

Possible proximity of the Iridates $(\text{Na,Li})_2\text{IrO}_3$ to a topologically ordered Mott insulator

Phase diagram of the Heisenberg-Kitaev model

APS March Meeting, Boston 2012

Simon Trebst
University of Cologne

Overview

honeycomb Iridates $(\text{Na,Li})_2\text{IrO}_3$

microscopics – Heisenberg-Kitaev model

outlook / a theorist's wishlist

In collaboration with

Hong-Chen Jiang (KITP), Zheng-Chen Gu (KITP), Xiao-Liang Qi (Stanford),
Johannes Reuther (UC Irvine), Ronny Thomale (Stanford)

Spin-orbit entanglement

- Spin-orbit coupling has long been considered an afterthought, a relativistic correction.
- Recent years have seen an plethora of novel states that arise solely due to SOC in a variety of underlying electronic states:
 - SOC-driven band inversion $\rightarrow$ topological insulator
 - SOC in chiral magnet MnSi $\rightarrow$ skyrmion lattices
 - SOC in Sr_2RuO_4 $\rightarrow$ $p_x + ip_y$ superconductor
 - This talk: SOC in correlated Mott insulators

Spin-orbit coupling in Mott insulators

Good candidate systems? – 5d transition metal oxides

- *strong* spin-orbit coupling
- *weak* Mott insulators
- *enhanced sensitivity* to crystal fields

Periodic Table of the Elements

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Legend:

- hydrogen
- alkali metals
- alkali earth metals
- transition metals
- poor metals
- nonmetals
- noble gases
- rare earth metals

The periodic table shows elements from Hydrogen (1) to Oganesson (118). The transition metals, located in the d-block (groups 3-10), are highlighted in red. A red circle is drawn around the transition metals in the 5th and 6th periods, specifically around the elements from Scandium (21) to Nickel (28) and from Yttrium (39) to Cadmium (48).

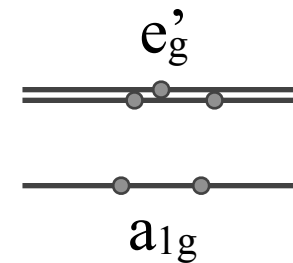
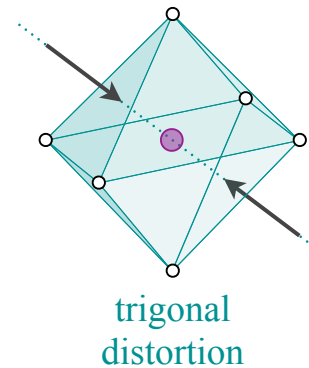
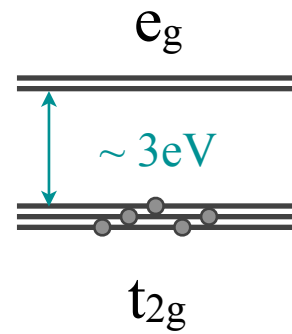
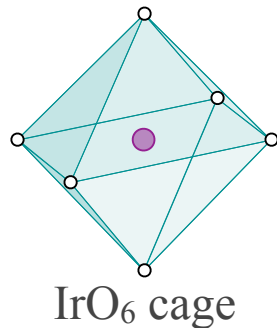
Spin-orbit entanglement in Iridates

most common
Iridium valence

Ir^{4+} ($5d^5$)

d-orbitals

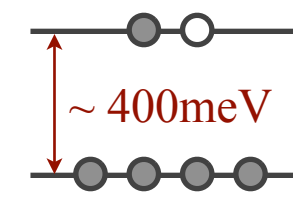
octahedral
crystal field



spin-orbit *locking*
via SOC

YB Kim's talk

spin-orbit
coupling
 $\vec{L} \cdot \vec{\sigma}$

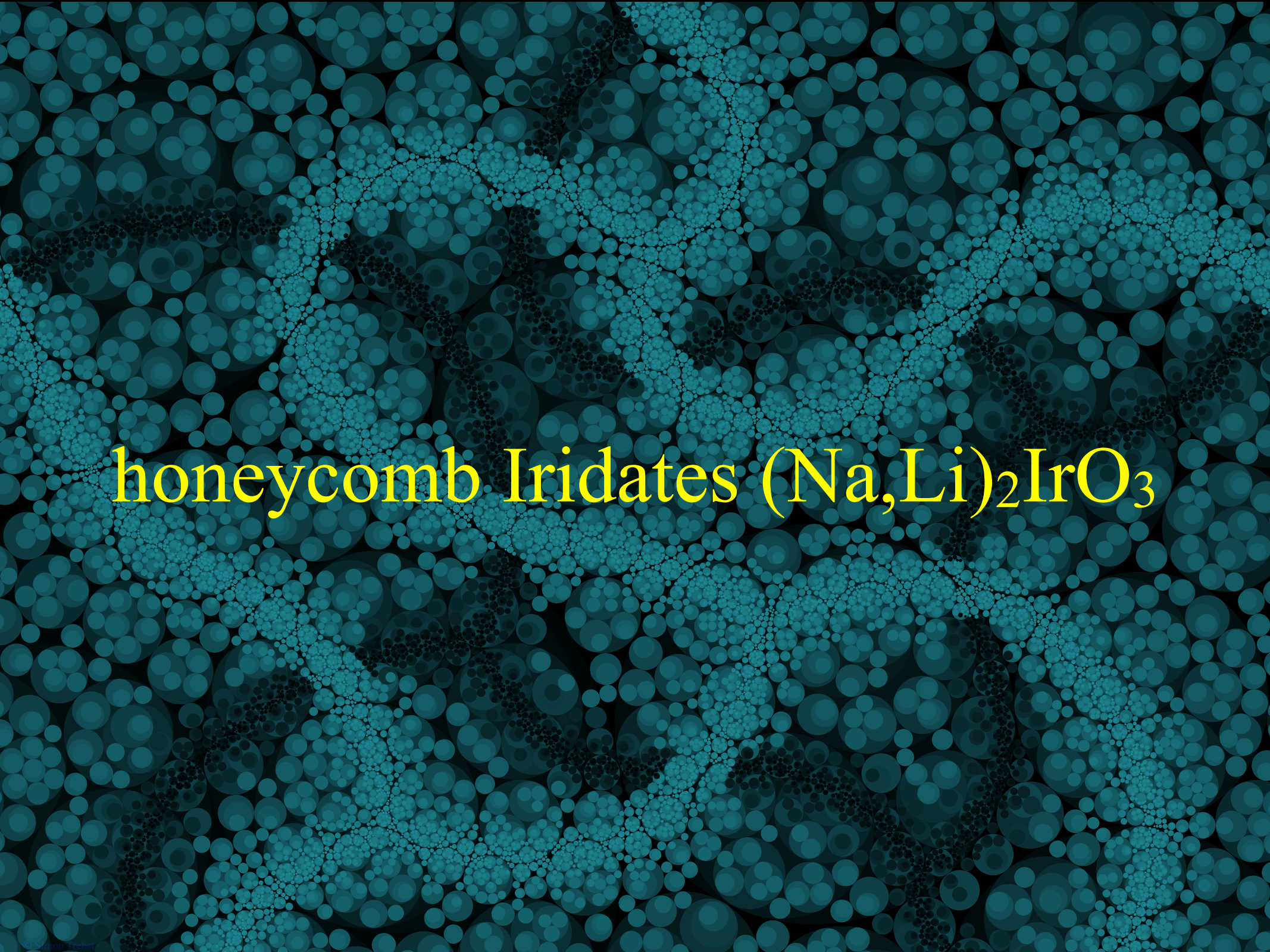


Sr_2IrO_4

B.J. Kim *et al.* PRL **101**, 076402 (2008)

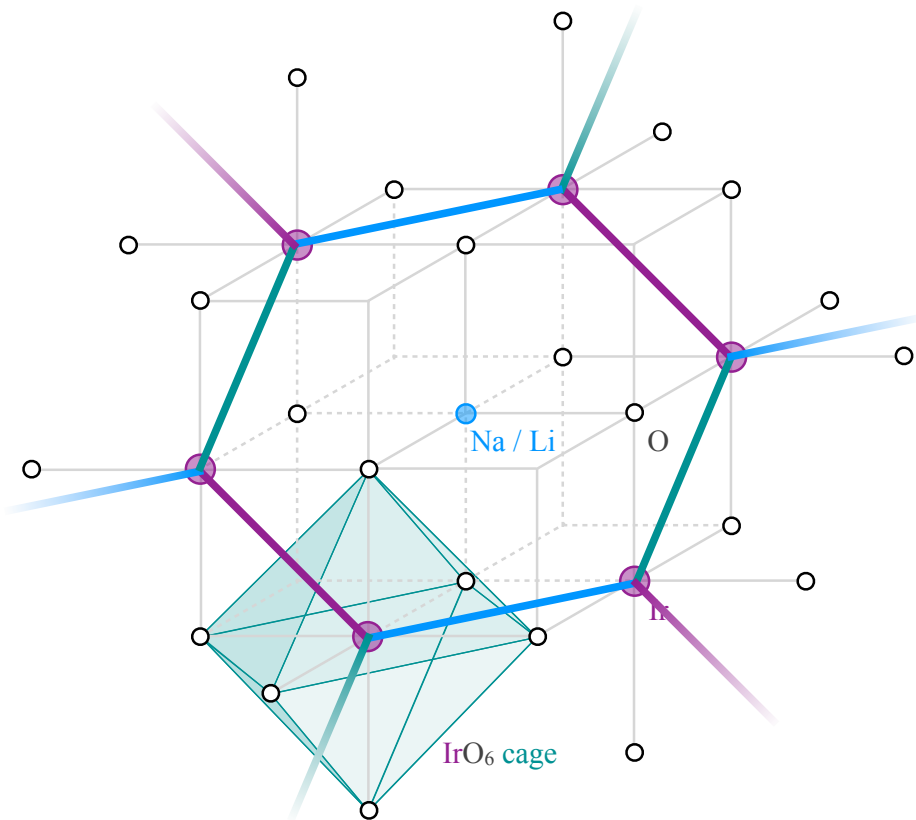
B.J. Kim *et al.* Science **323**, 1329 (2009)

$(\text{Na,Li})_2\text{IrO}_3$?



