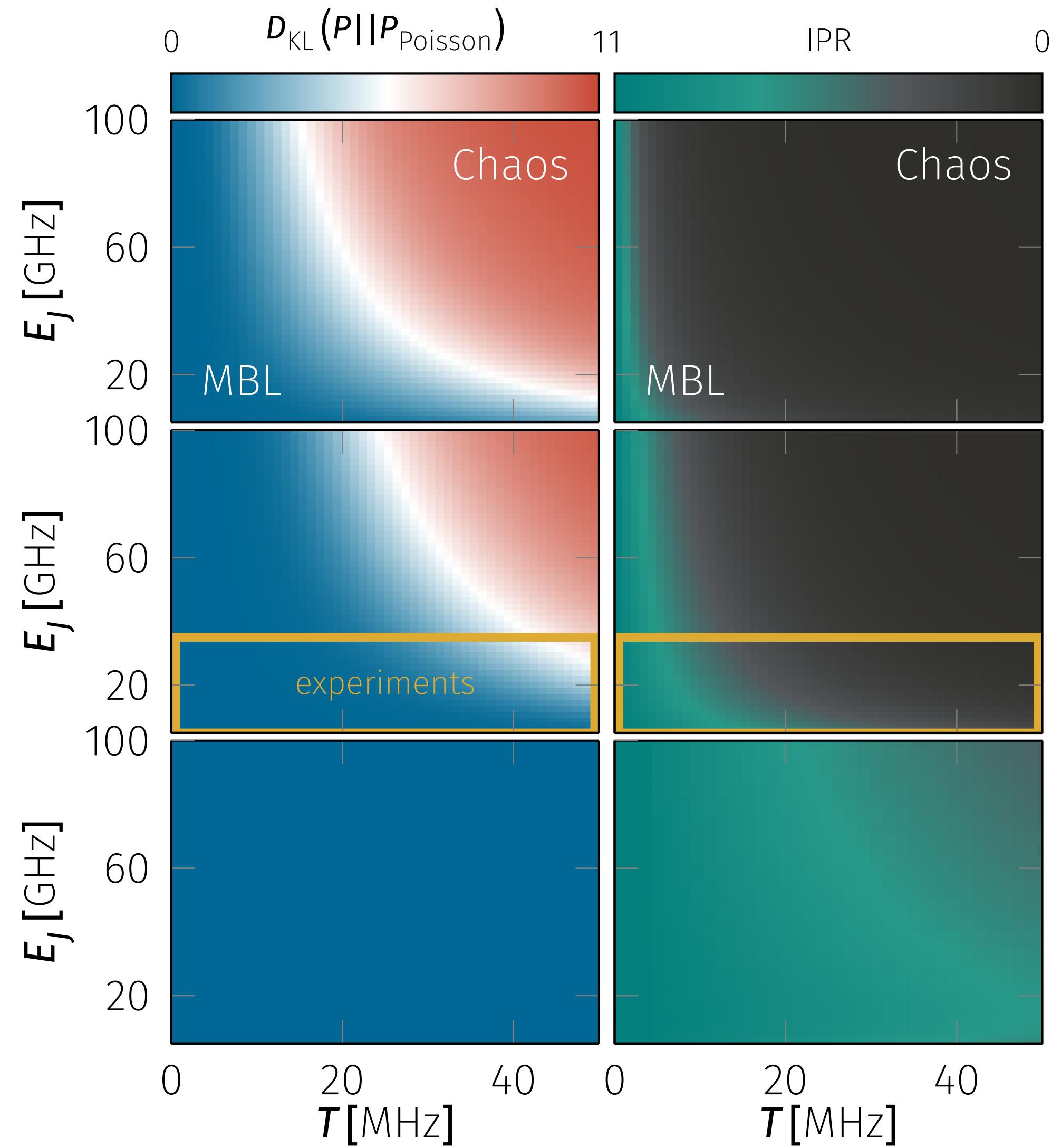
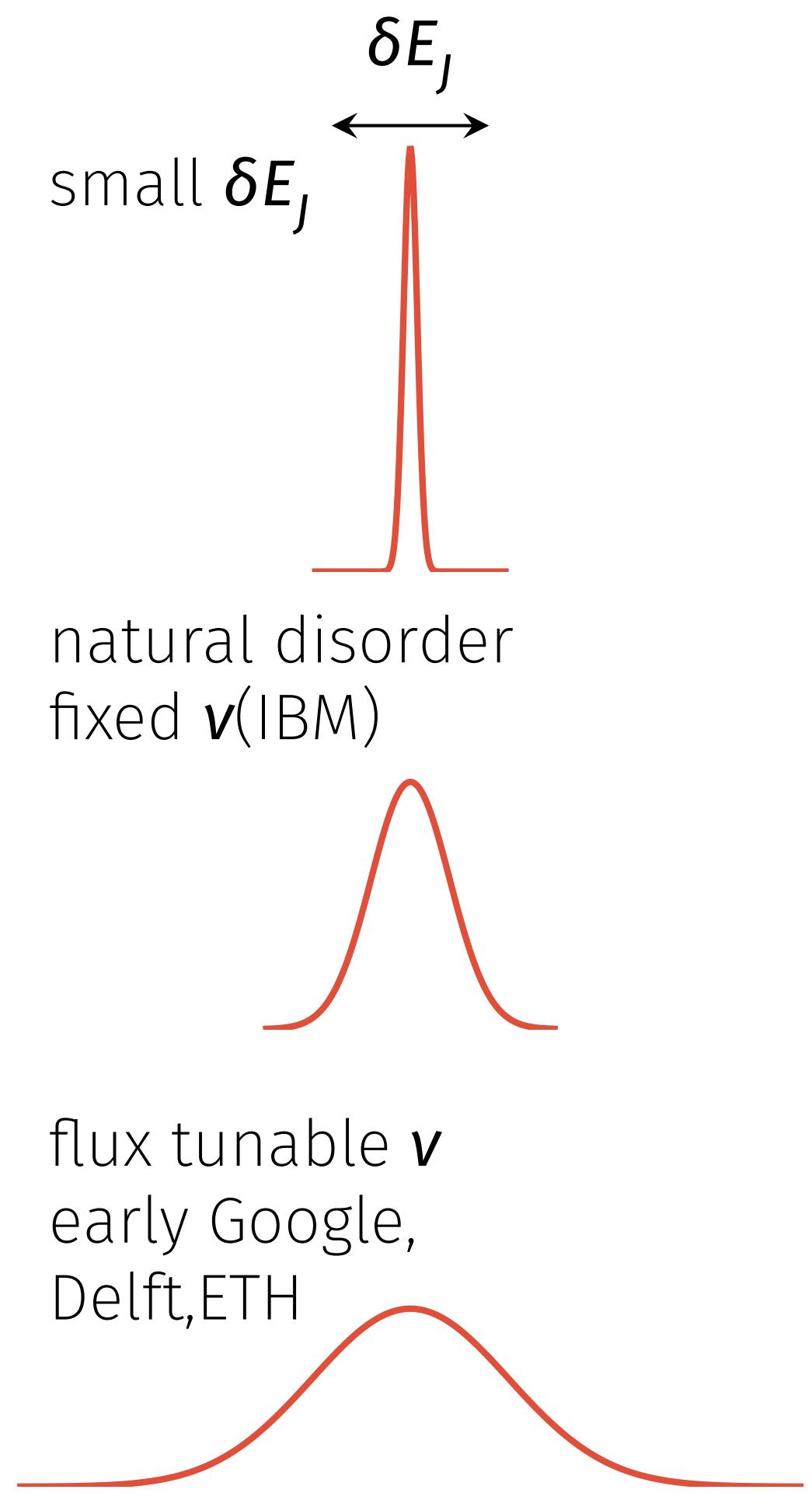
wavefunction statistics

