

$$H = -t \sum_{\langle i,j \rangle} (a_i^\dagger a_j + a_j^\dagger a_i) + V_2 \sum_{\langle \langle i,k \rangle \rangle} n_i n_k - \mu \sum_i n_i$$