

$$Z = \text{Tr} \, e^{-\beta H} = \sum_{n=0}^{\infty} \frac{\beta^n}{n!} \text{Tr} \, (-H)^n = \sum_{n=0}^{\infty} g(n) \, \beta^n$$