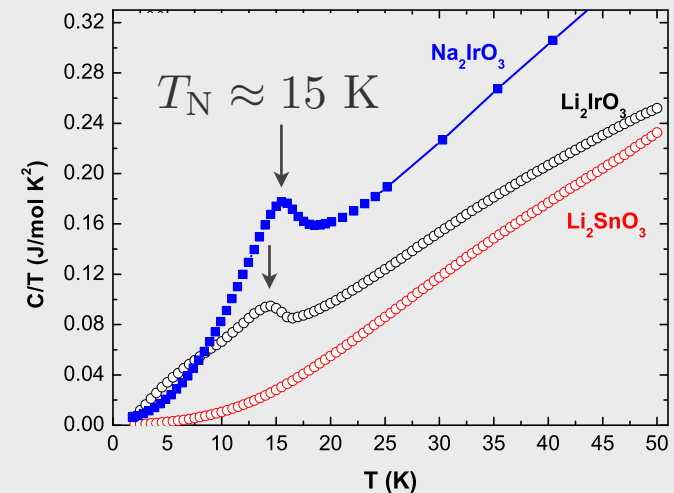
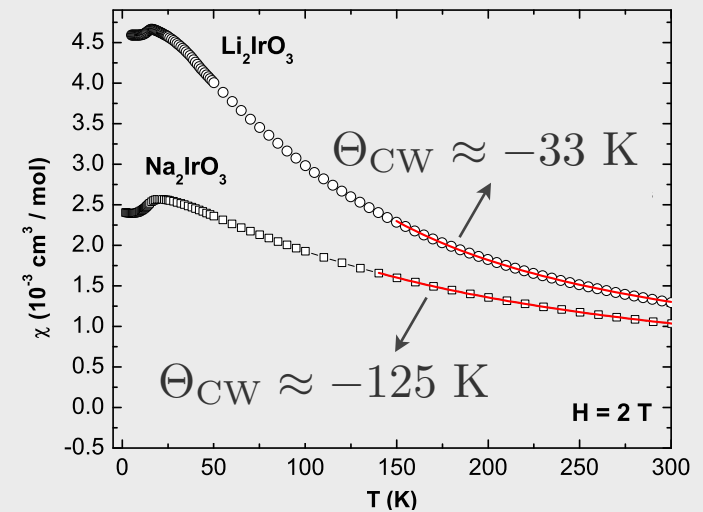
honeycomb Iridates $(\text{Na,Li})_2\text{IrO}_3$

$(\text{Na,Li})_2\text{IrO}_3$ – spin-orbit Mott insulators



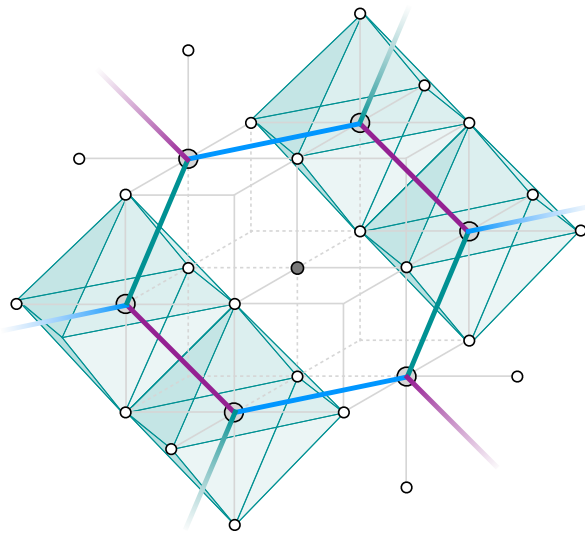
$$\text{Na}_2\text{IrO}_3 \quad \frac{|\Theta_{\text{CW}}|}{T_{\text{N}}} \approx 8$$

$$\text{Li}_2\text{IrO}_3 \quad \frac{|\Theta_{\text{CW}}|}{T_{\text{N}}} \approx 1.7$$

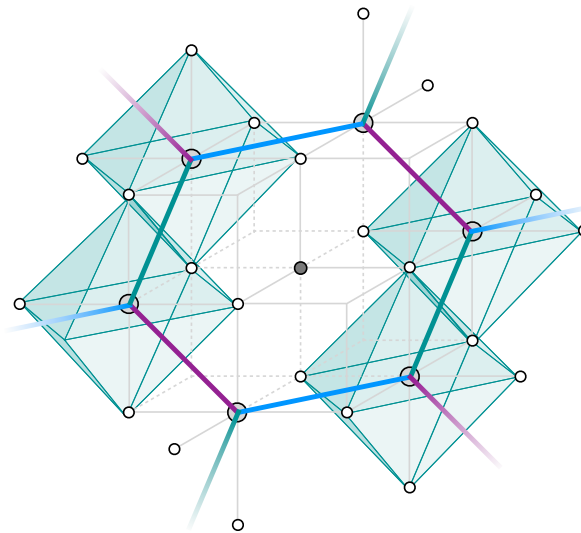


Experiments by Gegenwart group

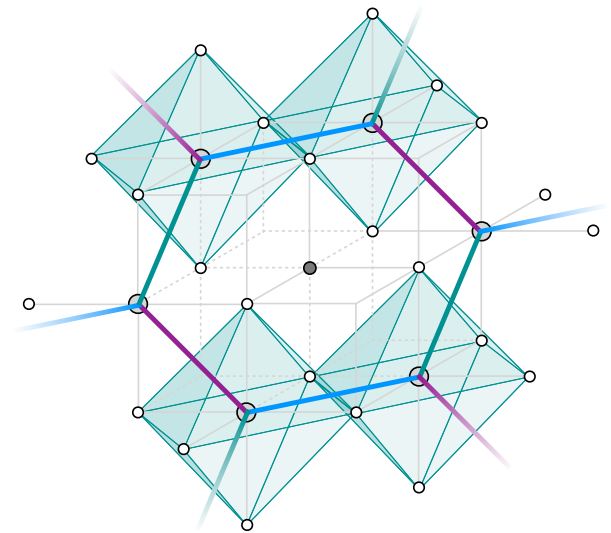
Microscopic exchange



“x-bonds”



“y-bonds”

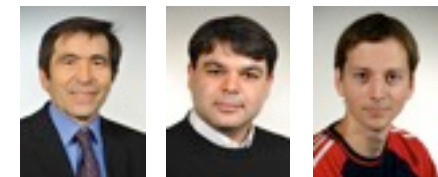


“z-bonds”

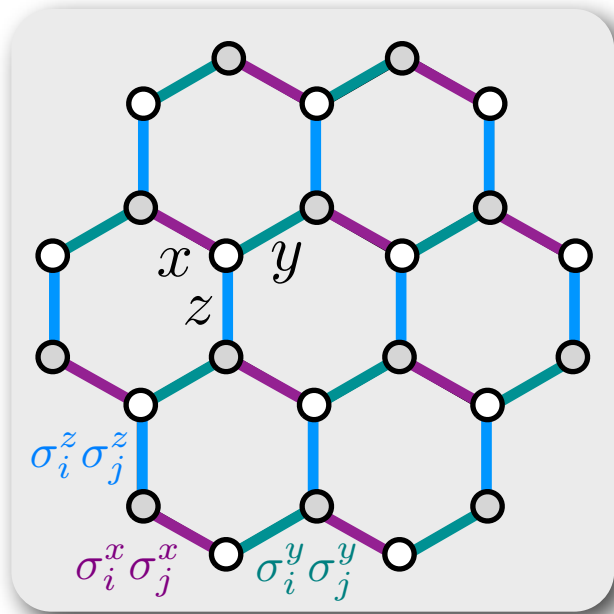
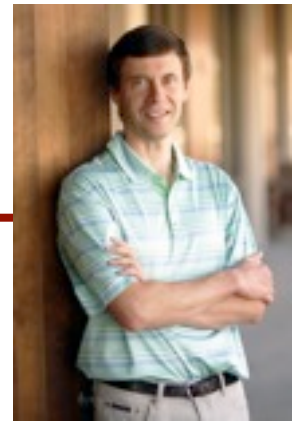
Exchange along all three bonds is mediated via **edge-sharing** IrO₆ octahedra, 90° Ir-O-Ir path.
Spin-orbit entangled degrees of freedom suggested to interact via “**Heisenberg-Kitaev**” model.

$$H_{\text{HK}} = (1 - \alpha) \sum_{\langle i, j \rangle} \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma\text{-links}} \sigma_i^\gamma \sigma_j^\gamma$$

G. Jackeli and G. Khaliullin, PRL **102**, 017205 (2009)
J. Chaloupka, G. Jackeli, and G. Khaliullin, PRL **105**, 027204 (2010)

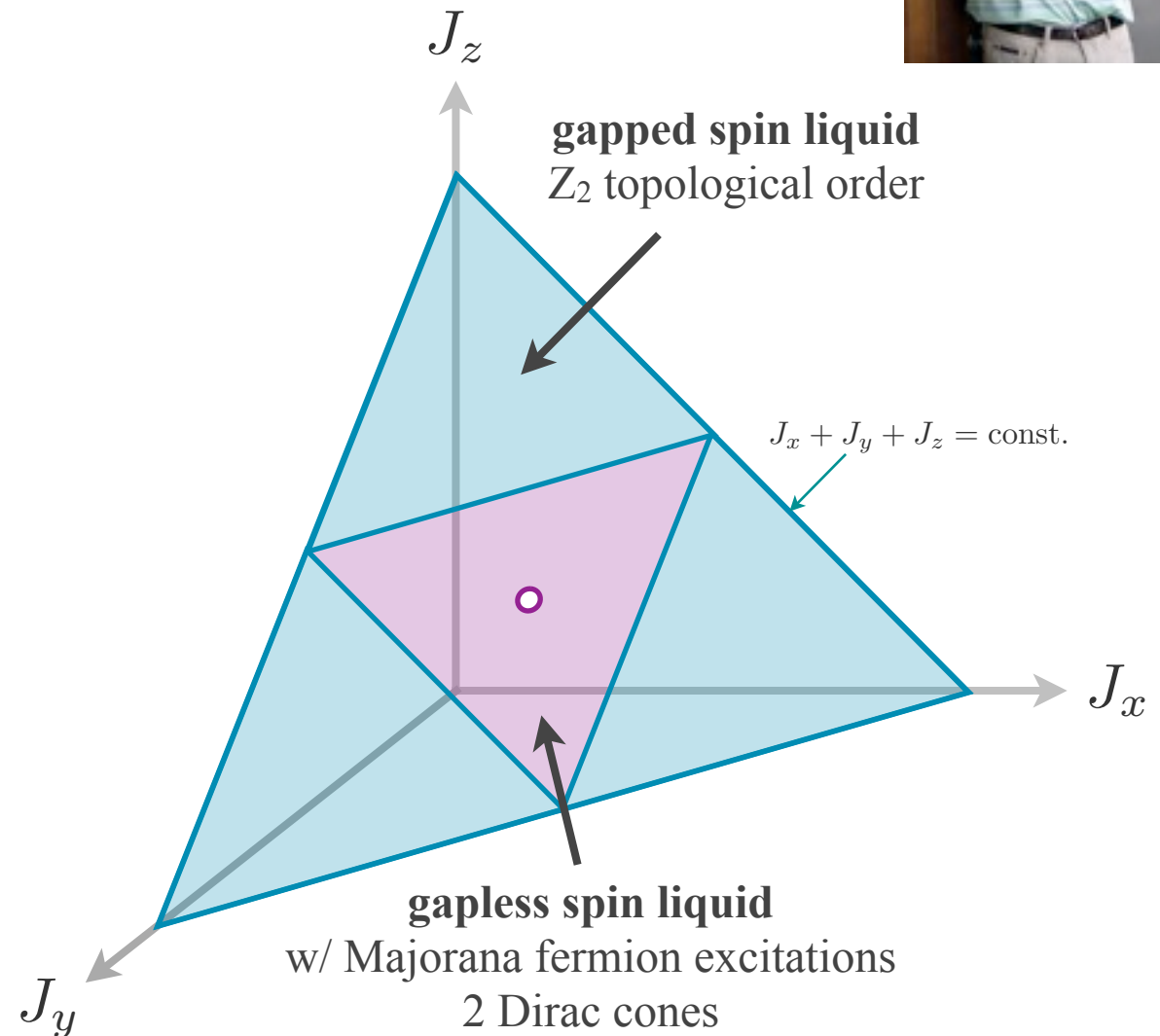


The Kitaev model



$$H_{\text{Kitaev}} = \sum_{\gamma\text{-links}} J_{\gamma} \sigma_i^{\gamma} \sigma_j^{\gamma}$$

Rare combination of a model of fundamental conceptual importance and an *exact* analytical solution.