$$\text{IPR} = \sum_c |\langle c | \psi \rangle|^4$$



quantifying chaos

patterned disorder
natural disorder
tunable disorder



computational states

non-computational subspace

$$\dim \mathcal{H} \approx 8 \cdot 10^8$$

$$\dim \mathcal{H}_{\text{cs}} \approx 3 \cdot 10^6$$



computational subspace

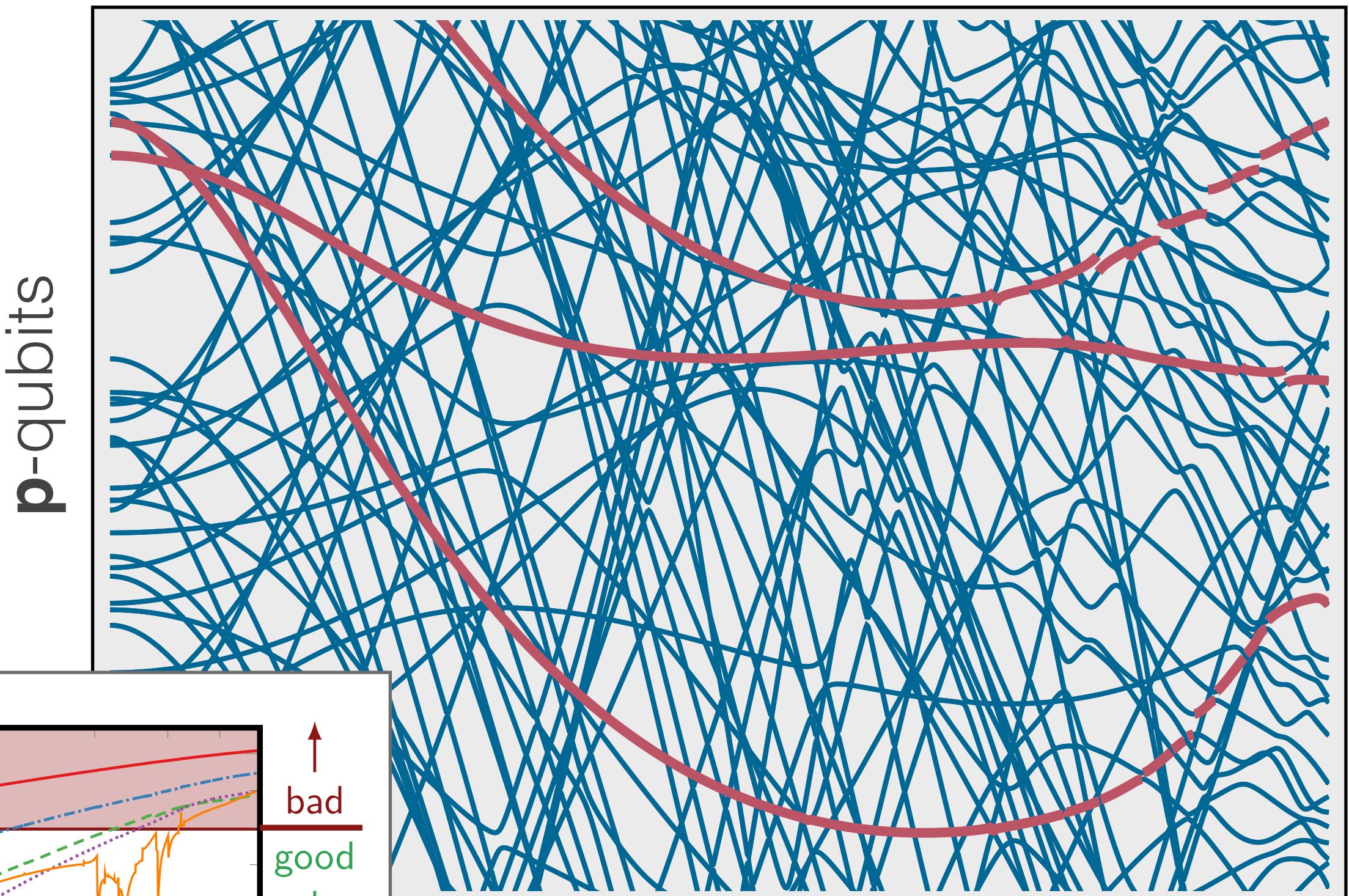
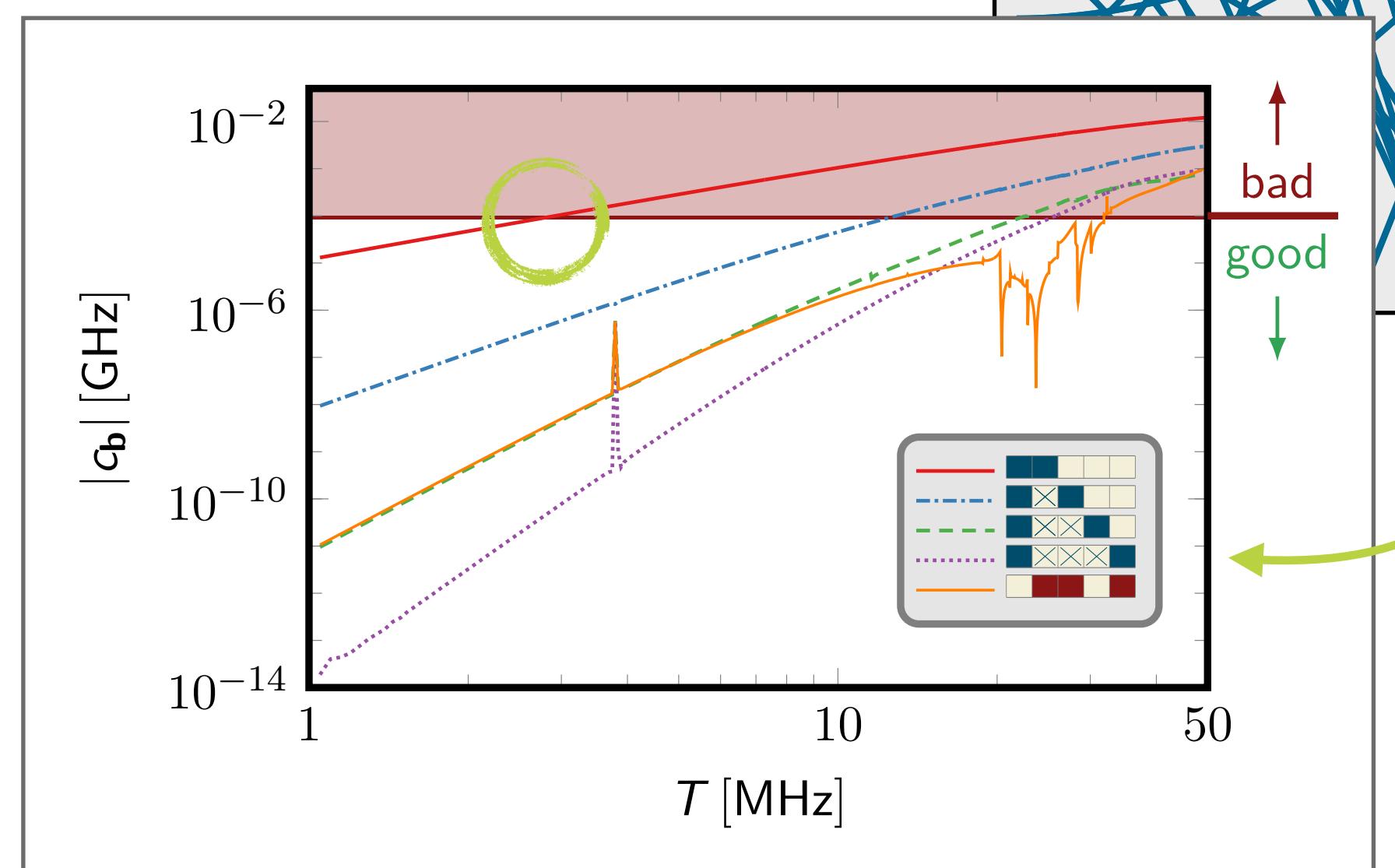
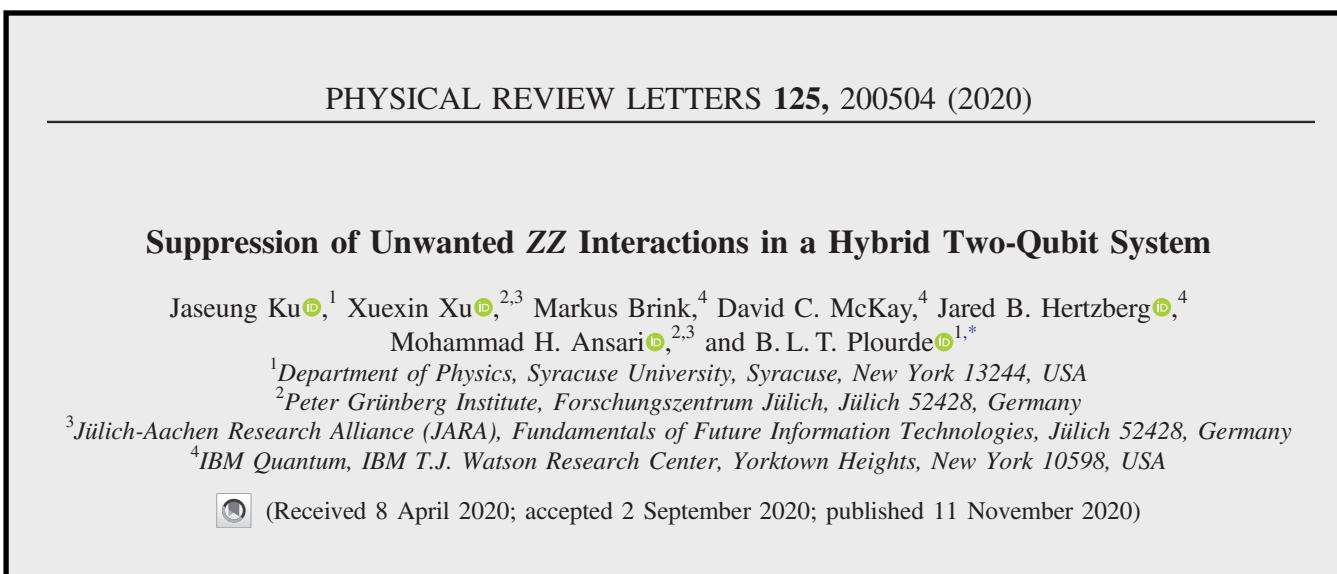
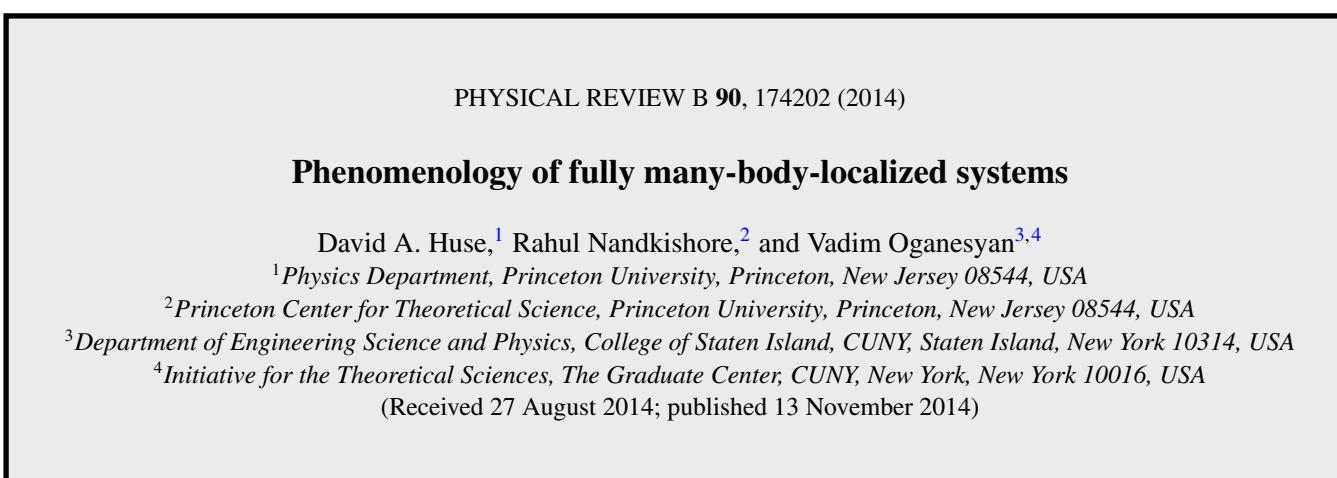
correlations

ZZ couplings & more

p-qubits and I-qubits

$$H = \sum_i h_i \tau_i^z + \sum_{ij} J_{ij} \tau_i^z \tau_j^z + \sum_{ijk} K_{ijk} \tau_i^z \tau_j^z \tau_k^z + \dots$$

τ - Hamiltonian
of many-body localization



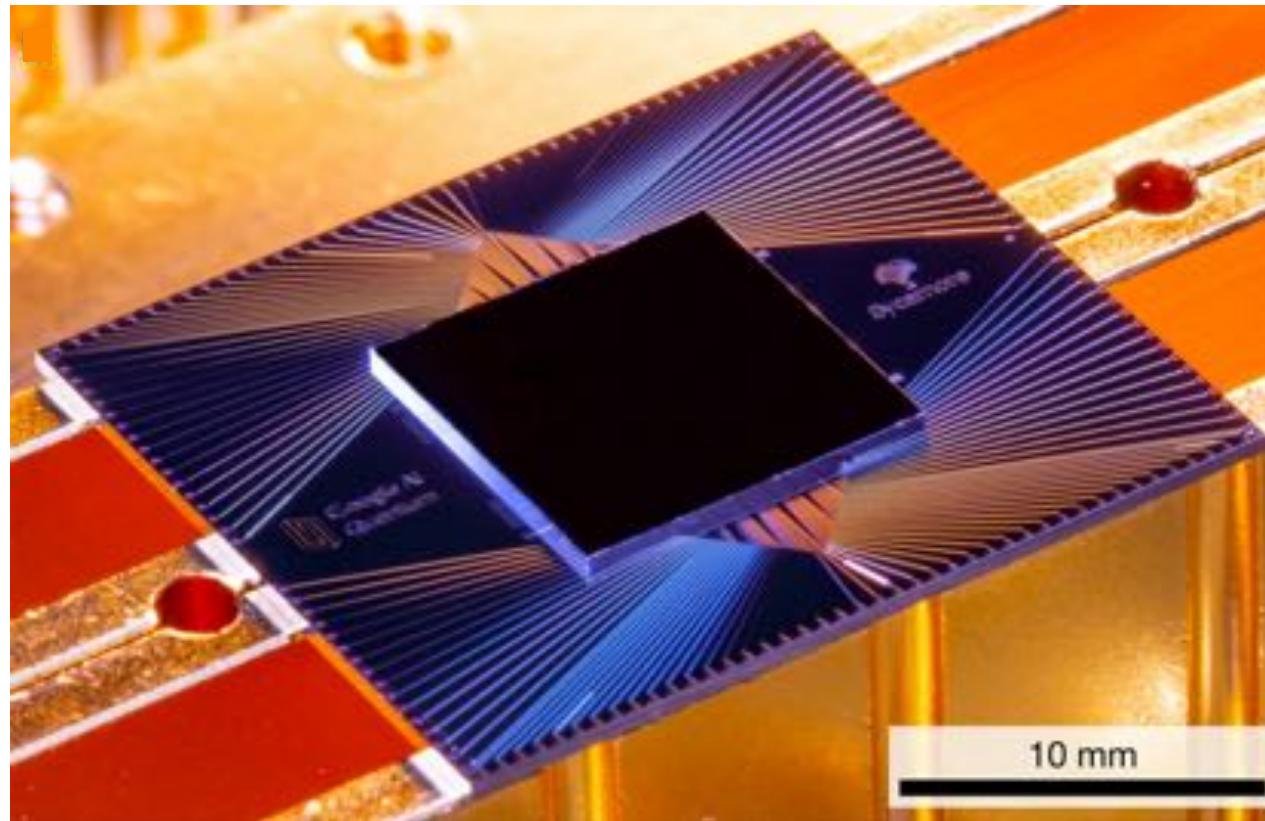
I-qubits

Walsh transform

disorder engineering

or how much imperfection should we really tolerate?

