

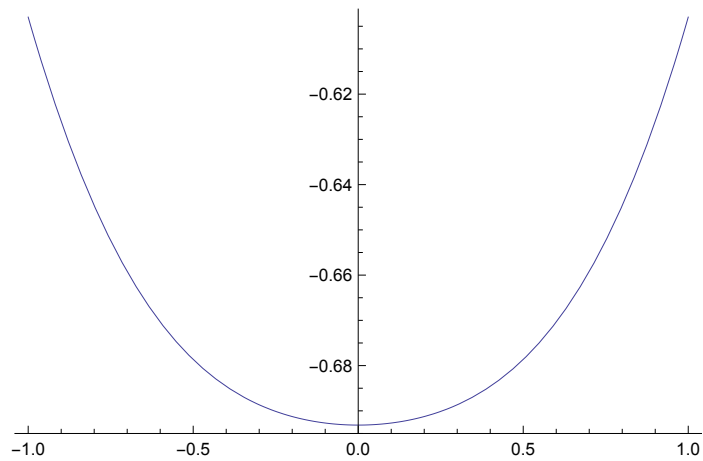
(\*this Mathematica notebook evaluates the free energy function  
of the Weiss ferromagnet (mean field ferromagnet) with  $J=1$  \*)

(\*  $Z = \exp\{-N \beta f(\beta, h)\} = \int dm \exp\{-N \beta f(\beta, h, m)\}$  \*)  
(\* we consider  $\beta f(\beta, h, m)$ , denoted by  $\beta f$  \*)

$\beta f[\beta_, h_, m_] := \beta m^2/2 - \text{Log}[2 \text{Cosh}[\beta m + \beta h]]$

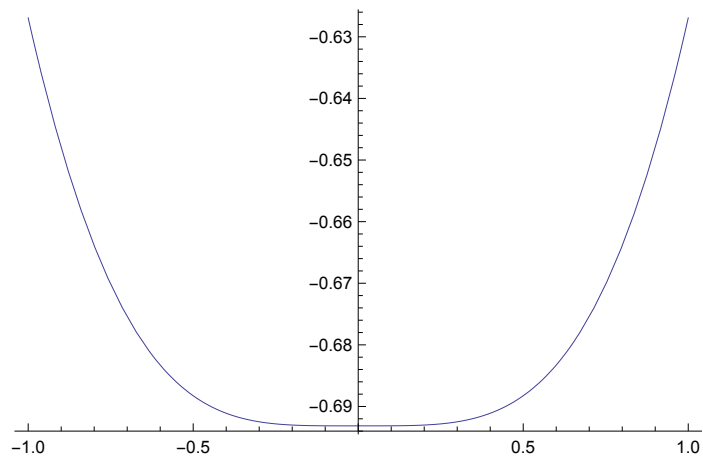
(\* first we plot  $\beta f$  as a function of  $m$  in the high temperature phase,  
 $\beta = 0.9 < \beta_c = 1$  \*)

`Plot[ $\beta f[.9, 0, m]$ , {m, -1, 1}]`

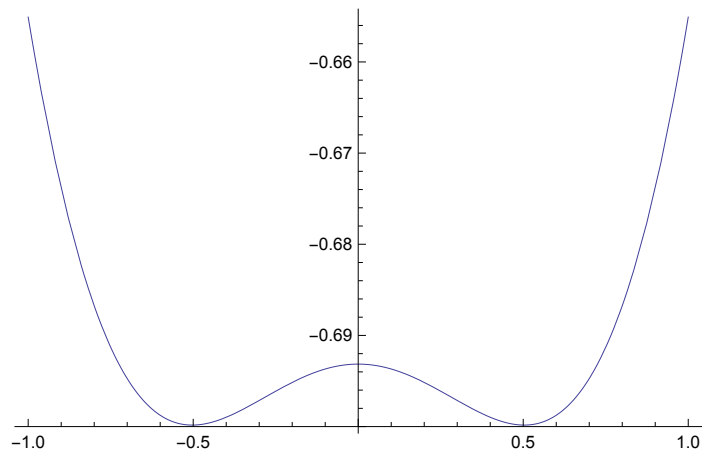


(\*at the critical temperature  $\beta = \beta_c = 1$ \*)

`Plot[ $\beta f[1, 0, m]$ , {m, -1, 1}]`



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(*in the low temperature phase, beta=1.1>beta_c=1*)
Plot[betaf[1.1, 0, m], {m, -1, 1}]
```



(\*explore the free energy function yourself by tuning beta and h.

Initially beta is set to the critical value beta=1 and h=0\*)

(\*for instance, what happens if you turn on a magnetic field,  
either below  $T_c$  or above  $T_c$  ? \*)

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Animate[Plot[betaf[beta, h, m], {m, -1, 1}], {{beta, 1}, 0.1, 2}, {{h, 0}, -.5, .5},
], AnimationRunning -> False]
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