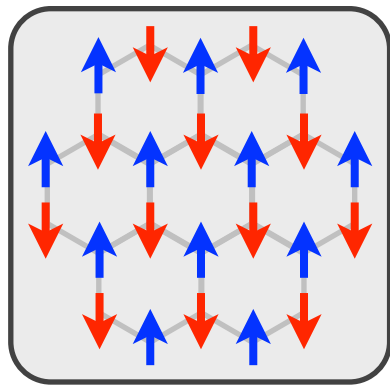


A. Kitaev, Ann. Phys. **321**, 2 (2006)

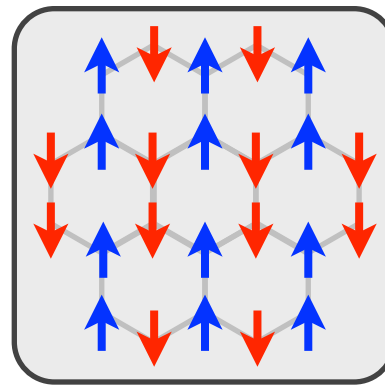
The Heisenberg-Kitaev model

The zero-temperature phase diagram

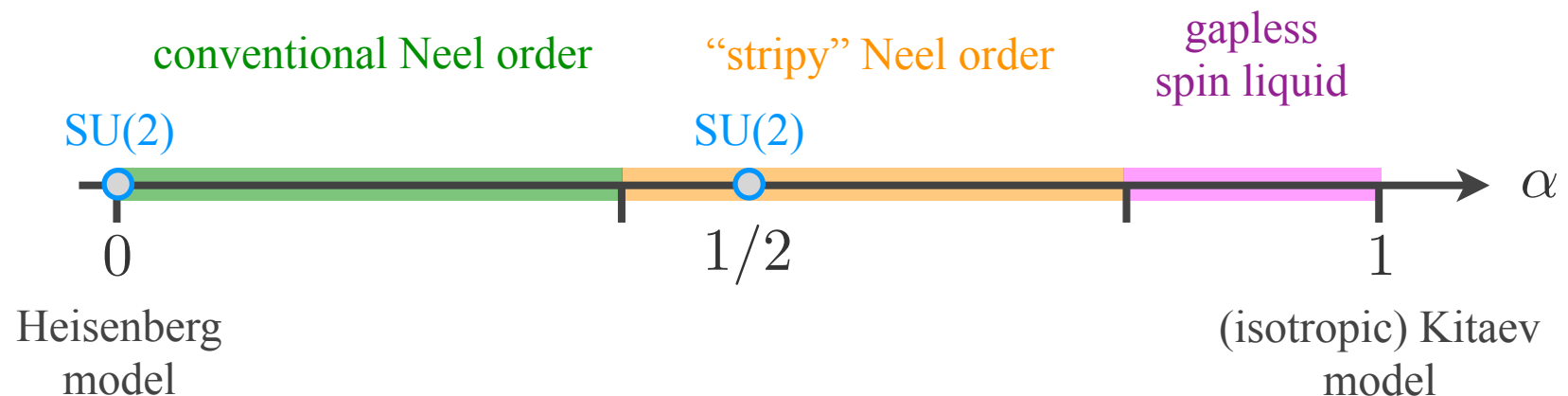
$$H_{\text{HK}} = (1 - \alpha) \sum_{\langle i,j \rangle} \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma\text{-links}} \sigma_i^\gamma \sigma_j^\gamma$$



conventional Neel order



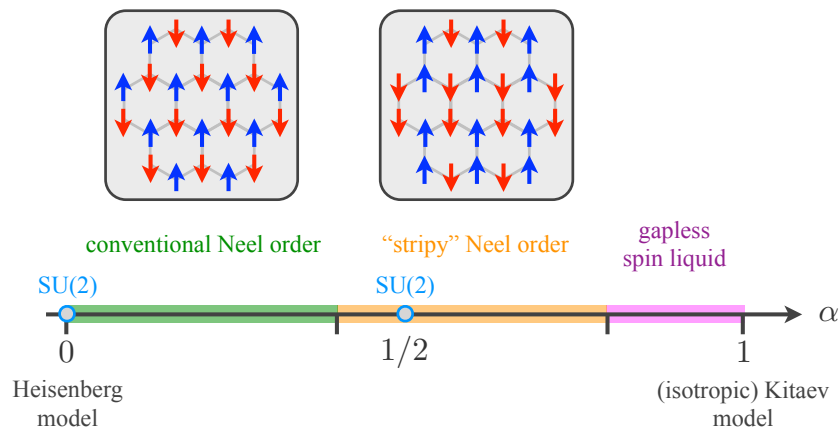
“stripy” Neel order



The Heisenberg-Kitaev model

The zero-temperature phase diagram

$$H_{\text{HK}} = (1 - \alpha) \sum_{\langle i,j \rangle} \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma\text{-links}} \sigma_i^\gamma \sigma_j^\gamma$$



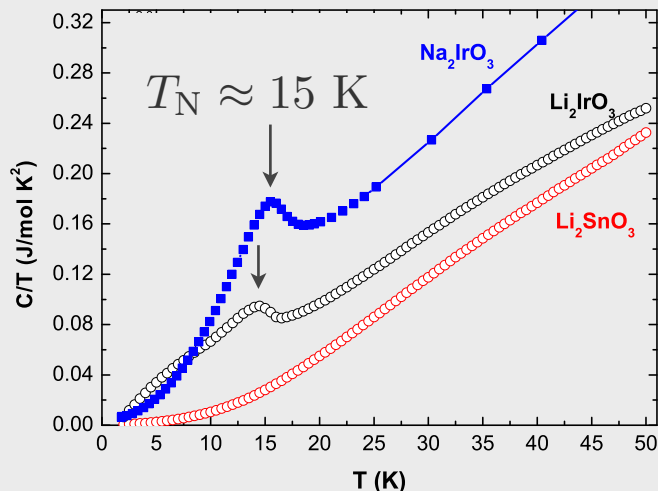
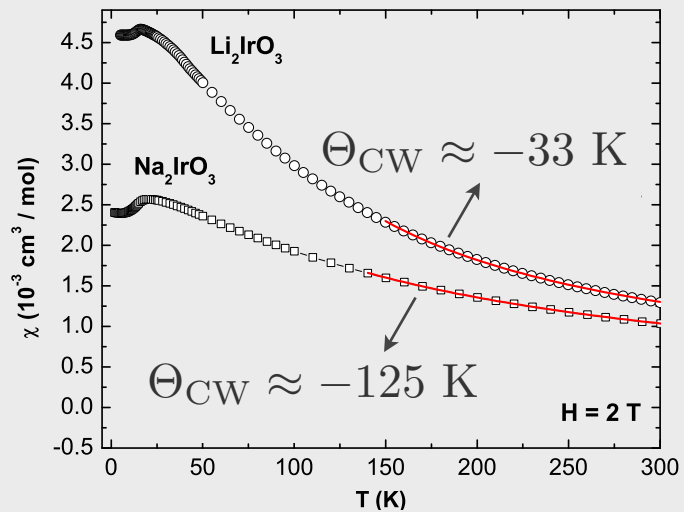
Open questions

T=0: Does this model reproduce the experimentally observed magnetic ordering?

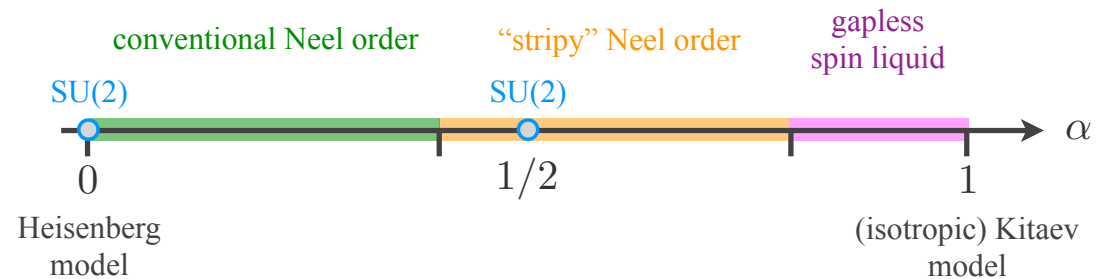
Finite T: Can we explain thermodynamic properties such as the ratio of Curie-Weiss and ordering temperature?

Magnetic field: How close are the experimental systems to even more exotic, topologically ordered ground states?

Thermodynamic properties



$$H_{\text{HK}} = (1 - \alpha) \sum_{\langle i, j \rangle} \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma\text{-links}} \sigma_i^\gamma \sigma_j^\gamma$$



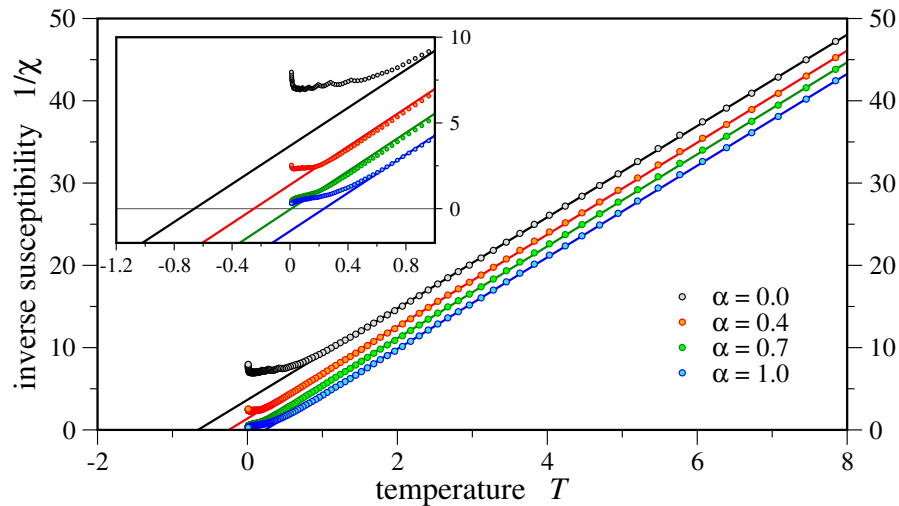
increasing frustration?

Our approach: functional renormalization group
We access finite-temperature physics by identifying the RG flow parameter with a temperature scale.