Google quantum processor



Google's **frequency engineering**

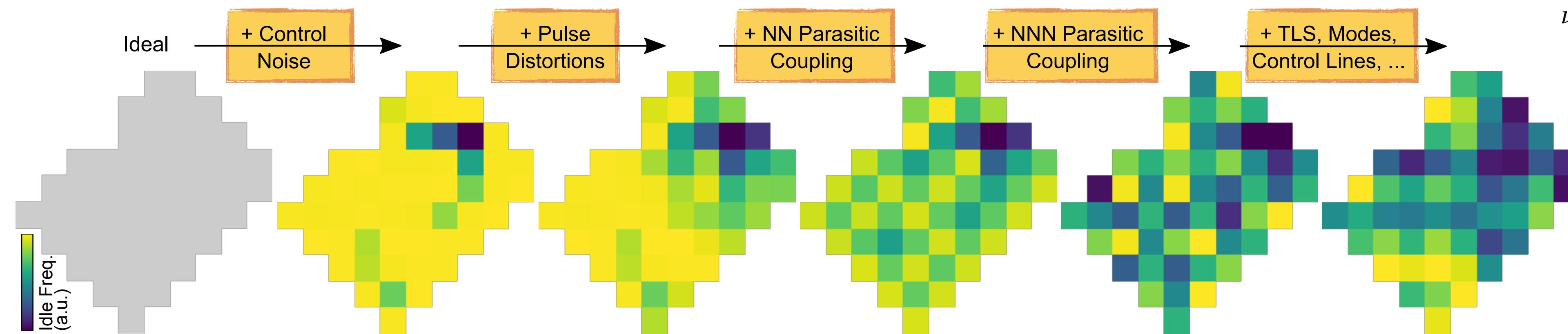
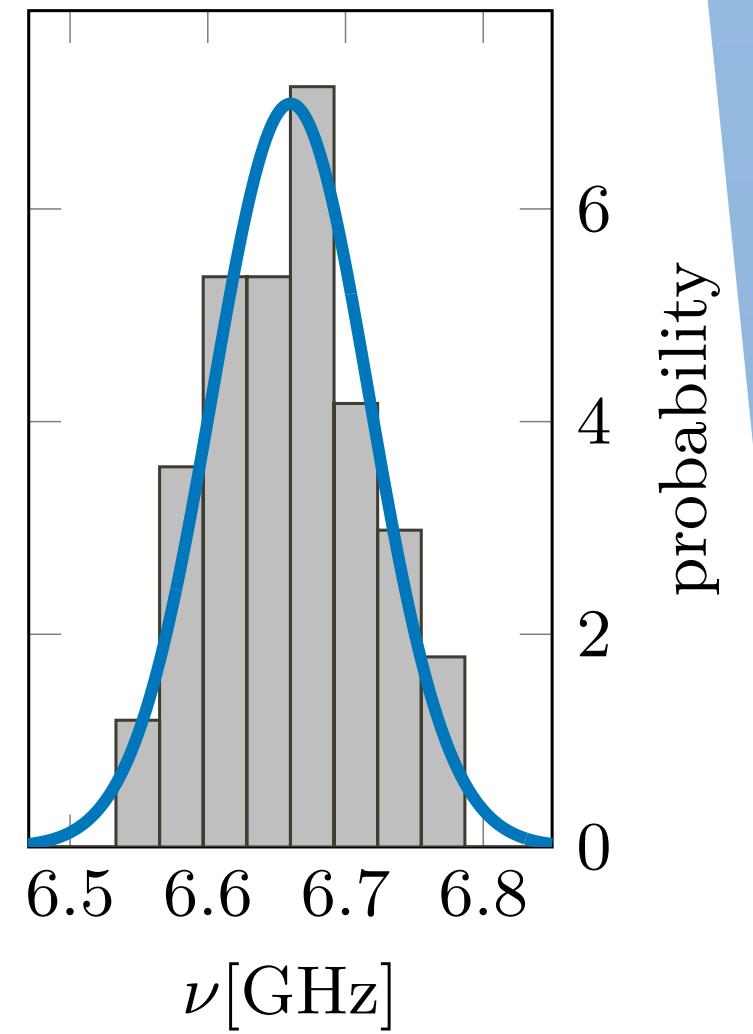


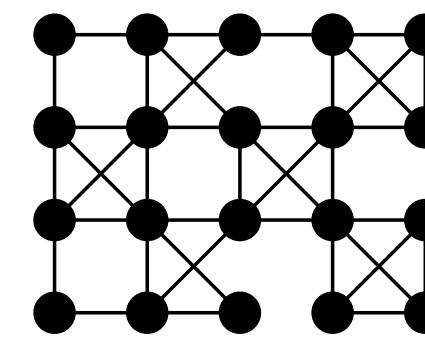
FIG. S12. **Idle frequency solutions found by our Snake optimizer with different error mechanisms enabled.** The optimizer makes increasingly complex tradeoffs as more error mechanisms are enabled. These tradeoffs manifest as a transition from a structured frequency configuration into an unstructured one. Similar tradeoffs are simultaneously made in optimizing interaction and readout frequencies. Optimized idle and interaction operating frequencies are shown in Figure S13 and optimized readout frequencies are shown in Figure S20. Color scales are chosen to maximize contrast. Grey indicates that

