

9th exercise sheet on Relativity and Cosmology I

Winter term 2015/16

Deadline for delivery: Thursday, 7th January 2016 during the exercise class.

Exercise 23 (8 credit points): *Dust*

- 23.1** Derive the continuity equation and the Euler equation for dust given in the lecture within the framework of special relativity.
- 23.2** Show that in an arbitrary reference frame it follows from the conservation of the energy–momentum tensor of dust that dust particles move on geodesics.

Exercise 24 (12 credit points): *Ideal fluid*

The energy–momentum tensor of an ideal fluid is given by

$$T^{\mu\nu} = \rho u^\mu u^\nu + P (u^\mu u^\nu + g^{\mu\nu}),$$

where u^μ is the four-velocity, ρ is the density and P is the pressure of the fluid.

- 24.1** Use the fact that the energy–momentum tensor of an ideal fluid is divergence-free to derive the continuity equation and the Euler equation.
- 24.2** Write out the continuity equation for the metric

$$g_{\mu\nu} = \text{diag} \left[-1, a(t)^2, a(t)^2, a(t)^2 \right].$$