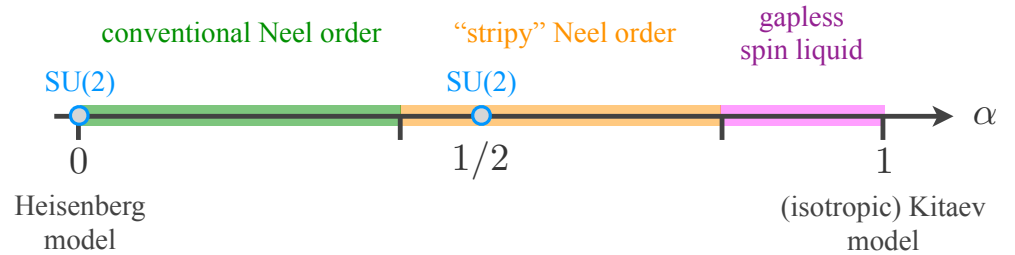
For details of this approach:
talk by Johannes Reuther Z8.00011
Friday afternoon 1:15pm

Thermodynamic properties

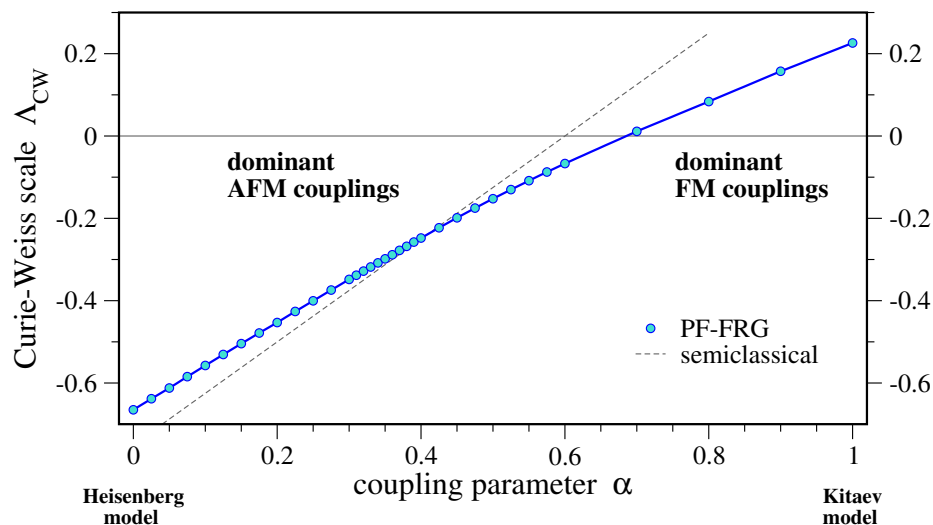
J. Reuther, R. Thomale, ST, PRB **84**, 100406(R) (2011).



$$H_{\text{HK}} = (1 - \alpha) \sum_{\langle i, j \rangle} \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma\text{-links}} \sigma_i^\gamma \sigma_j^\gamma$$

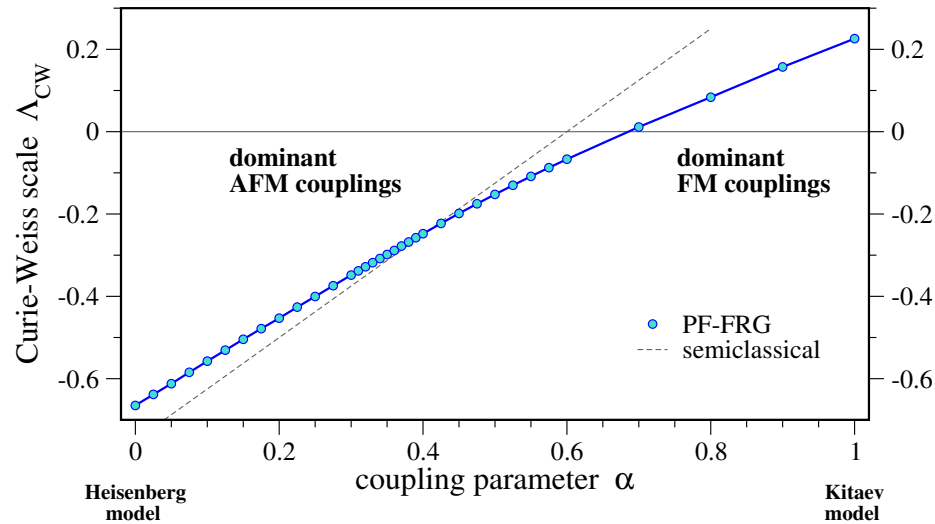


increasing frustration?

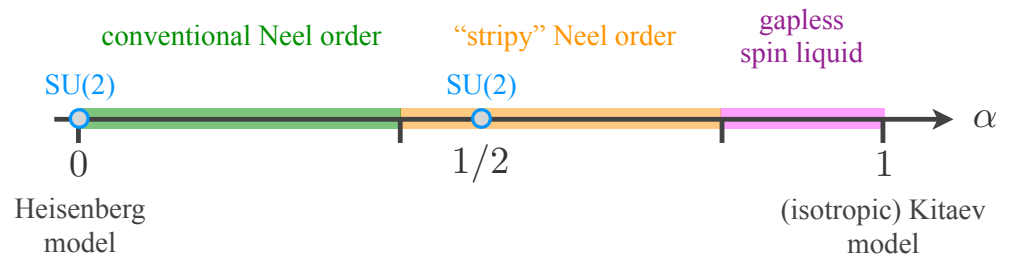


Thermodynamic properties

J. Reuther, R. Thomale, ST, PRB **84**, 100406(R) (2011).



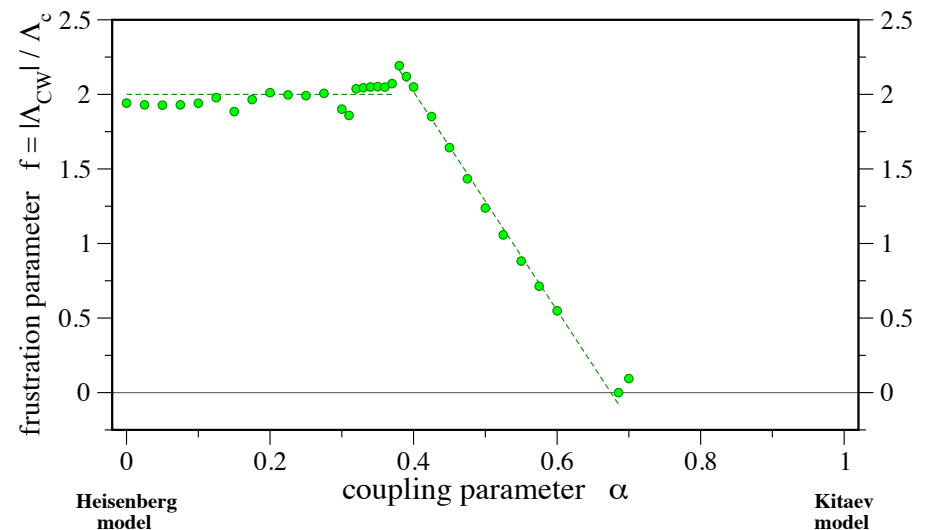
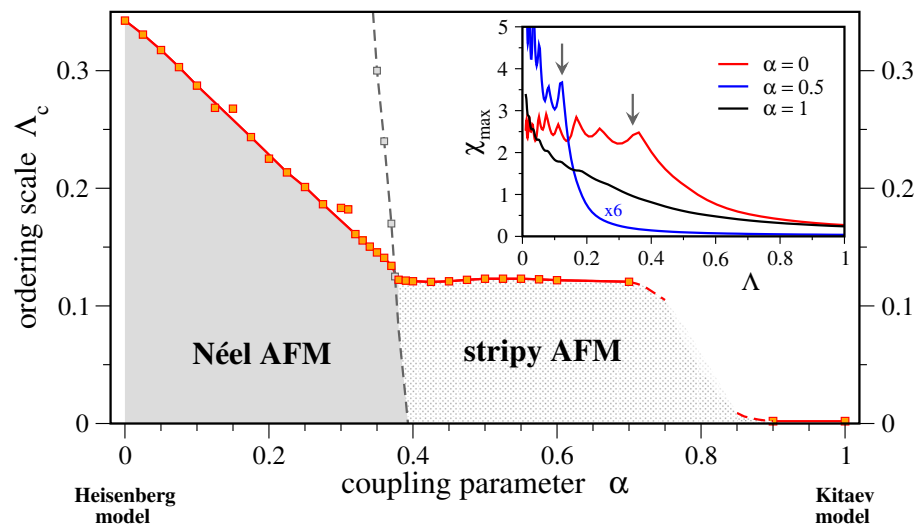
$$H_{HK} = (1 - \alpha) \sum_{\langle i,j \rangle} \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma\text{-links}} \sigma_i^\gamma \sigma_j^\gamma$$



increasing frustration?

No!

We need another mechanism to introduce frustration.



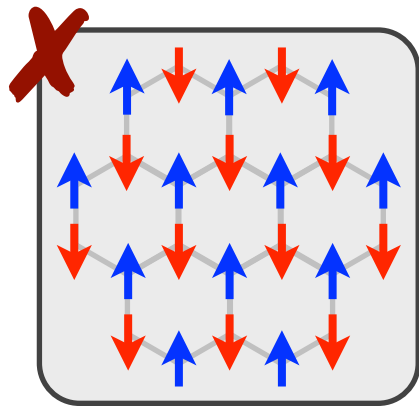
Magnetic order in experiments

X-ray and inelastic neutron scattering experiments on Na_2IrO_3 indicate **zig-zag** magnetic order.

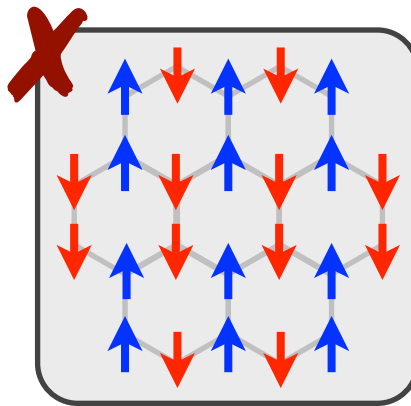
X. Liu *et al.*, PRB **83**, 220403(R) (2011)

S.K. Choi *et al.*, arXiv:1202.1268 (2012)

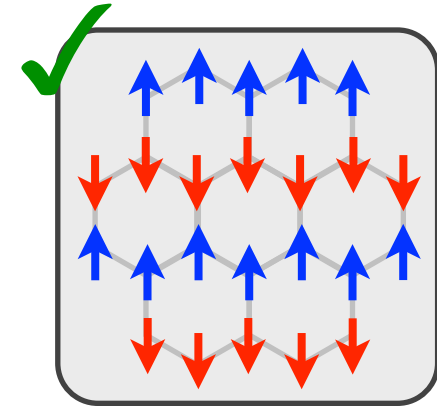
Y. Feng *et al.*, arXiv:1202.3995 (2012)



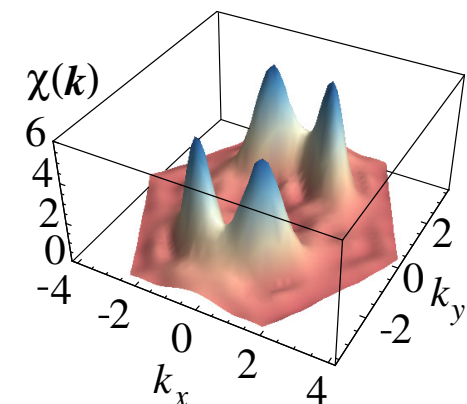
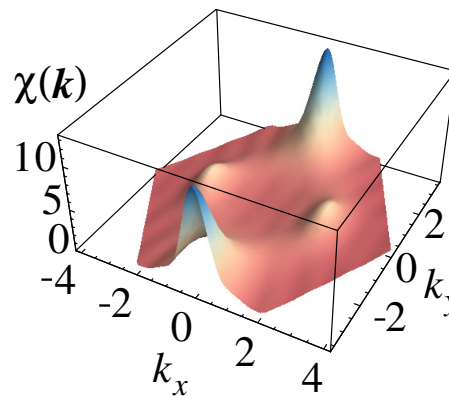
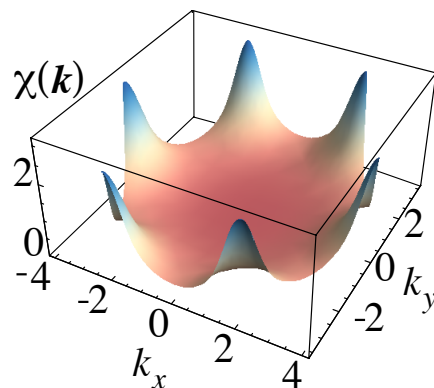
conventional Neel order