IBM quantum processors

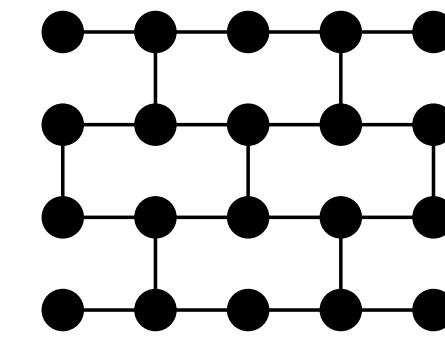
IBM's strategy to avoid

frequency crowding

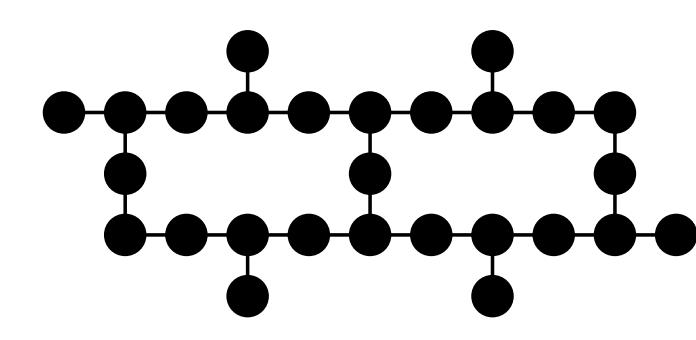
- optimize device geometry



2018

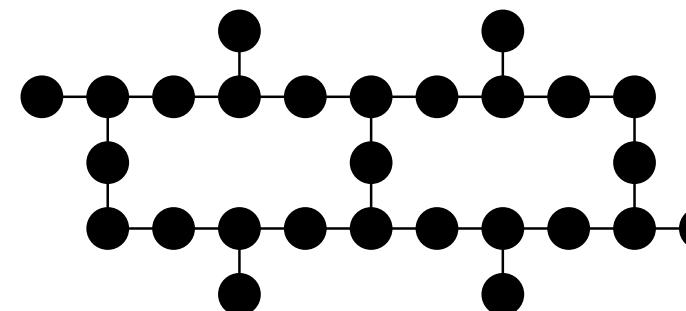


2019

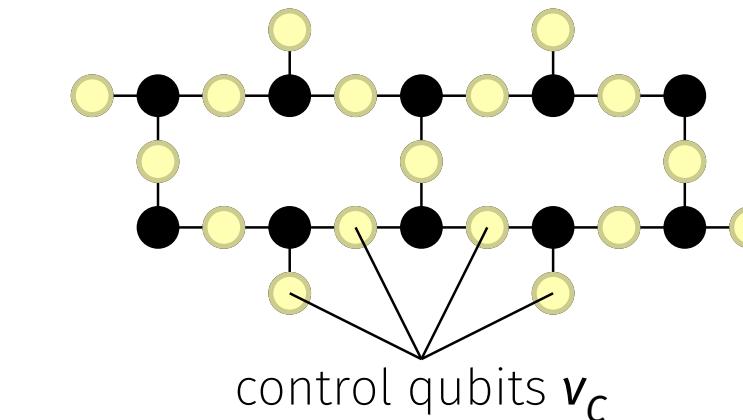


2020

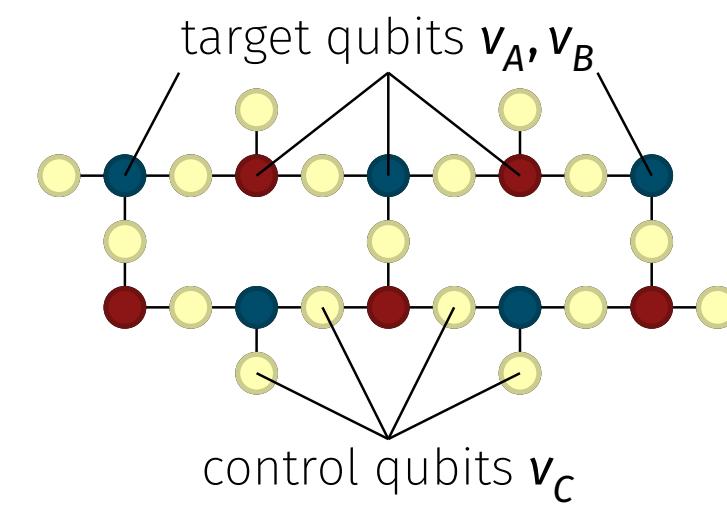
- frequency patterns



uniform



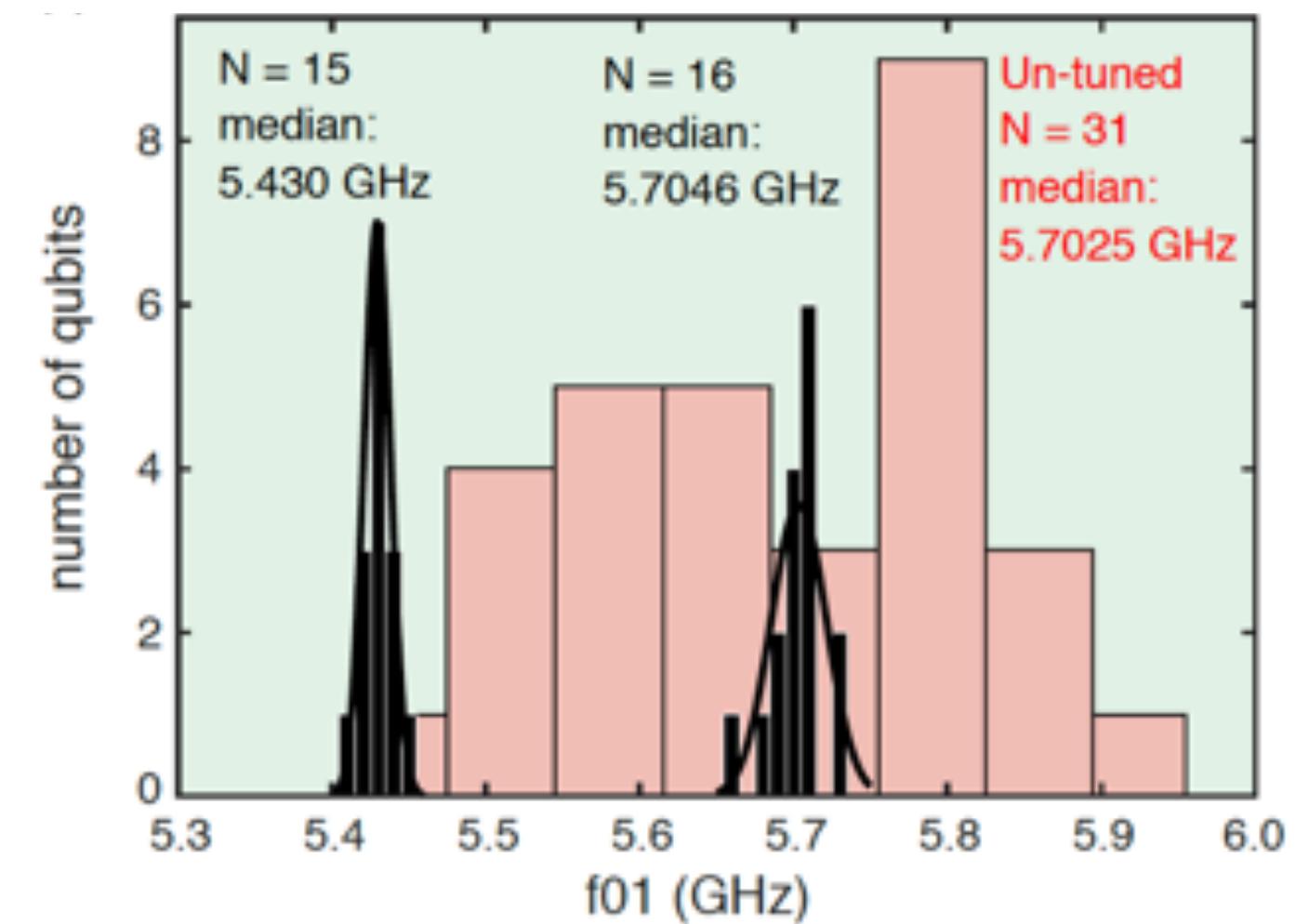
A - B



A - B - C

pattern engineering

via laser annealing



npj Quantum Information

ARTICLE OPEN

Laser-annealing Josephson junctions for yielding scaled-up superconducting quantum processors

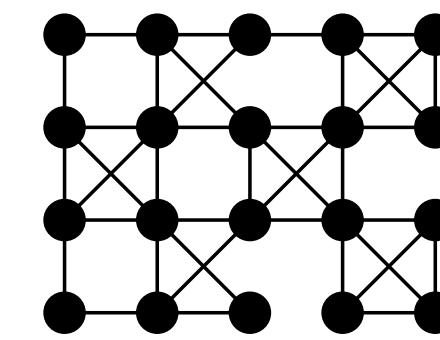
Jared B. Hertzberg , Eric J. Zhang¹, Sami Rosenblatt , Easwar Magesan¹, John A. Smolin¹, Jeng-Bang Yau¹, Vivekananda P. Adiga , Martin Sandberg , Markus Brink , Jerry M. Chow¹ and Jason S. Orcutt

IBM quantum processors

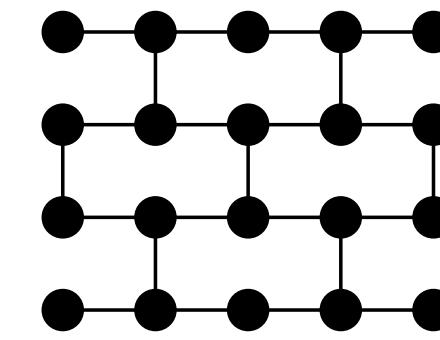
IBM's strategy to avoid

frequency crowding

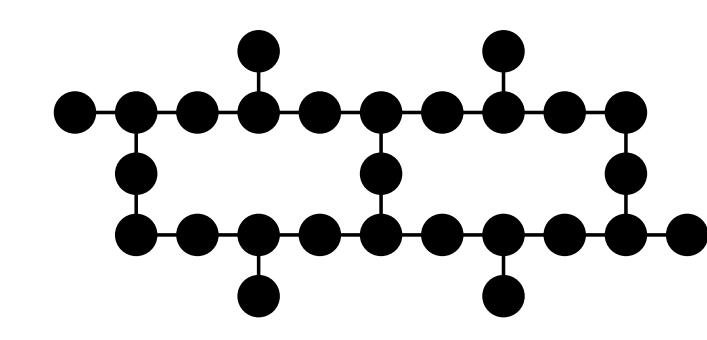
- optimize device geometry



2018

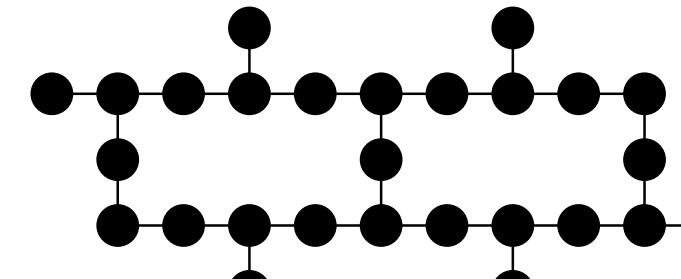


2019

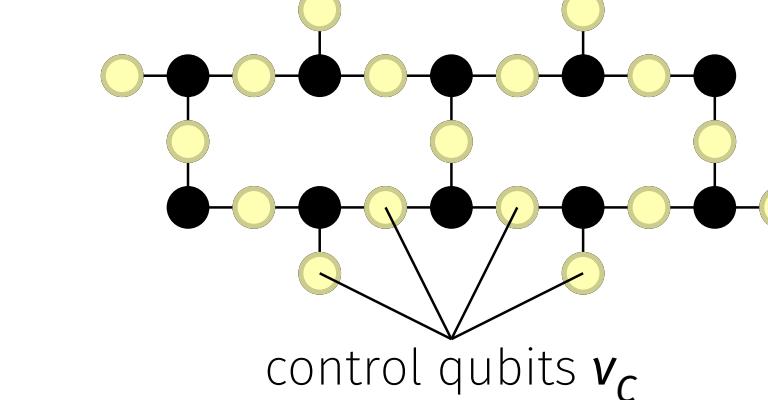


2020

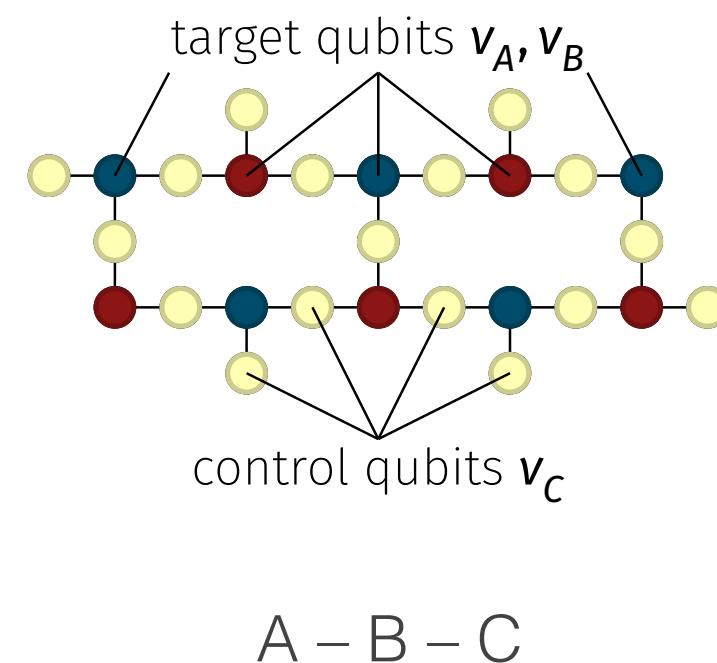