“stripy” order

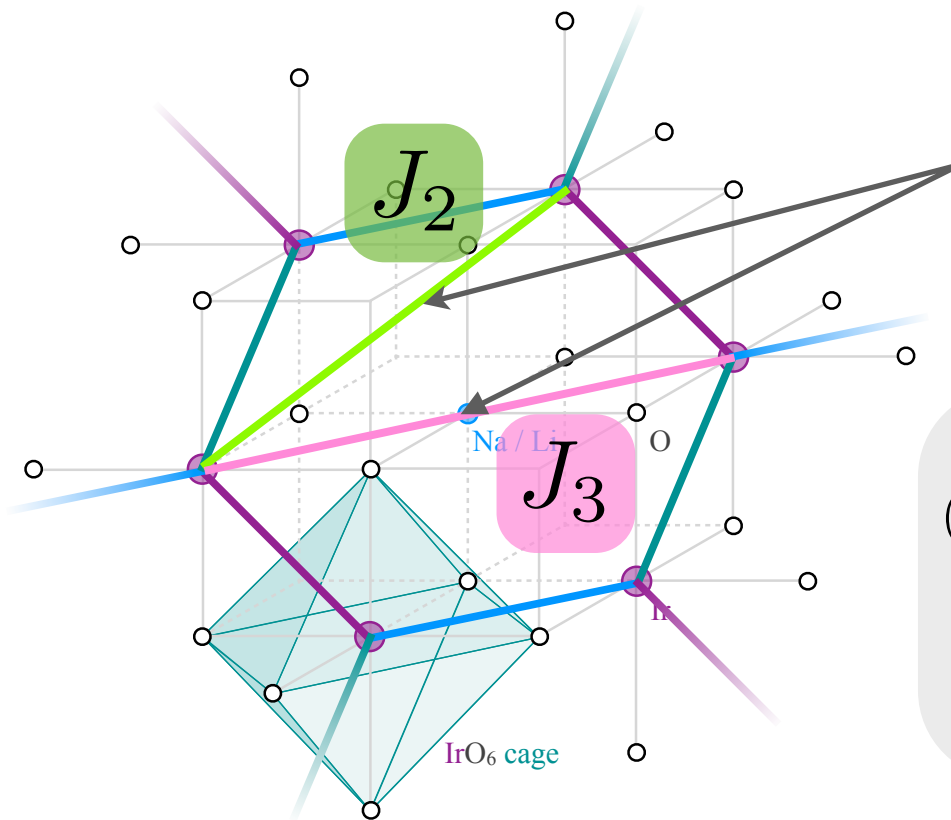


“zig-zag” order



Geometric frustration

Introduce **geometric frustration** by including next-nearest and 3rd-nearest neighbor interactions.



$$(1 - \alpha) \left(\sum_{\langle ij \rangle} + J_2 \sum_{\langle\langle i,j \rangle\rangle} + J_3 \sum_{\langle\langle\langle i,j \rangle\rangle\rangle} \right) \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma} \sigma_i^{\gamma} \sigma_j^{\gamma}$$

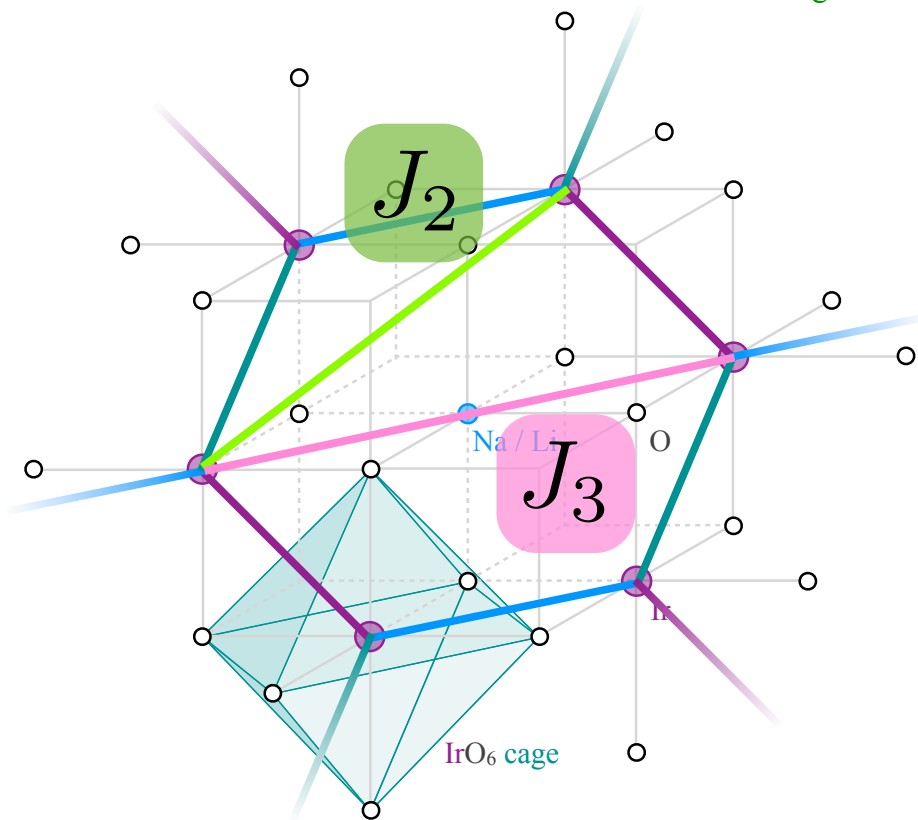
I. Kimchi and Y.-Z. You, PRB **84**, 180407(R) (2011)

The next-nearest neighbor coupling J_2 destabilizes the Neel state in favor of **spin spiral** states.

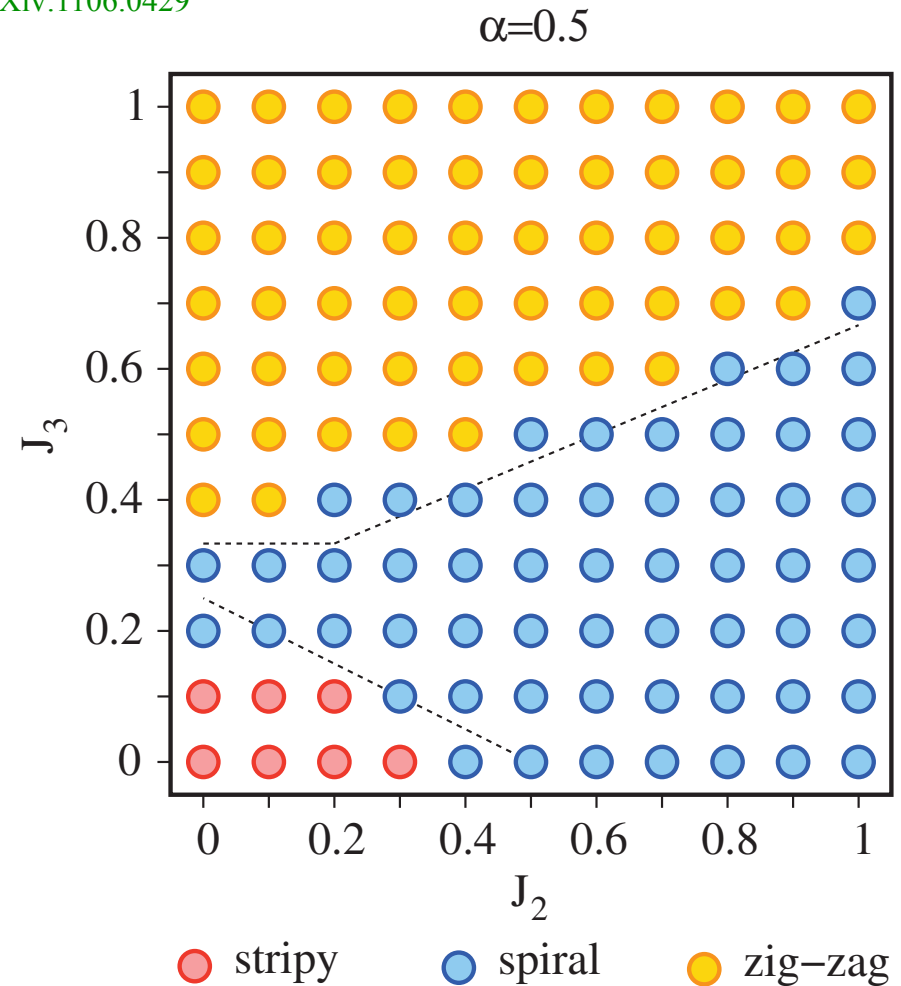
The 3rd-nearest neighbor coupling J_3 indeed favors **zig-zag** magnetic order.

Geometric frustration

Y. Singh *et al.*, arXiv:1106.0429



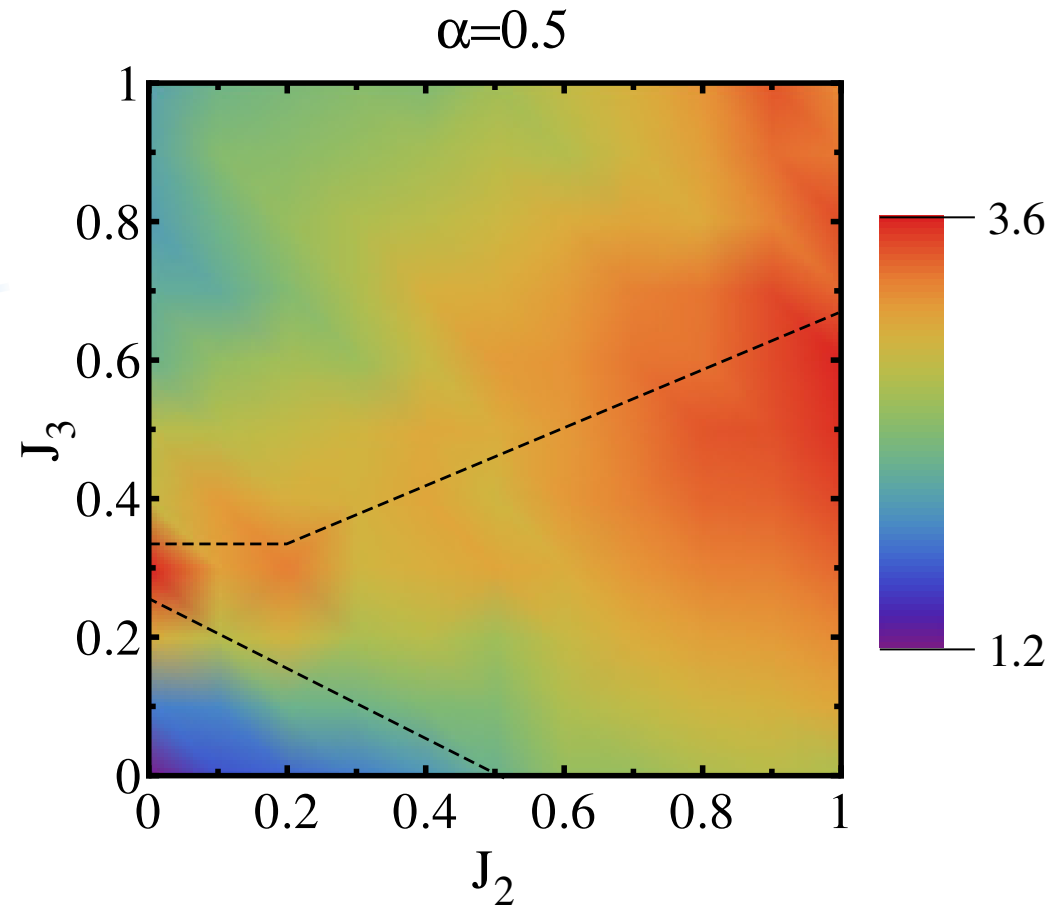
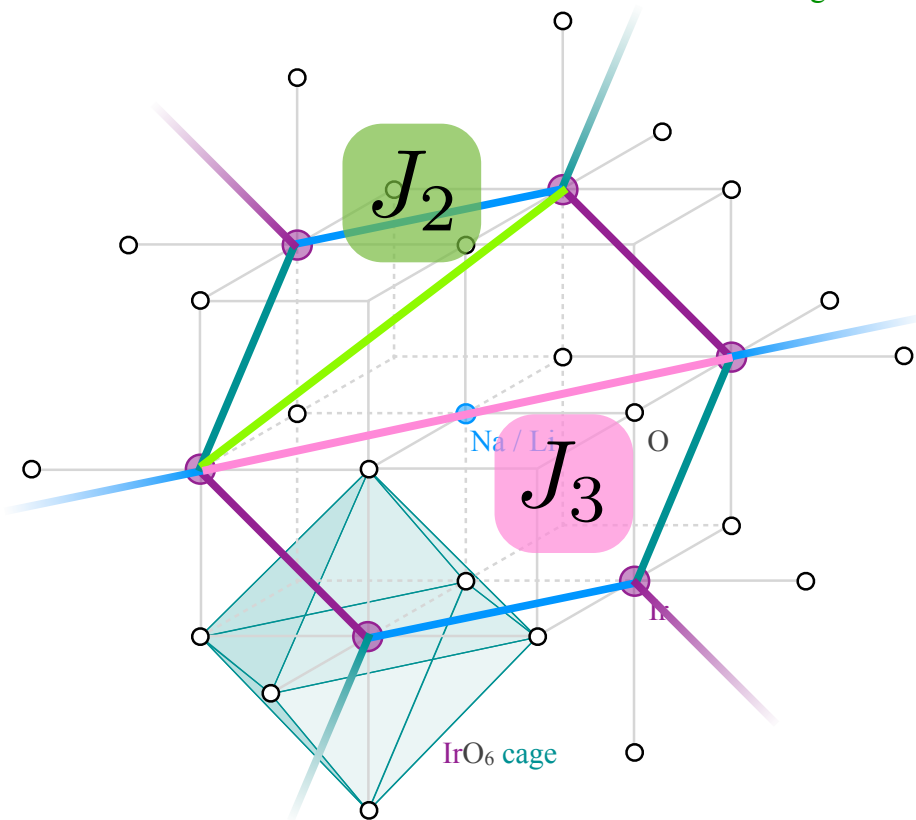
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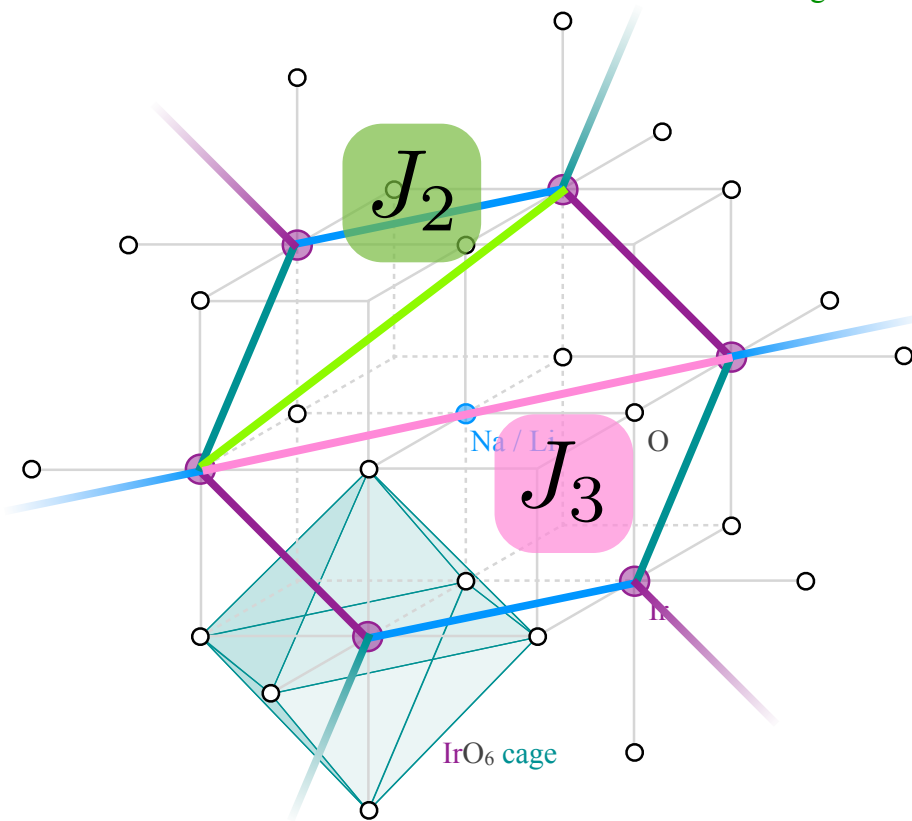


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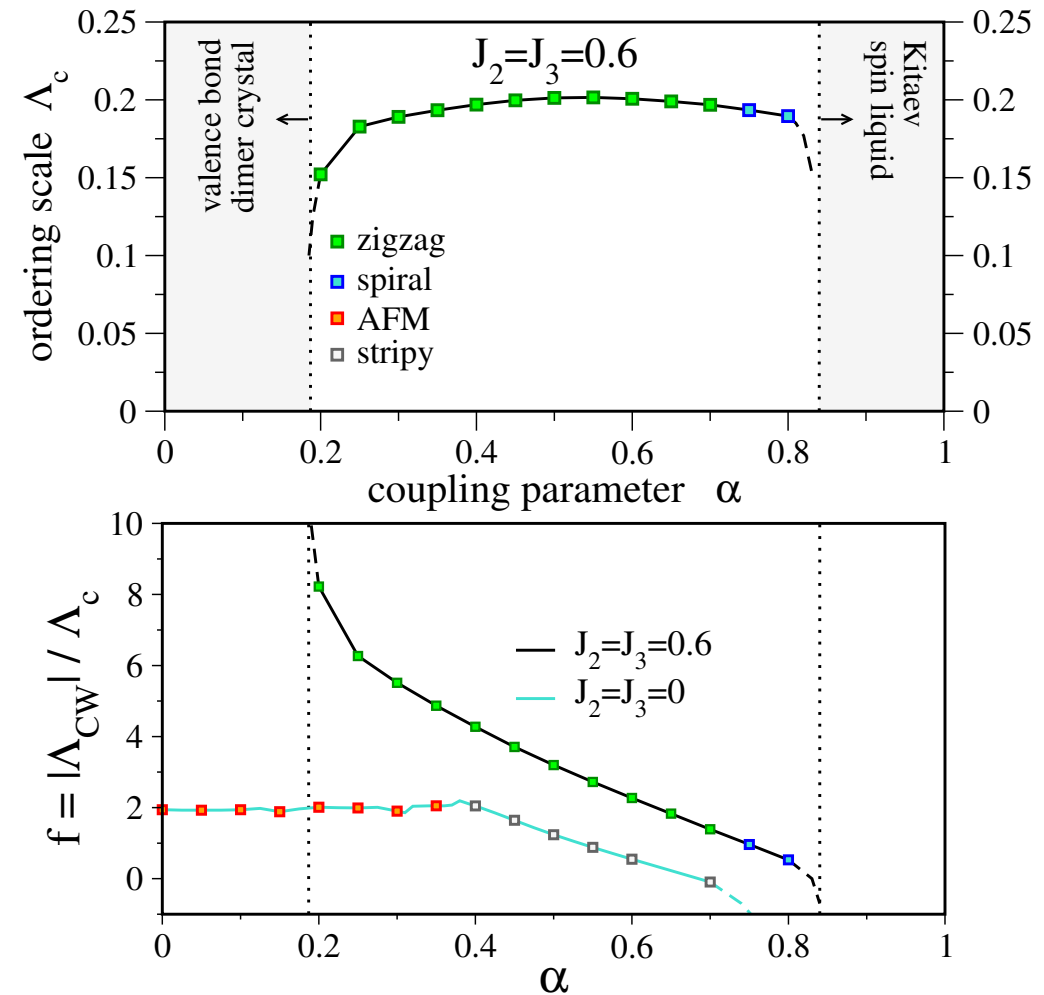
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The 3rd-nearest neighbor coupling J_3 indeed favors **zig-zag** magnetic order.

Microscopic parameter estimates

Y. Singh *et al.*, arXiv:1106.0429

Na₂IrO₃

$$\Theta_{\text{CW}} \approx -125 \text{ K}$$

$$T_{\text{N}} \approx 15 \text{ K}$$

zig-zag order



$$J_2/J_1 \approx 0.6$$

$$J_3/J_1 \approx 0.6$$

$$\alpha \approx 0.25$$

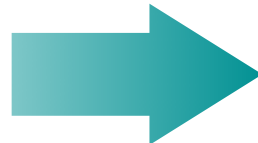
Heisenberg : Kitaev $\sim 3 : 2$

Li₂IrO₃

$$\Theta_{\text{CW}} \approx -33 \text{ K}$$

$$T_{\text{N}} \approx 15 \text{ K}$$

zig-zag order



$$J_2/J_1 \gtrsim 0.6$$

$$J_3/J_1 \gtrsim 0.6$$

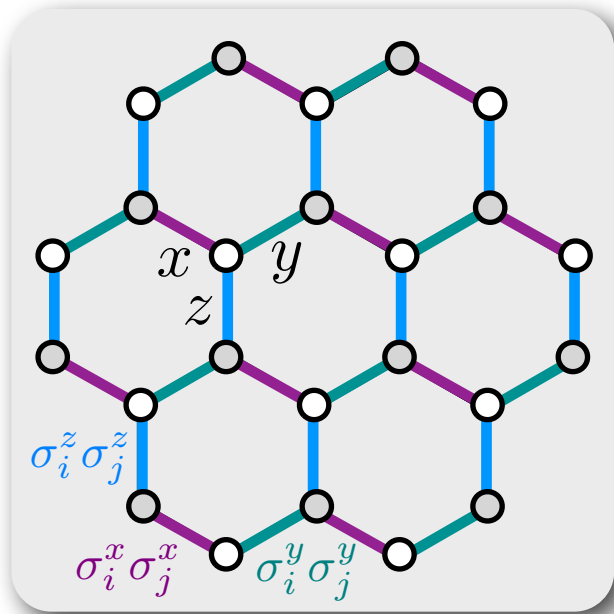
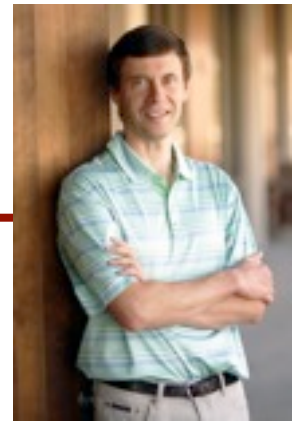
$$\alpha \gtrsim 0.65$$

Heisenberg : Kitaev $\sim 1 : 4$

The background is a dark teal color filled with a dense pattern of lighter teal circles of various sizes. Overlaid on this are several intricate, fractal-like patterns that resemble branching structures or complex, interconnected paths, also in shades of teal.