- frequency patterns



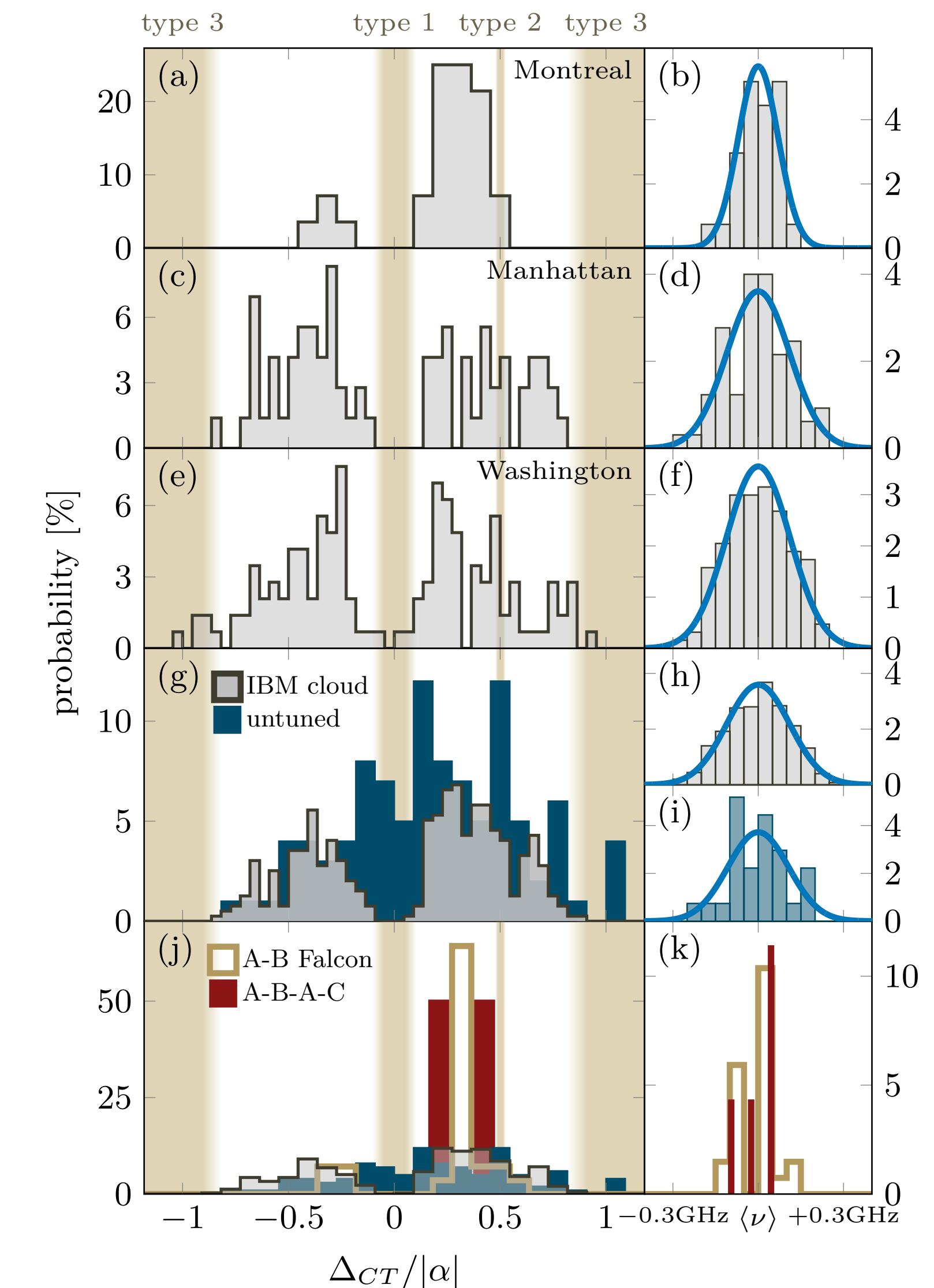
uniform



A - B

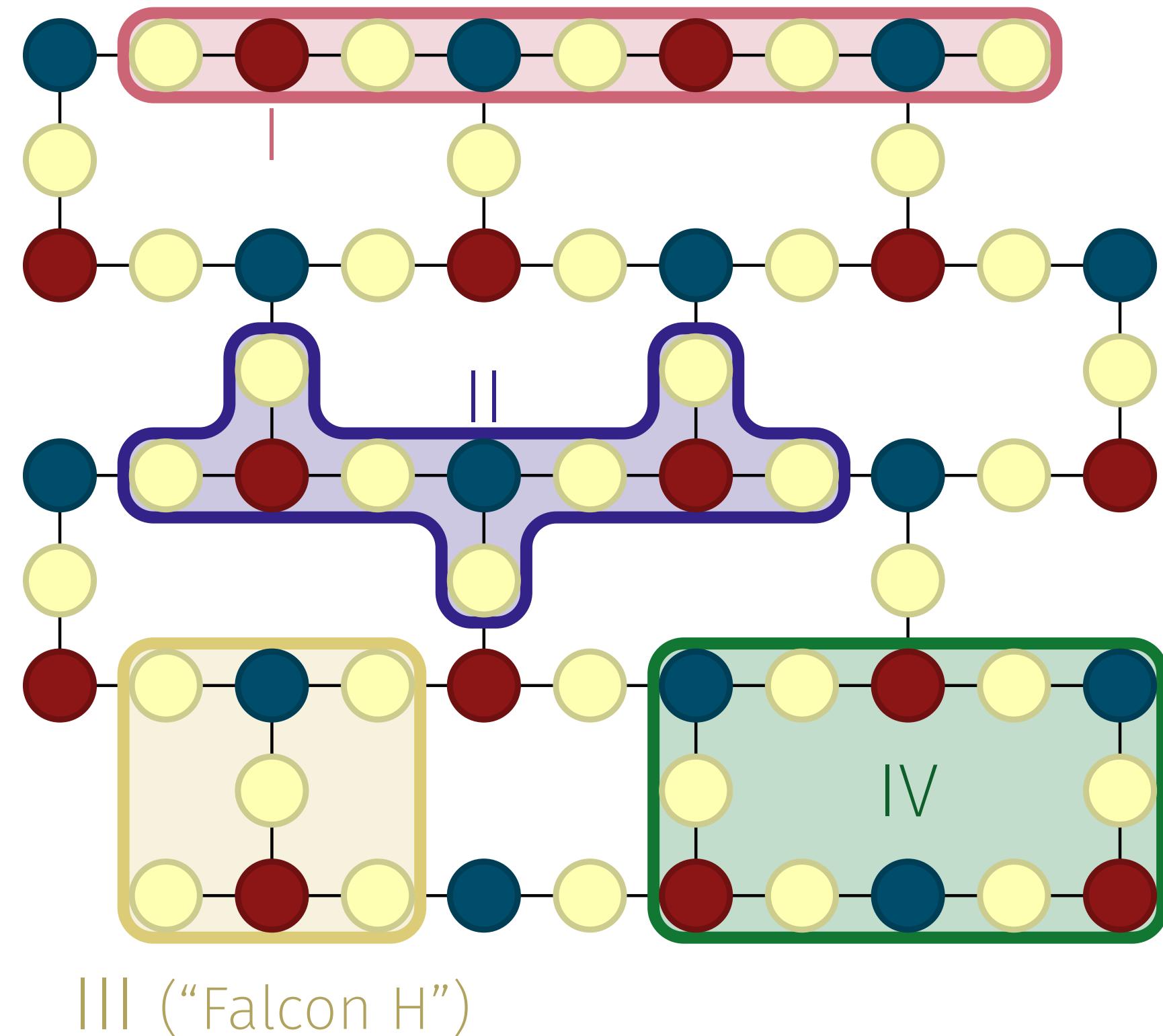


A - B - C

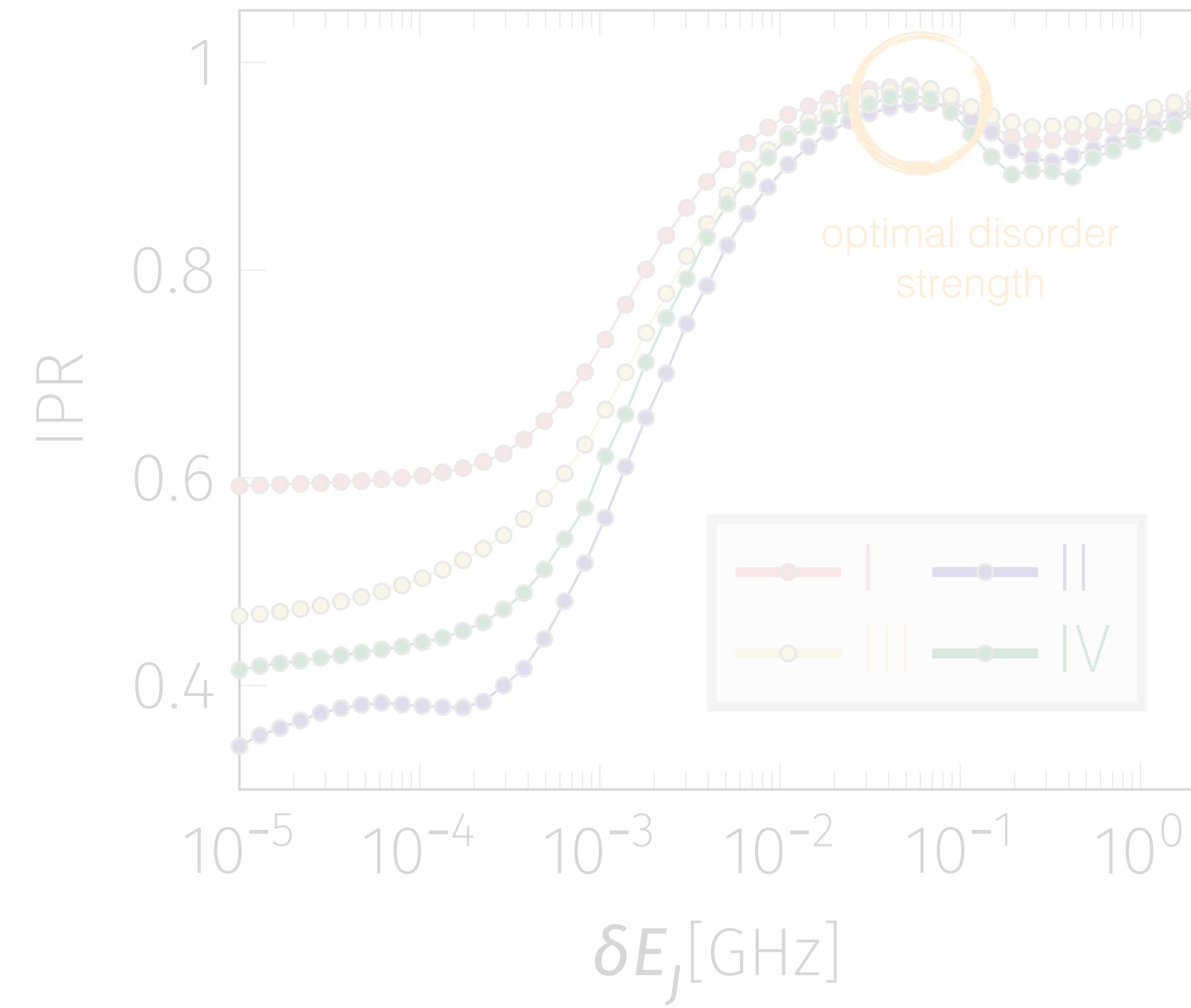


A – B – C frequency patterns

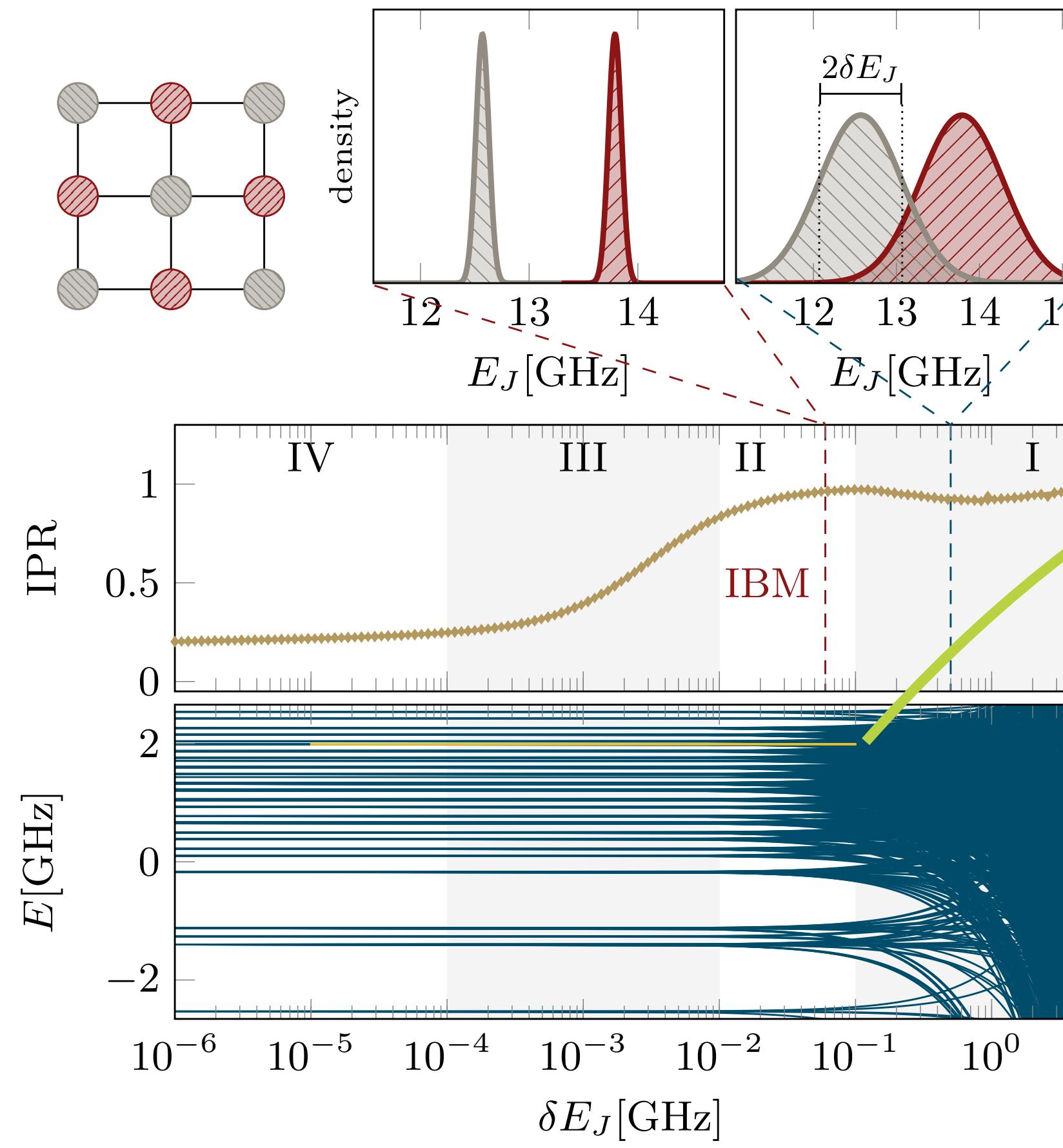
device layouts



inverse participation ratio

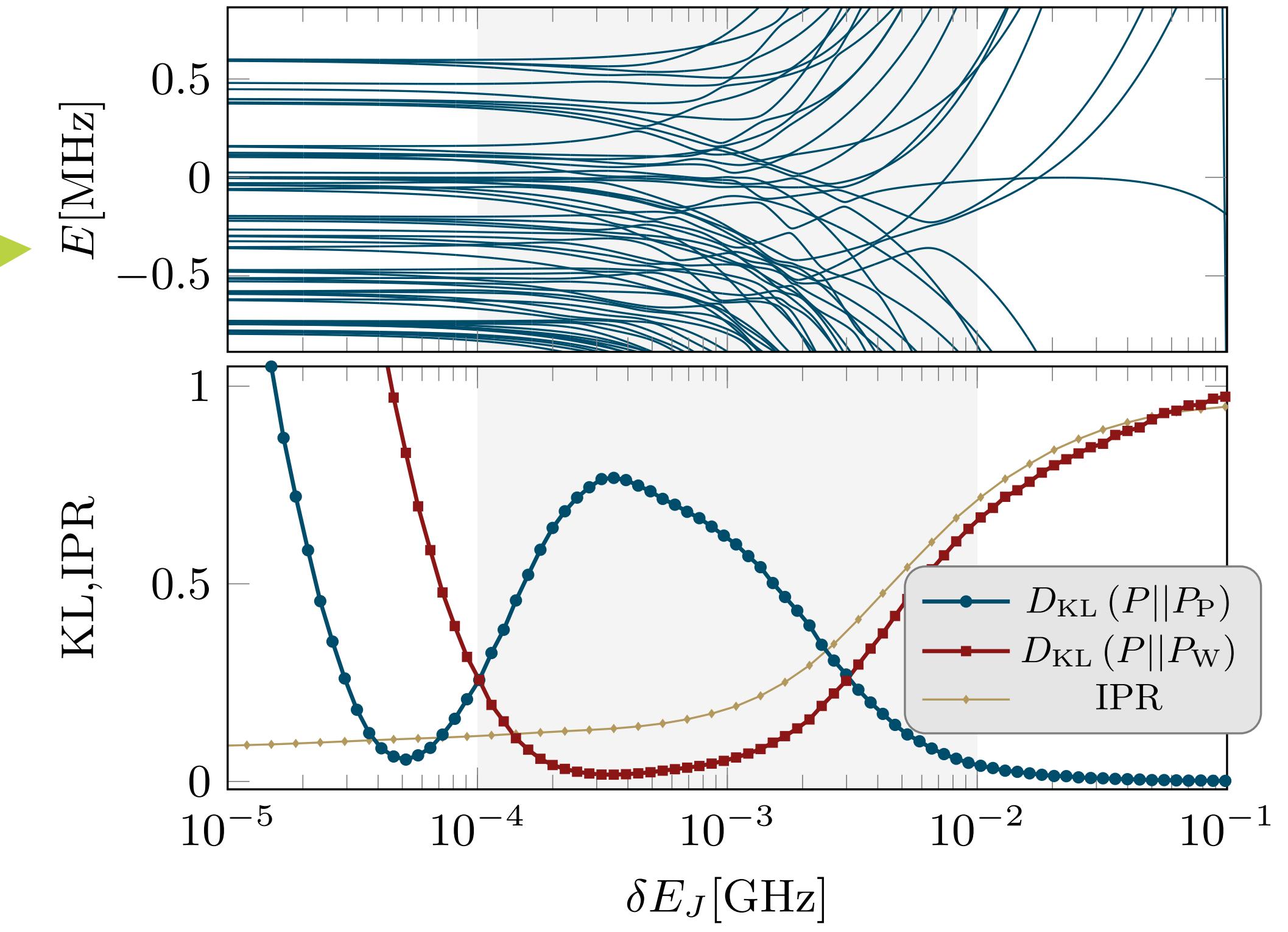