What next?

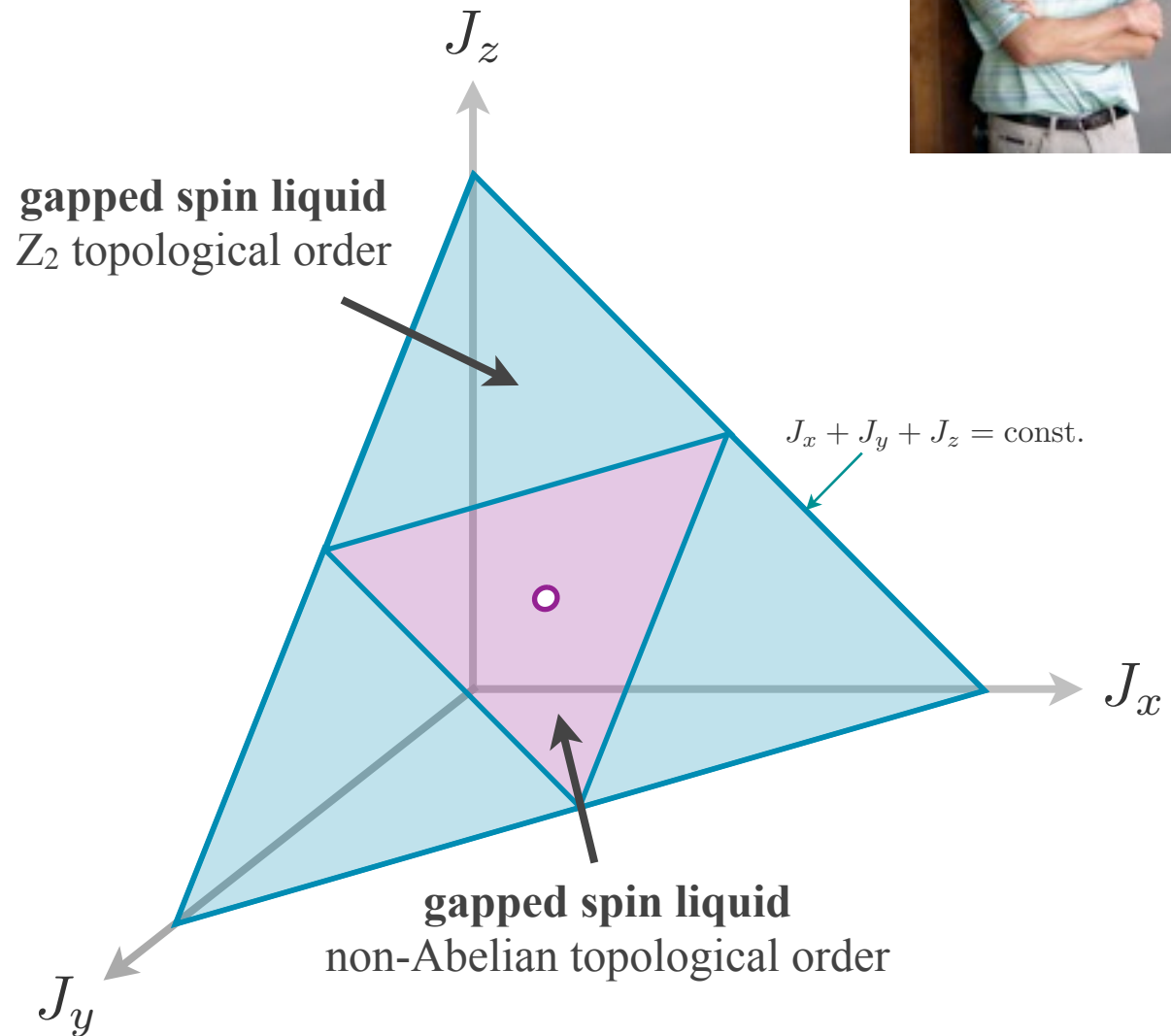
The Kitaev model + field



$$H_{\text{Kitaev+h}} = \sum_{\gamma\text{-links}} J_{\gamma} \sigma_i^{\gamma} \sigma_j^{\gamma}$$

$$-\sum_i \vec{h} \cdot \vec{\sigma}_i$$

$$\vec{h} = h(1, 1, 1)$$

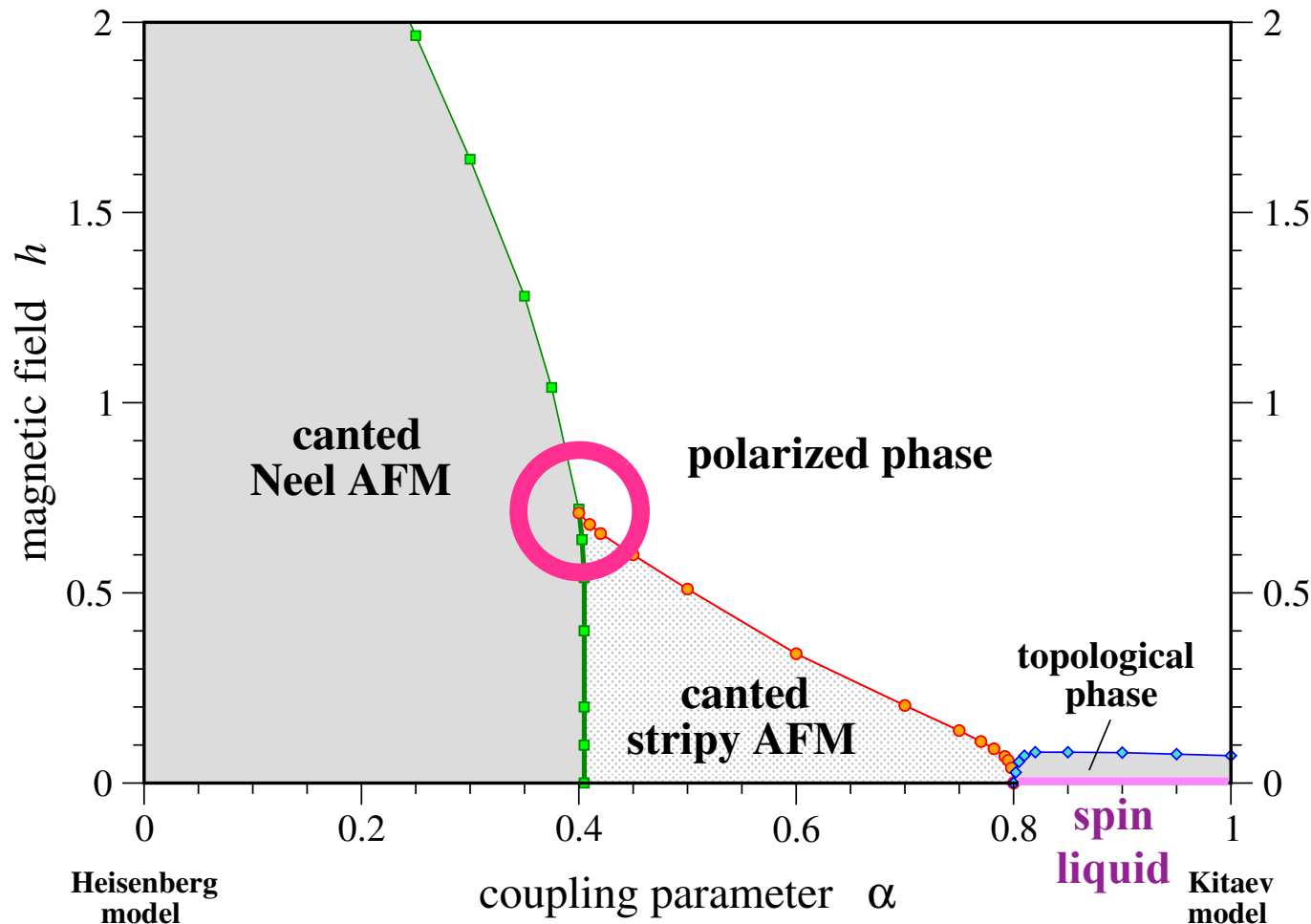


vortices are **Ising anyons** with **Majorana fermion** zero modes

Heisenberg-Kitaev model + field

H.-C. Jiang, Z.-C. Gu, X.-L. Qi., ST, PRB **83**, 245104 (2011).

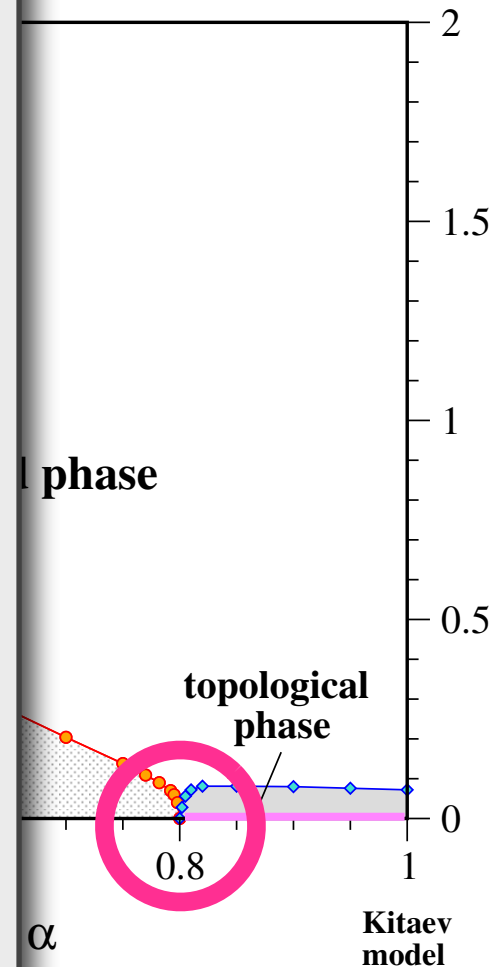
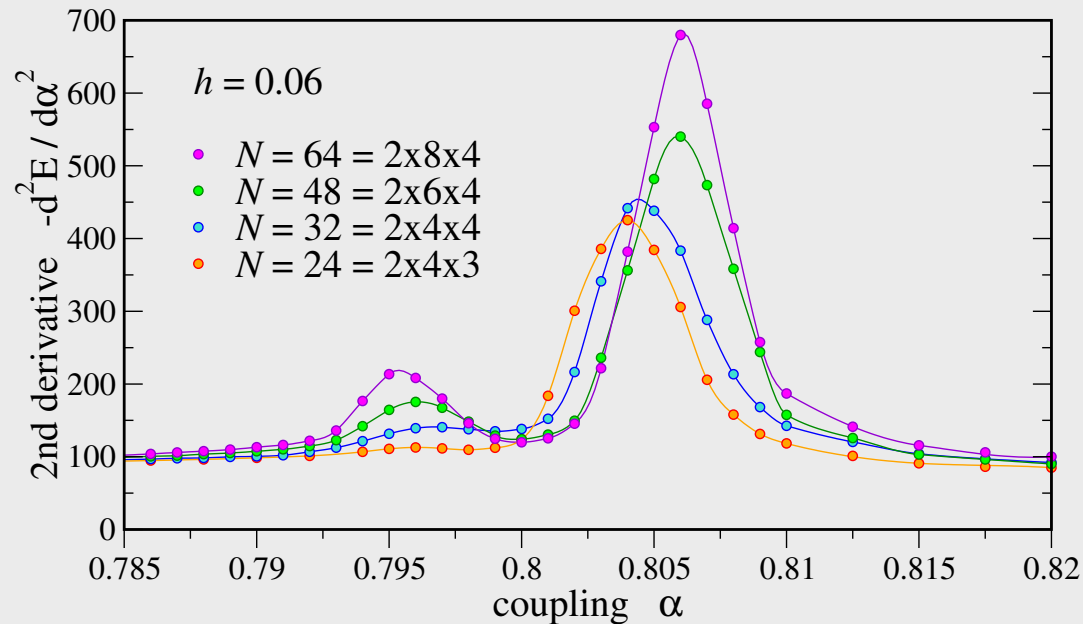
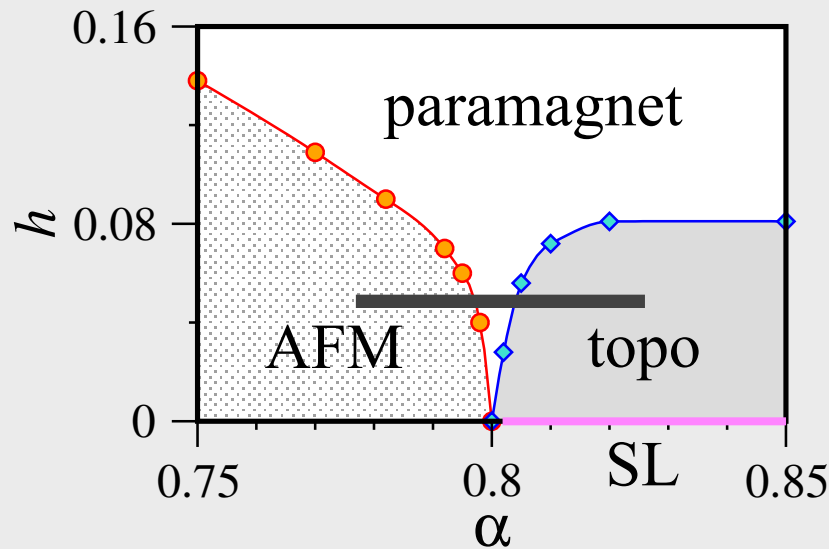
$$H_{\text{HK}} = (1 - \alpha) \sum_{\langle i,j \rangle} \vec{\sigma}_i \cdot \vec{\sigma}_j - 2\alpha \sum_{\gamma\text{-links}} \sigma_i^\gamma \sigma_j^\gamma - \sum_i \vec{h} \cdot \vec{\sigma}_i$$



Heisenberg-Kitaev model + field

H.-C. Jiang, Z.-C. Gu, X.-L. Qi., ST, PRB **83**, 245104 (2011).

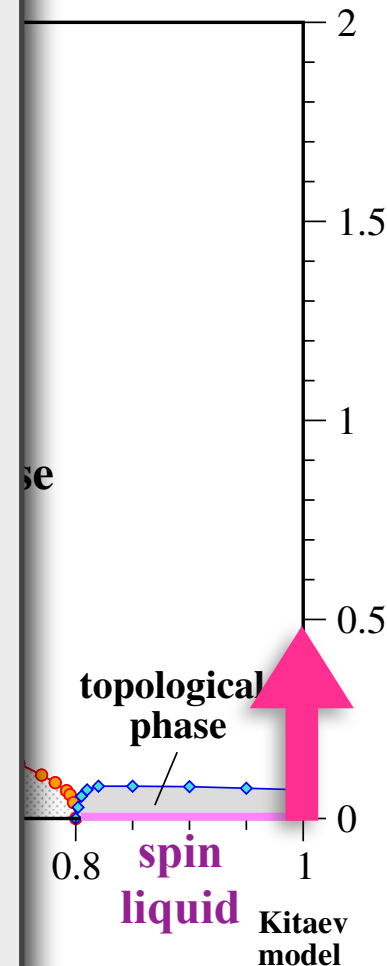
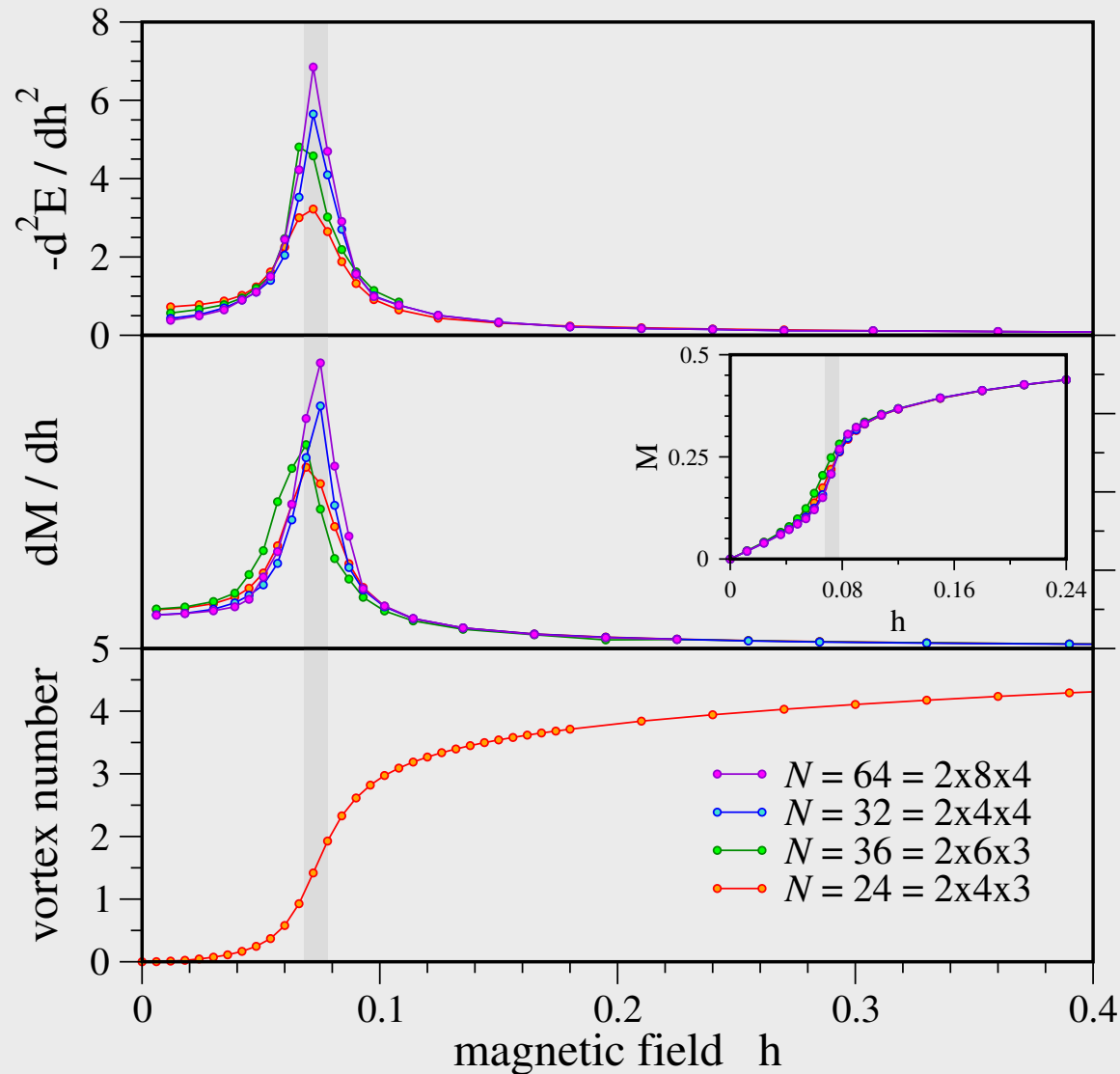
$$\sum_{\langle i,j \rangle} \sigma_i^\gamma \sigma_j^\gamma - \sum_i \vec{h} \cdot \vec{\sigma}_i$$



Heisenberg-Kitaev model + field

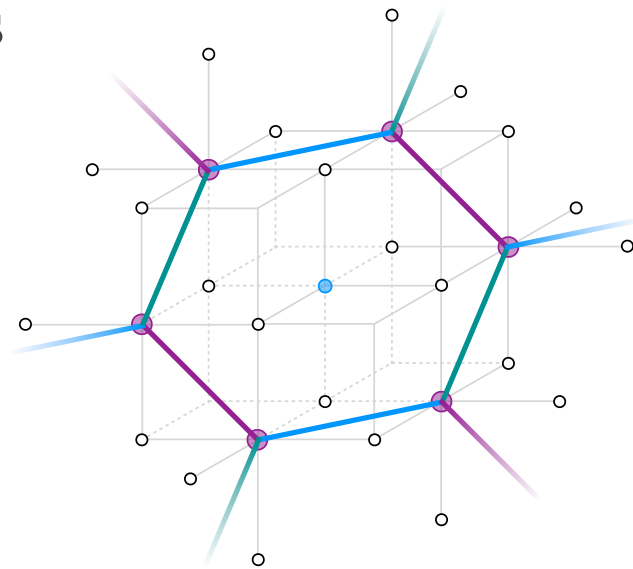
H.-C. Jiang, Z.-C. Gu, X.-L. Qi., ST, PRB **83**, 245104 (2011).

$$\sigma_i^\gamma \sigma_j^\gamma - \sum_i \vec{h} \cdot \vec{\sigma}_i$$



Summary

- Spin-orbit coupling in correlated electron materials can lead to a plethora of novel electronic states
 - spin-orbital ordered states
 - spin liquids
 - topological order
 - ...
- 5d transition metal oxides, particularly Iridates (Osmates?), offer a first glimpse of such spin-orbit entangled collective states.
- $(\text{Na,Li})_2\text{IrO}_3$ show signs of spin-orbital order, but the Li-system might be close to even more exotic states.



J. Reuther, R. Thomale, ST, PRB **84**, 100406(R) (2011).
H.-C. Jiang, Z.-C. Gu, X.-L. Qi., ST, PRB **83**, 245104 (2011).
Y. Singh *et al.*, arXiv:1106.0429