extreme disorder engineering



staggered
disorder
regimes

evolution of
5-excitation
bundle



reentrant chaotic behavior
(multiplet delocalization)

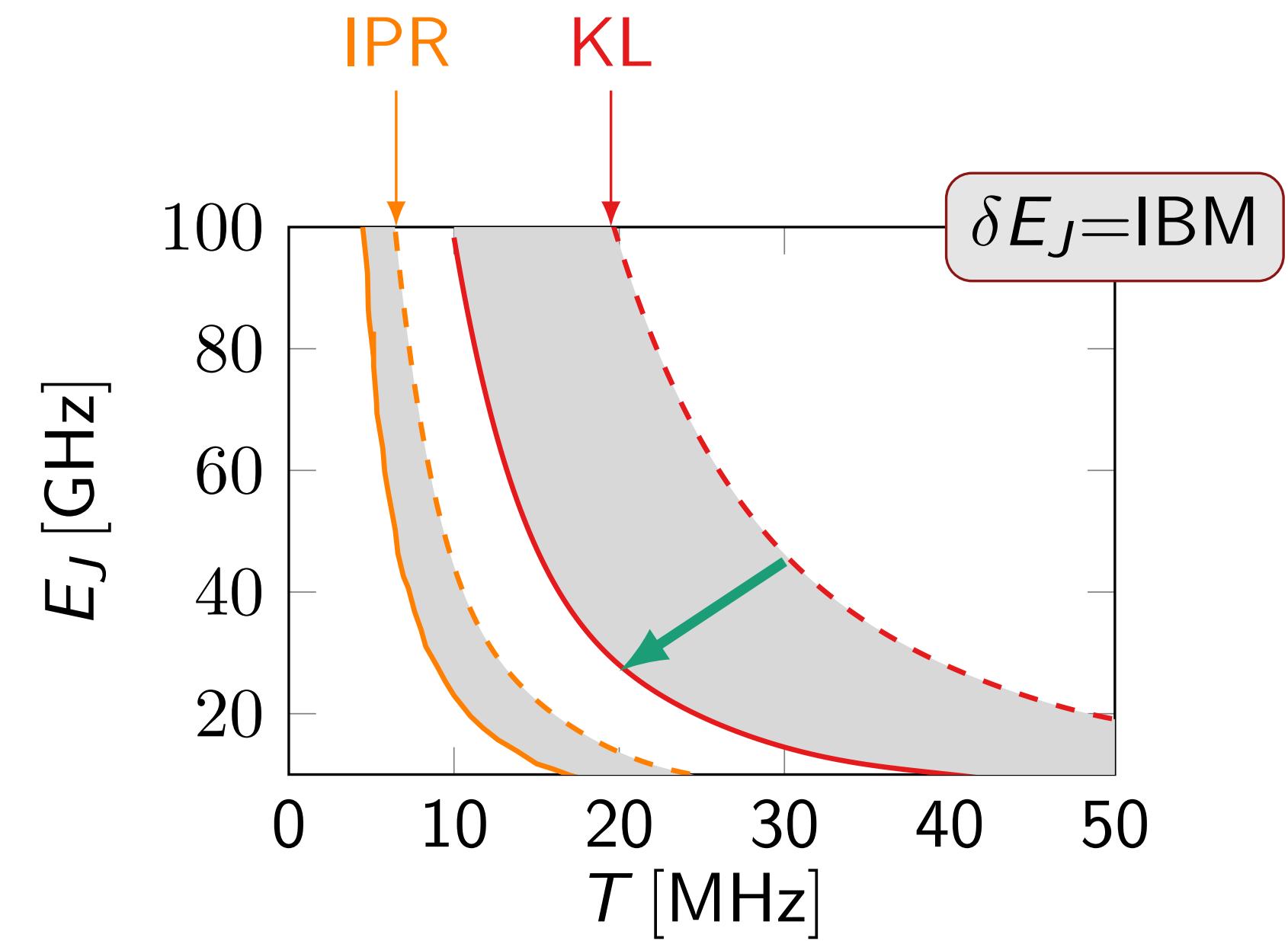
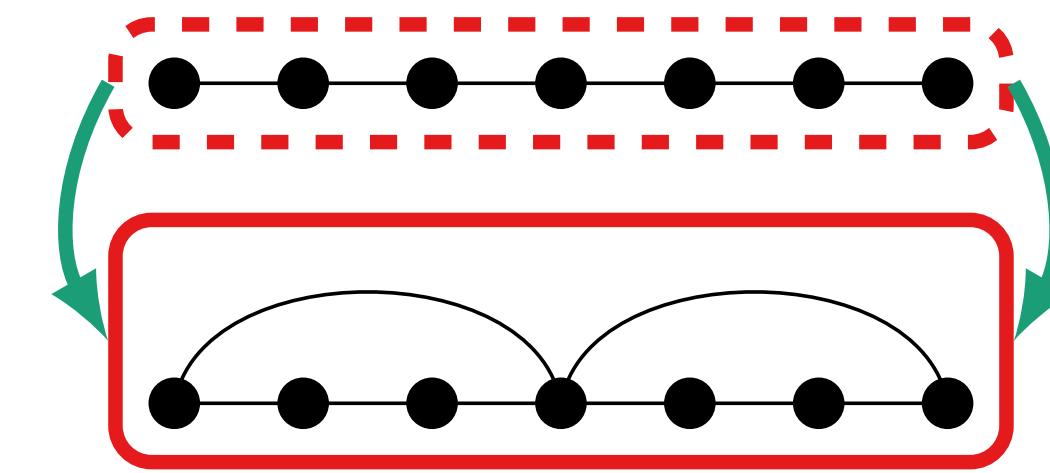
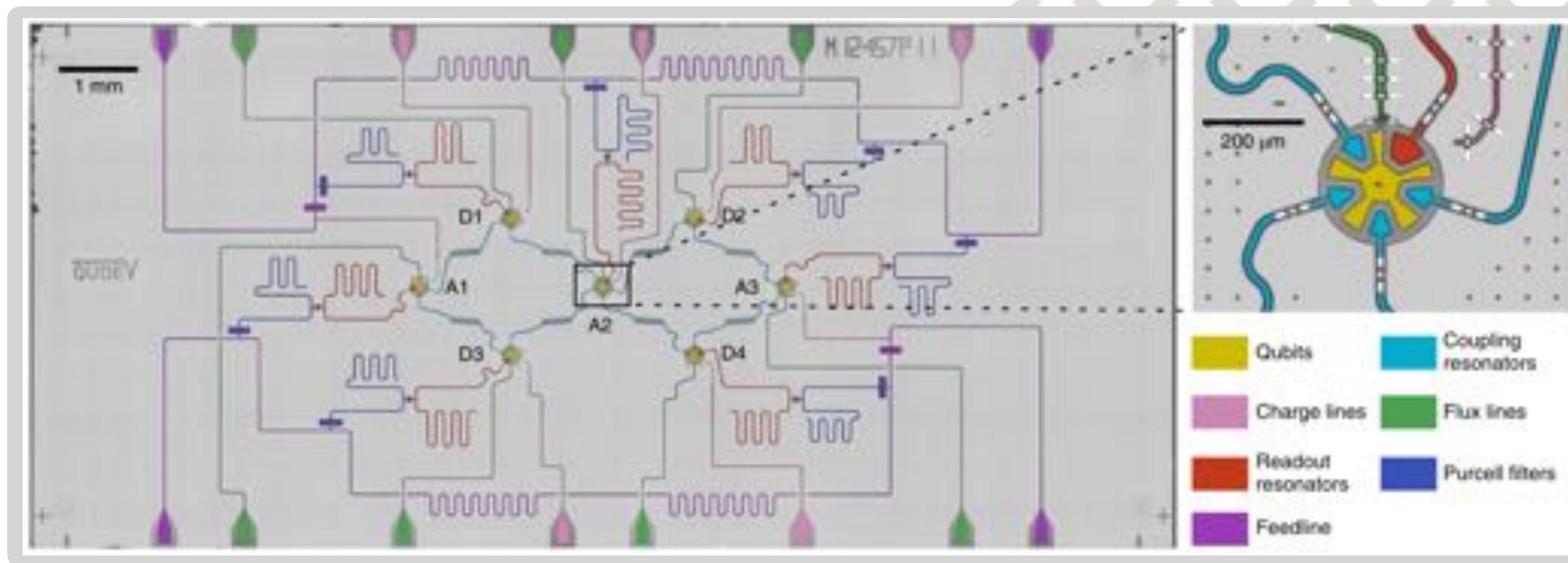
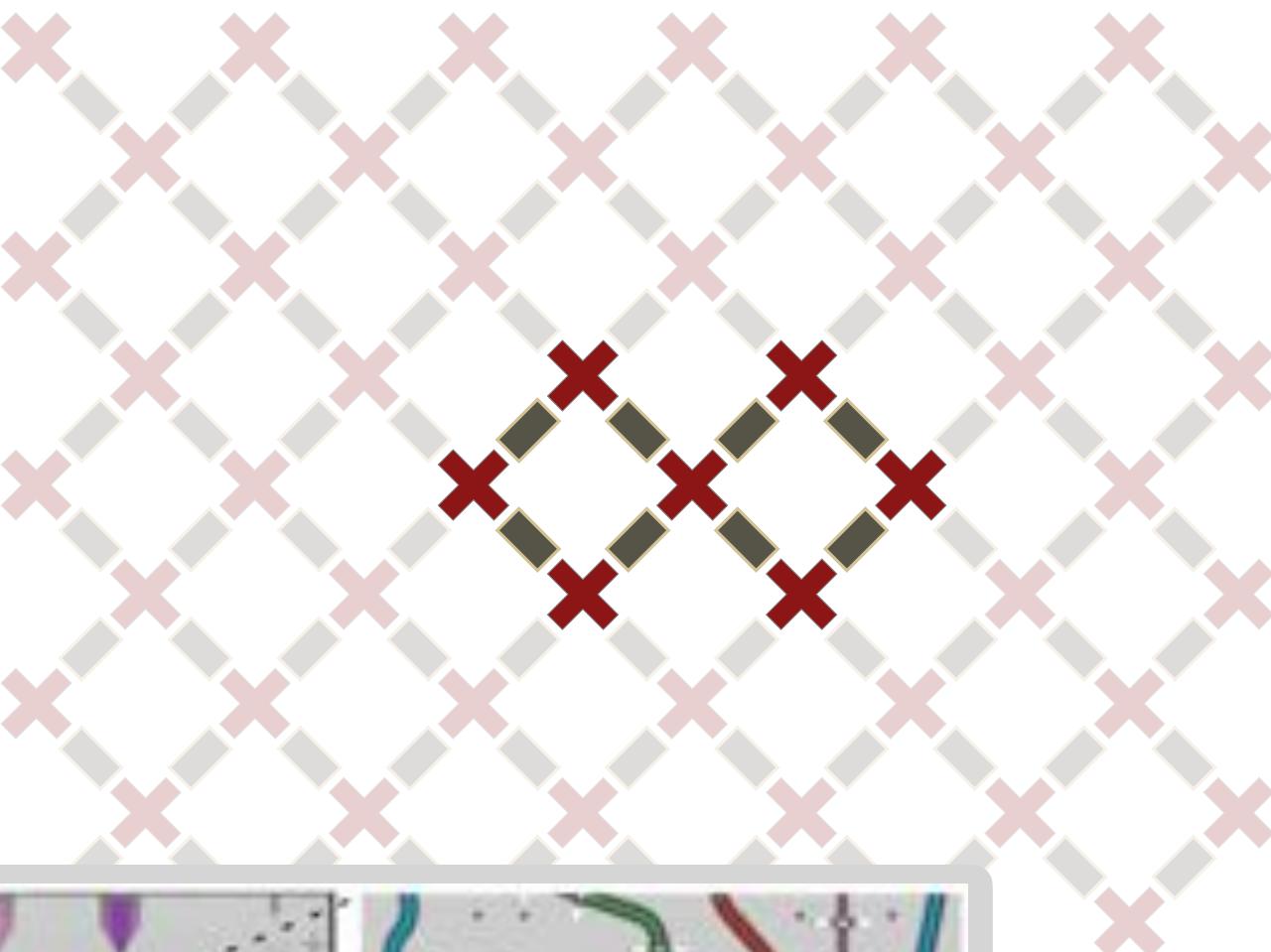


2D geometries

surface codes

Google's
sycamore processor

surface 7



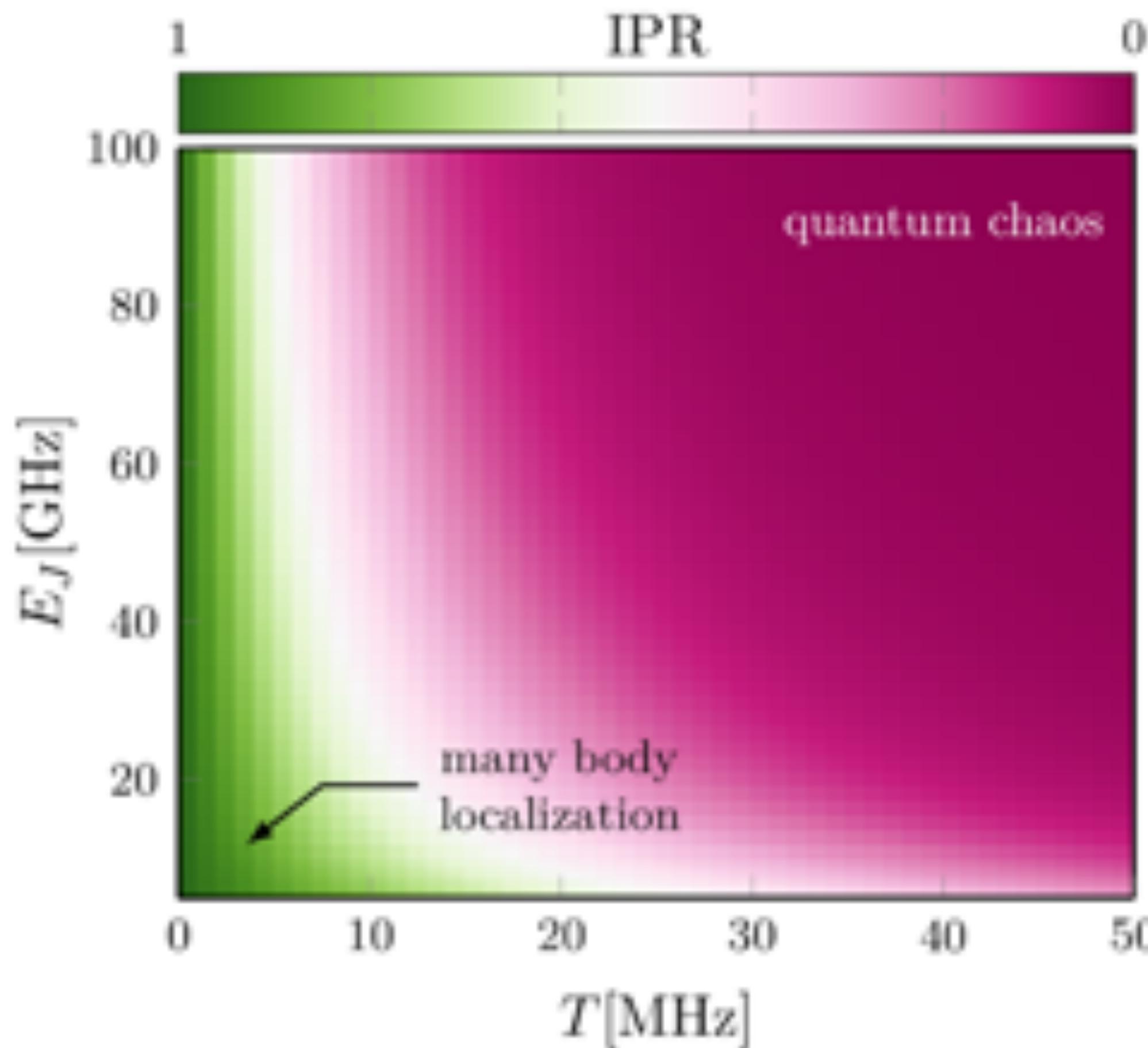


design simulations

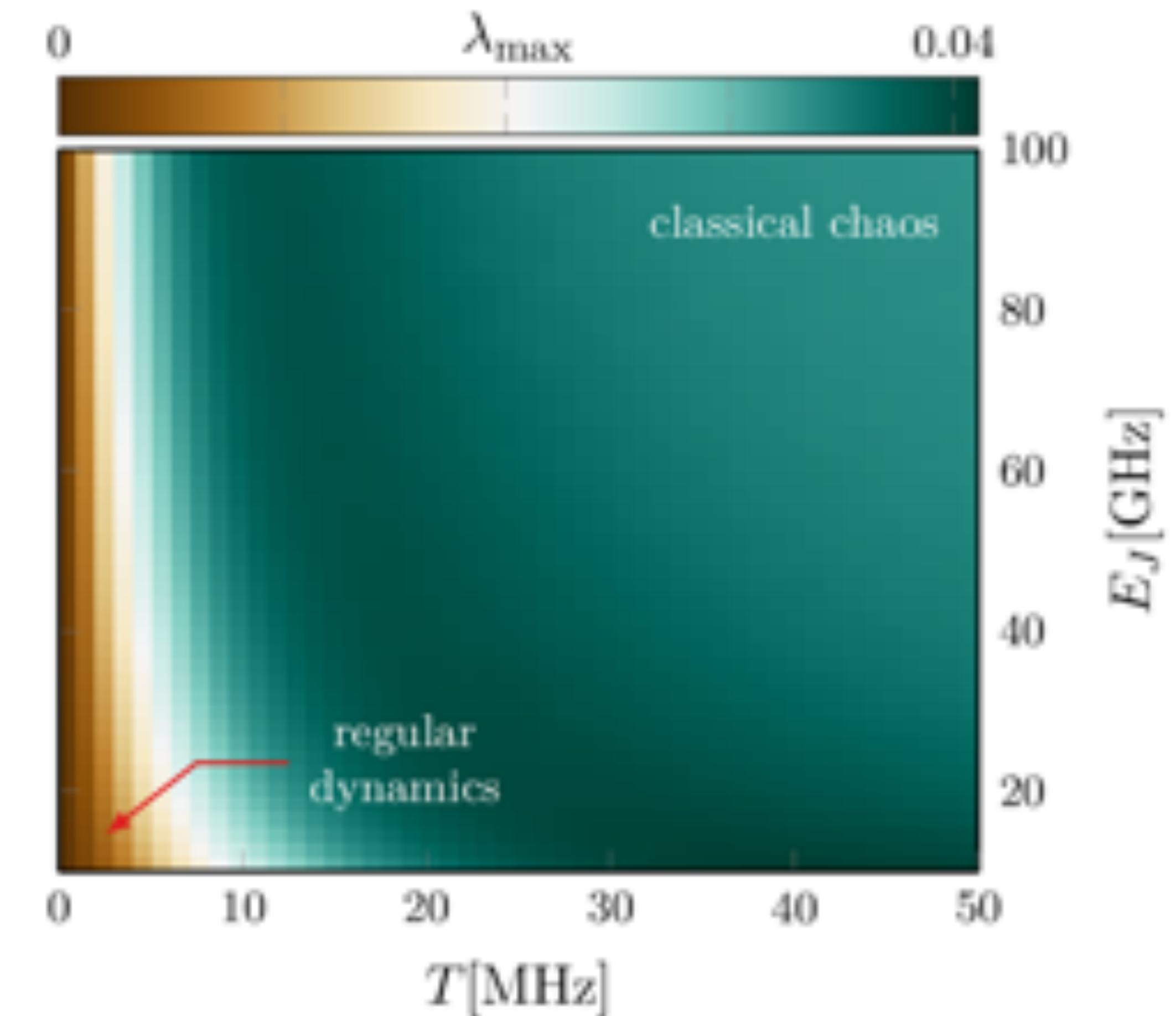
or how can we help avoiding chaos?

many-body numerics to the rescue

quantum simulations

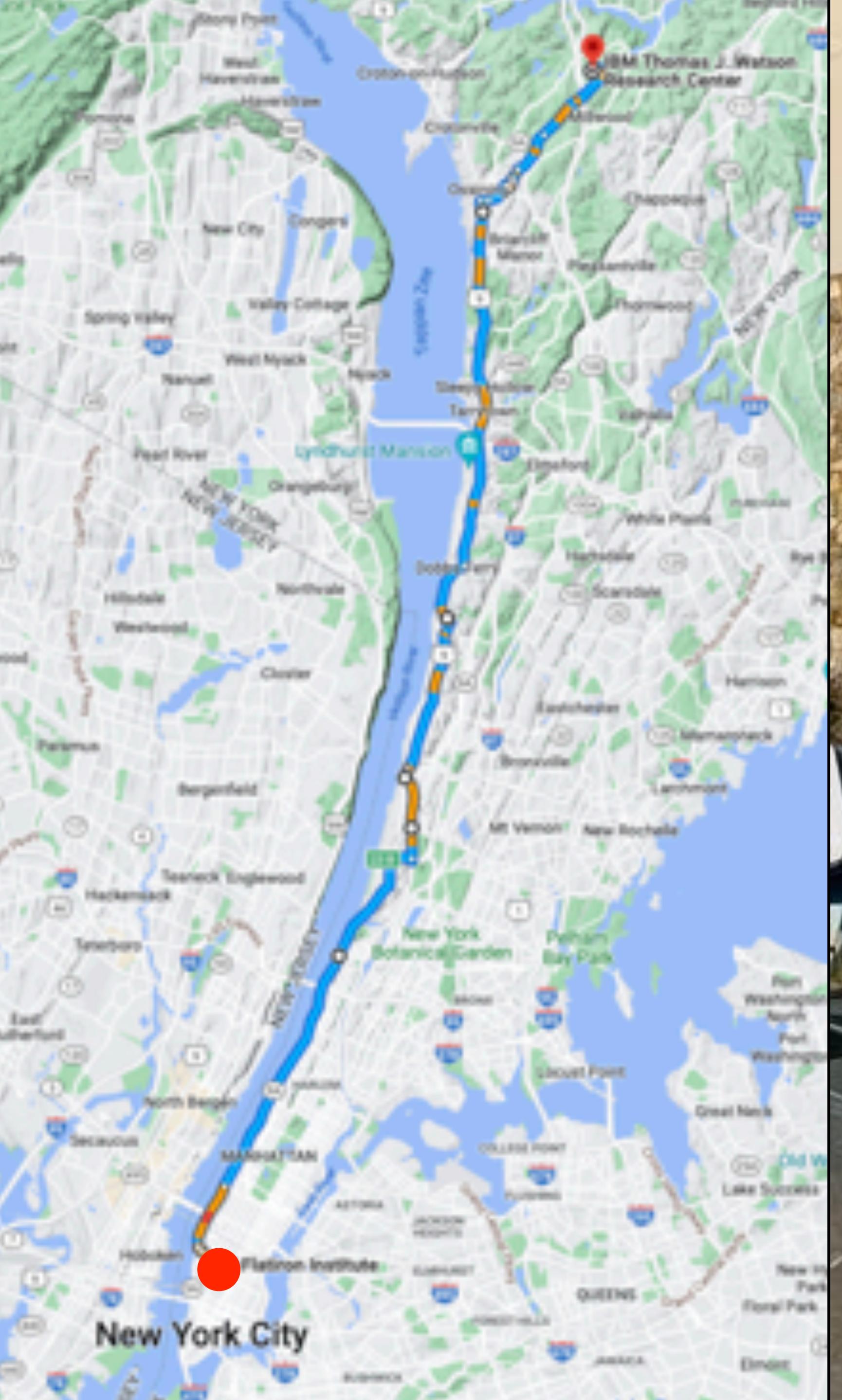


classical simulations





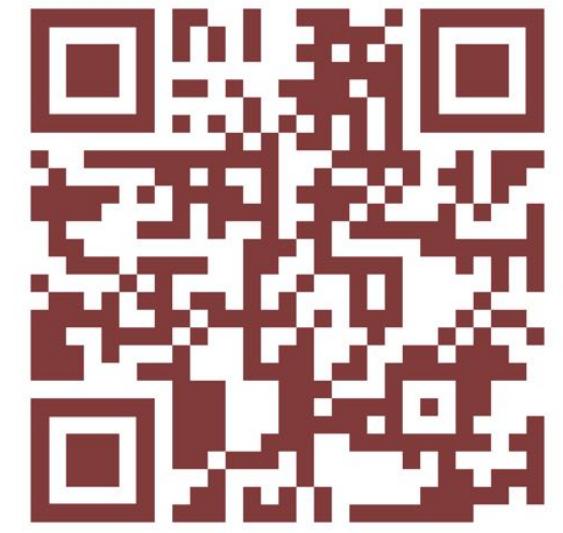
Where to go
from here?



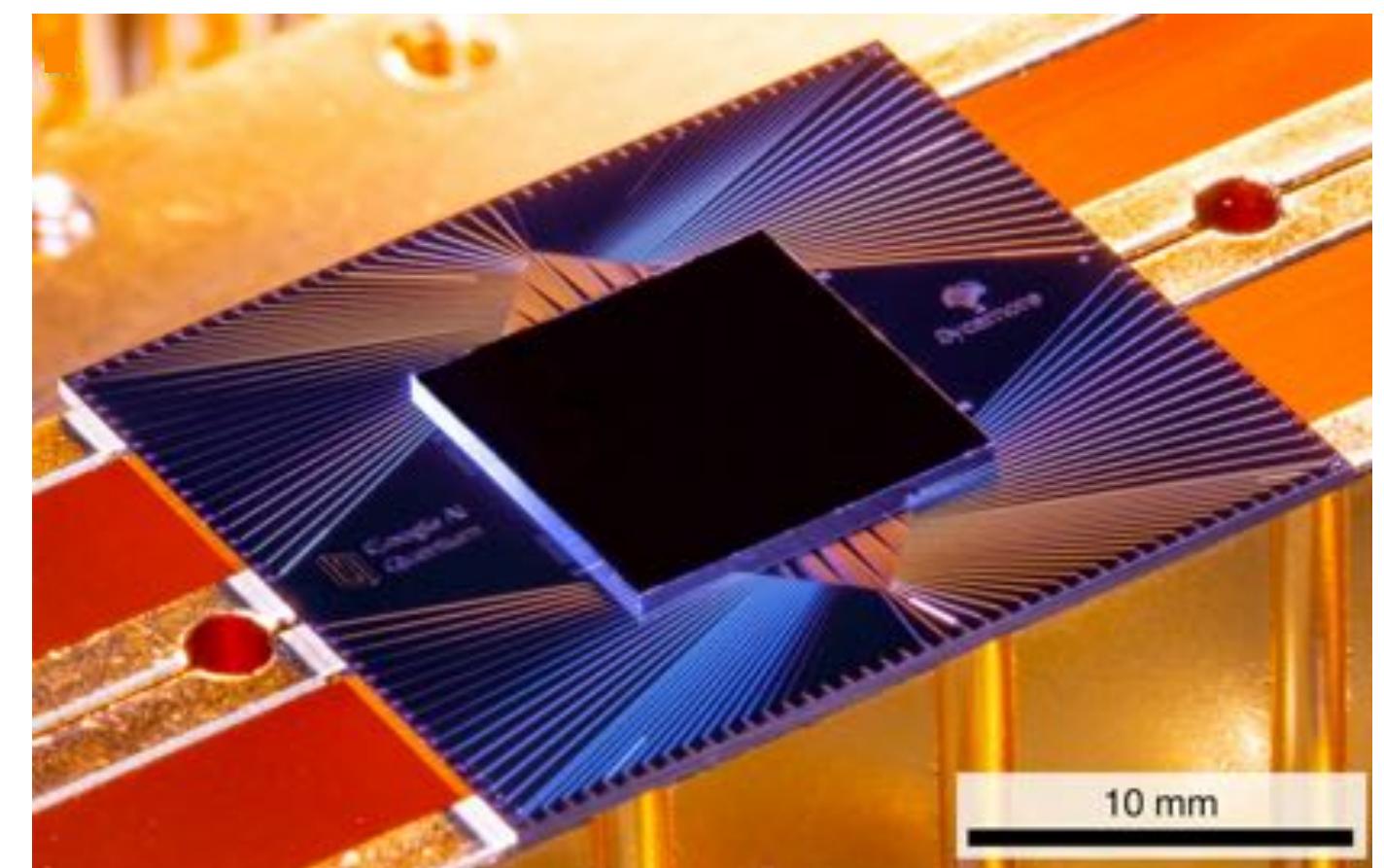
summary

Nature Comm. (2022)

Take-away messages



- The transition to **digital quantum computing** has been ushered in by “noisy intermediate-scale quantum” **NISQ devices**.
- **Tolerating imperfections** has been a key **guiding principle**.
- **Transmon qubit architectures** need to balance **intentional disorder** and **non-linear couplings**.
- **Quantum many-body perspective** – stay close to **many-body localization** and away from **chaos**.





Quantum Computing

“al dente”

Thanks!